

Advanced Study Institute (ASI) on
Science and Application of Spin Electronics
Hongkong, 15.8.2005

25 Years Quantum (not Spin) Hall Effect



K. v. Klitzing

**Max-Planck-Institut für
Festkörperforschung
Stuttgart**

FIRST PUBLICATION ABOUT THE QUANTUM HALL EFFECT

25 years + 4 days →

11 AUGUST 1980

VOLUME 45, NUMBER 6

PHYSICAL REVIEW LETTERS

11 AUGUST 1980

New Method for High-Accuracy Determination of the Fine-Structure Constant Based on Quantized Hall Resistance

K. v. Klitzing

*Physikalisches Institut der Universität Würzburg, D-8700 Würzburg, Federal Republic of Germany, and
Hochfeld-Magnetlabor des Max-Planck-Instituts für Festkörperforschung, F-38042 Grenoble, France*

and

G. Dorda

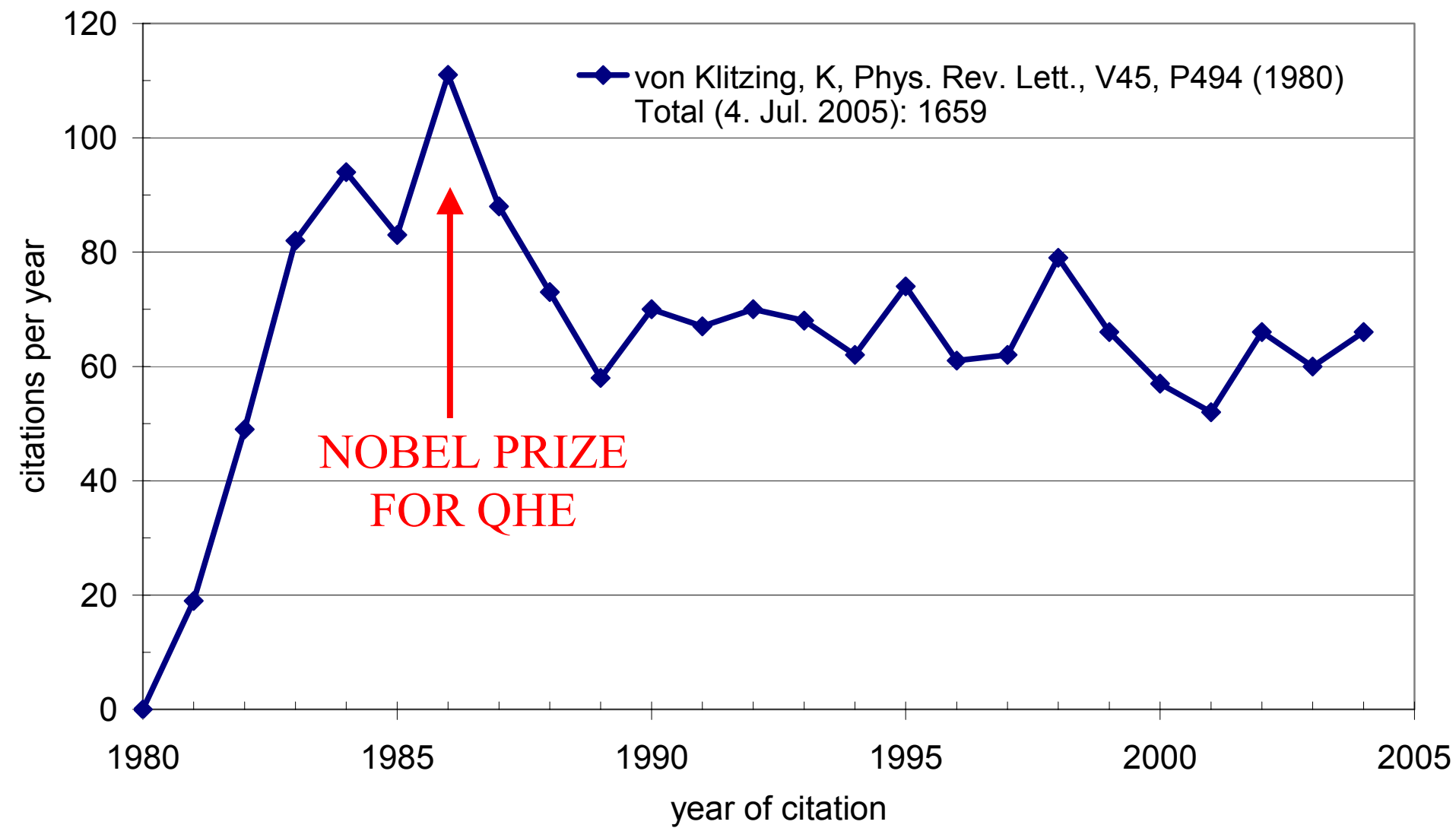
Forschungslaboratorien der Siemens AG, D-8000 München, Federal Republic of Germany

and

M. Pepper

Cavendish Laboratory, Cambridge CB3 0HE, United Kingdom

(Received 30 May 1980)



Integer Quantum Hall Effect (Nobel Prize in Physics 1985)

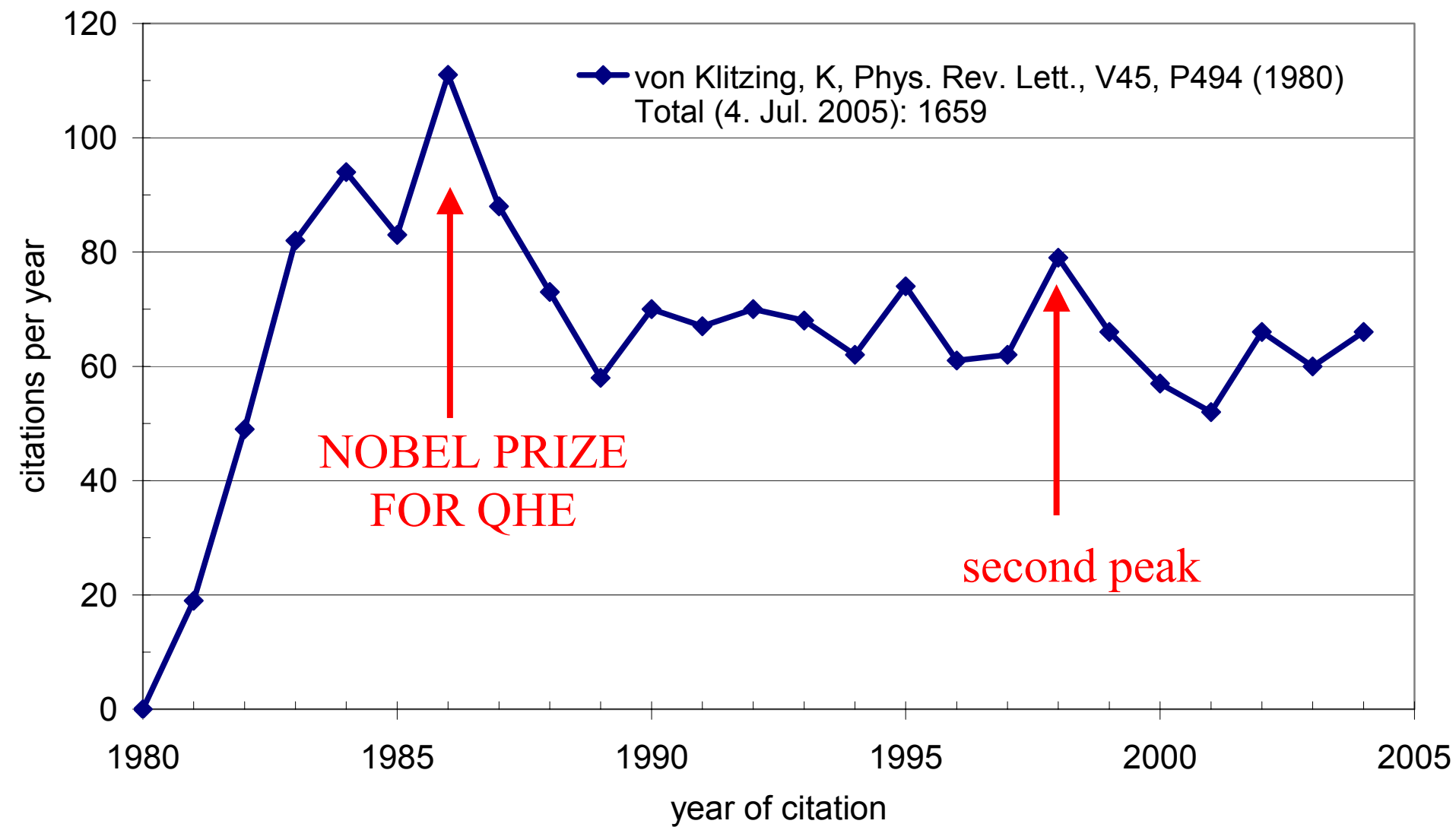
*Kungliga
Svenska Vetenskapsakademien
har den 16 oktober 1985 beslutat att med det
NOBELPRIS
som detta år tillerkännes den
som inom fysikens område
gjort den viktigaste upptäckten eller
uppfinningen belöna
Klaus von Klitzing
för upptäckten av den kvantiserade
Halleffekten*

STOCKHOLM DEN 10 DECEMBER 1985

Se/Johnson

And-Ganelius





Fractional Quantum Hall Effect (Nobel Prize in Physics 1998)



The Integral and Fractional Quantum Hall Effects

Edited by
C.T. Van Driel
M.E. Ca
S.M. Gir

$$R_K = h/e^2$$

$T = 278 \text{ mK}$
 $I = 0.255 \mu\text{A}$

D. Yoshioka The Quantum Hall Effect

SOLID-STATE SCIENCES

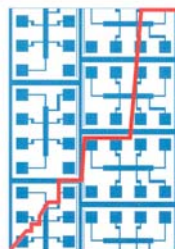


Springer

GRADUATE TEXTS IN CONTEMPORARY Physics

The Quantum Hall Effect

Physikalisch
Technische
Bundesanstalt
Braunschweig und Berlin



3. Auflage, Nov. 1998 PIB

email: presse@ptb.de
WWW: http://www.ptb.de/

M. Janßen, O. Viehweger
U. Fastenrath and J. Hajdu

Introduction to the Theory of the Integer Quantum Hall Effect

Composite Fermions

A Unified View of
the Quantum Hall Regime

Editor
O. Heinonen

World Scientific

Introduction to Quantum Hall Effect

Proceedings of the International Symposium

"Quantum Hall Effect: Past, Present and Future"

Stuttgart, Germany
2-5 July 2003



Editors

Rolf Haug
Dieter Weiss



astava

T.Chakraborty
P.Pietiläinen

The Quantum Hall Effects

Fractional and Integral

Second Edition

Quantum Hall Effects

Field Theoretical Approach
and Related Topics



Zyuan F. Ezawa

Quantum Hall Effects

Novel Quantum Liquids
in Low-Dimensional
Semiconductor Structures

Edited by
Sankar Das Sarma
Aron Pinczuk

QUANTUM HALL EFFECT

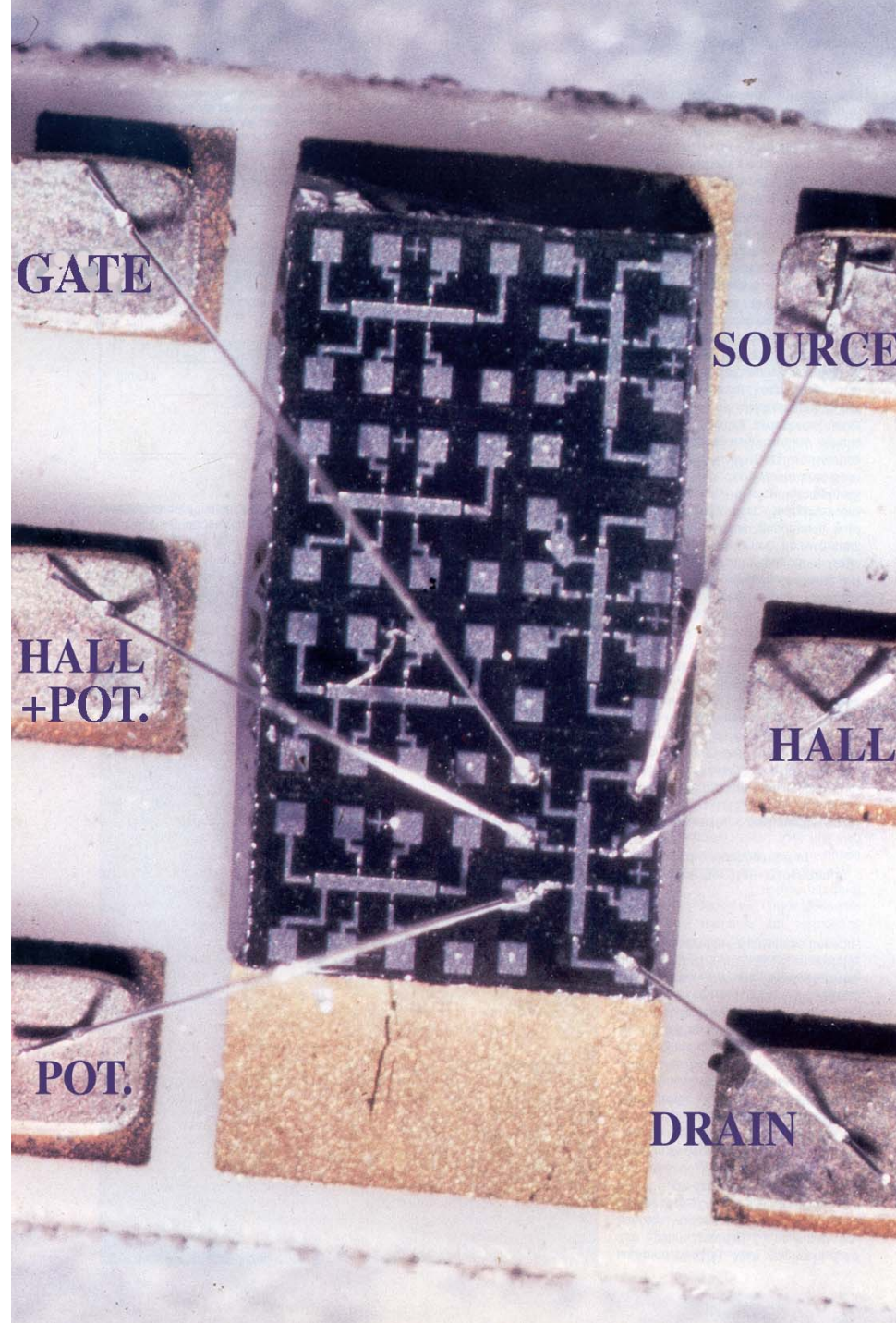
Editor
MICHAEL STONE

World Scientific

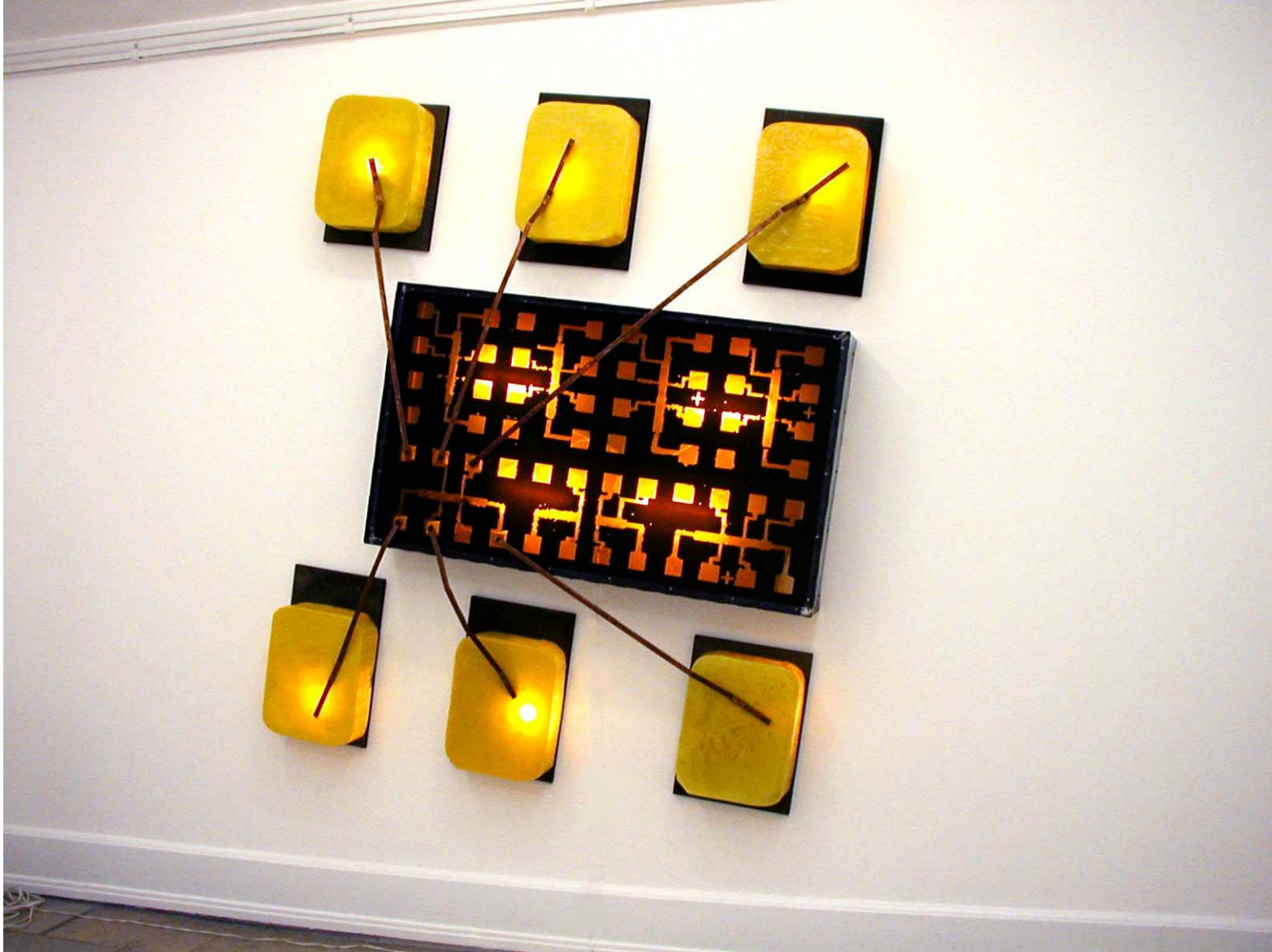


Si MOSFET

basic research on
such a device led
to the discovery
of the
Quantum Hall
Effect



Quantum Hall Effect in the Museum



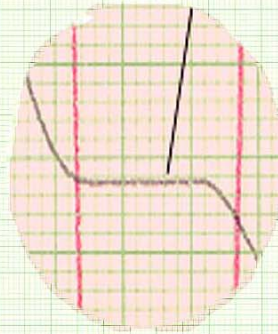
Exhibitions in Nürnberg and Basel

5.2.1980 BIRTHDAY OF QHE (at 2 a.m.)

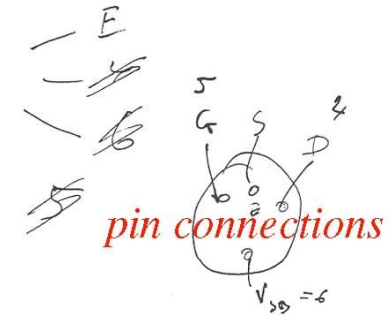
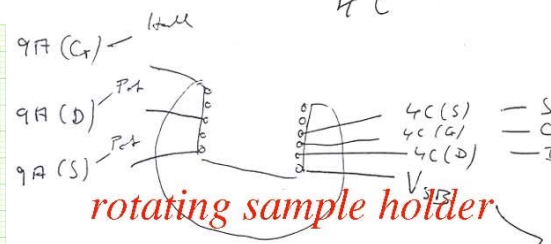
Resistance at B=0

Resistance at B=19.8 T

Hallresistance



GATEVOLTAGE



$$E_H = R_H \cdot D \cdot j = \frac{1}{n \cdot e} \cdot B \cdot \frac{I}{b}$$

$$U_H = \frac{B}{n \cdot e} \cdot I$$

$$N = \frac{eB}{2\pi k} \quad (g_s g_v = 1)$$

$$U_H = \frac{2\pi k B \cdot I}{e \cdot e \cdot B} = \left(\frac{h}{e^2} \cdot I \right)$$

25,76 kΩ
25813

Josephson

$$\frac{e^2}{h} \sqrt{\frac{h}{e^2}} = \frac{h}{e^2}$$

$$R_{KH} = \frac{1}{2} \alpha \cdot \sqrt{\frac{\mu_0}{\epsilon_0}} \Rightarrow 25813 \Omega$$

$$\mu_0 = 4\pi \cdot 10^{-9} \frac{Vs}{Ac}$$

$$\epsilon_0 = 0.8854 \cdot 10^{-12} \frac{As}{Vm}$$

$$\sqrt{\frac{\epsilon_0}{\mu_0}} = 2.65 \cdot 10^{-3} \Omega^{-1}$$

$$\sqrt{\frac{\mu_0}{\epsilon_0}} = 376.7 \Omega$$

notes of the phone call to PTB
PTB 531/5929 (5.2.1980)
2240

Prof. V. Kose

10⁻⁶

12945

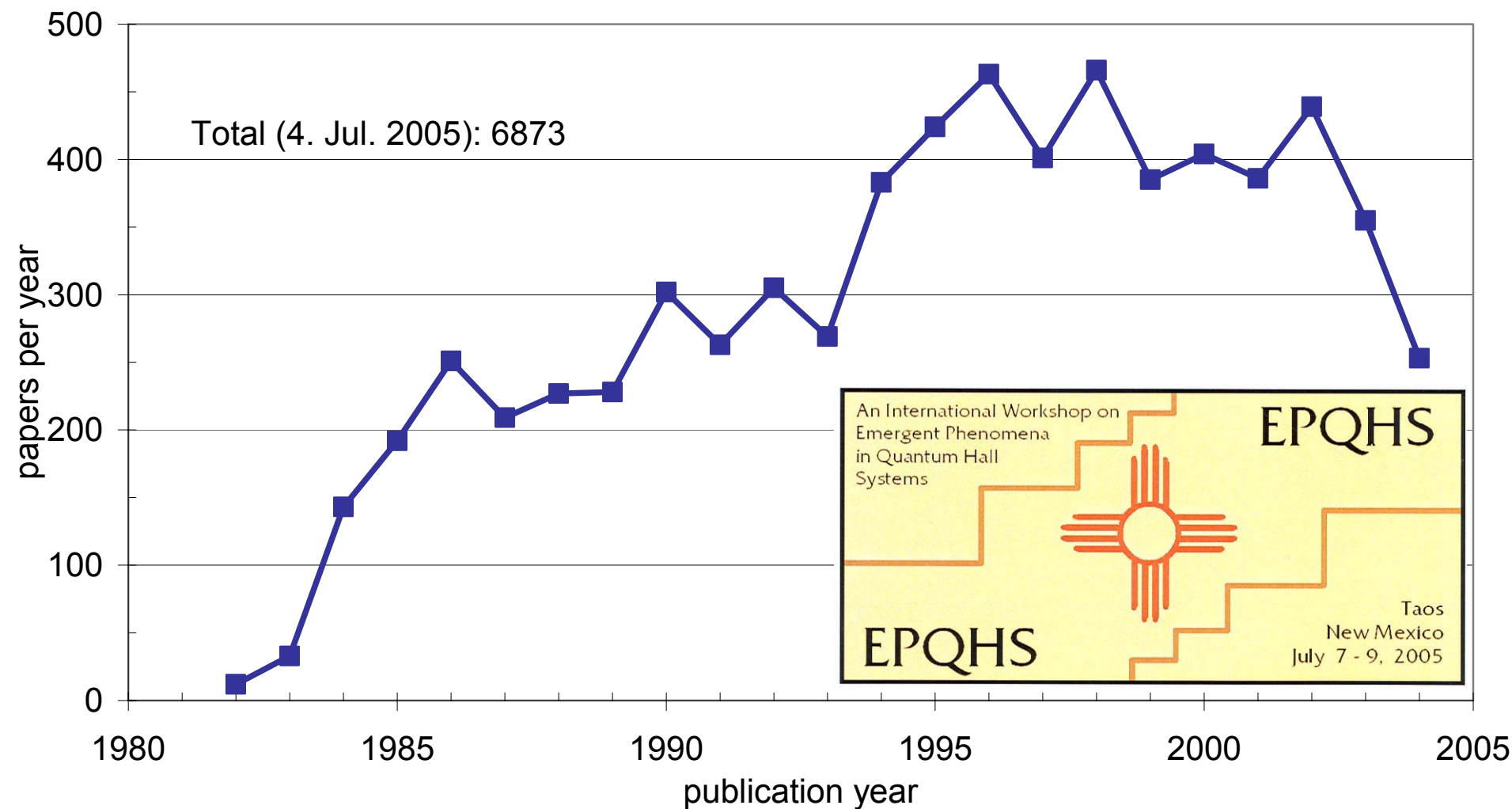
6 · 10⁻²

10⁻⁵ 12907

25813 Ω : N	25813	→	25163.46
1 MΩ parallel	12906.5		12742.04
	6453.25		6411.87
	3226.63		3216.25
	2151.08		2146.47

quantized resistances
with and without the
input resistance of the x-y recorder

Quantum Hall Effect papers in INSPEC



The quantum Hall effect-
a phenomenon for
(nearly) all area in physics

QUANTUM HALL EFFECT and BLACK HOLES

Edge States in Gravity and Black Hole Physics

A.P. Balachandran, L. Chandar, Arshad Momen

*Department of Physics, Syracuse University,
Syracuse, NY 13244-1130, U.S.A.*

Abstract

We show in the context of Einstein gravity that the removal of a spatial region leads to the appearance of an infinite set of observables and their associated edge states localized at its boundary. Such a boundary occurs in certain approaches to the physics of black holes like the one based on the membrane paradigm. The edge states can contribute to black hole entropy in these models. A “complementarity principle” is also shown to emerge whereby certain “edge” observables are accessible only to certain observers. The physical significance of edge observables and their states is discussed using their similarities to the corresponding quantities in the quantum Hall effect. The coupling of the edge states to the bulk gravitational field is demonstrated in the context of (2+1) dimensional gravity.

BTZ black hole and quantum Hall effect in the bulk/boundary dynamics

Y. S. Myung

Department of Physics, Inje University, Kimhae 621-749, Korea

Abstract

We point out an interesting analogy between the BTZ black hole and QHE (Quantum Hall effect) in the (2+1)-dimensional bulk/boundary theories. It is shown that the Chern-Simons/Liouville(Chern-Simons/chiral boson) is an effective description for the BTZ black hole (QHE). Also the IR(bulk)-UV(boundary) connection for a black hole information bound is realized as the UV(low-lying excitations on bulk)-IR(long-range excitations on boundary) connection in the QHE. An inflow of conformal anomaly($c = 1$ central charge) onto the timelike boundary of AdS_3 by the Noether current corresponds to an inflow of chiral anomaly onto the edge of disk by the Hall current.

QUANTUM HALL EFFECT and QUARKS

Quantum Hall quarks or Short distance physics of quantized Hall fluids

Martin Greiter

Department of Physics, Stanford University, Stanford, CA 94305, greiter@quantum.stanford.edu
(SU-ITP 96/30, cond-mat/9607014, July 2, 1996)

In order to obtain a local description of the short distance physics of fractionally quantized Hall states for realistic (e.g. Coulomb) interactions, I propose to view the zeros of the ground state wave function, as seen by an individual test electron from far away, as particles. I then present evidence in support of this interpretation, and argue that the electron effectively decomposes into quark-like constituent particles of fractional charge.

PACS numbers: 73.40.Hm, 73.20.Dx, 03.65.-w, 03.80.+r

QUANTUM HALL EFFECT and QUANTUM COMPUTER



ELSEVIER

2 March 1998

PHYSICS LETTERS A

Physics Letters A 239 (1998) 141–146

Quantum computation in quantum-Hall systems

V. Privman^a, I.D. Vagner^b, G. Kventsel^{b,c}

^a *Department of Physics, Clarkson University, Potsdam, NY 13699–5820, USA*

^b *Grenoble High Magnetic Field Laboratory, Max-Planck-Institut für Festkörperforschung, and Centre National de la Recherche Scientifique, BP 166, F-38042, Grenoble Cedex 9, France*

^c *Department of Chemistry, Technion – Israel Institute of Technology, Haifa 32000, Israel*

Received 17 July 1997; revised manuscript received 10 December 1997; accepted for publication 10 December 1997

Communicated by C.R. Doering

Abstract

We describe a quantum information processor (quantum computer) based on the hyperfine interactions between the conduction electrons and nuclear spins embedded in a two-dimensional electron system in the quantum-Hall regime. Nuclear spins can be controlled individually by electromagnetic pulses. Their interactions, which are of the spin-exchange type, can be possibly switched on and off pair-wise dynamically, for nearest neighbors, by controlling impurities. We also propose the way to feed in the initial data and explore ideas for reading off the final results. © 1998 Elsevier Science B.V.

THE EFFECTIVE ACTION FOR PHOTONS IN (2+1) DIMENSIONS

Richard J. Hughes

CERN -- Geneva

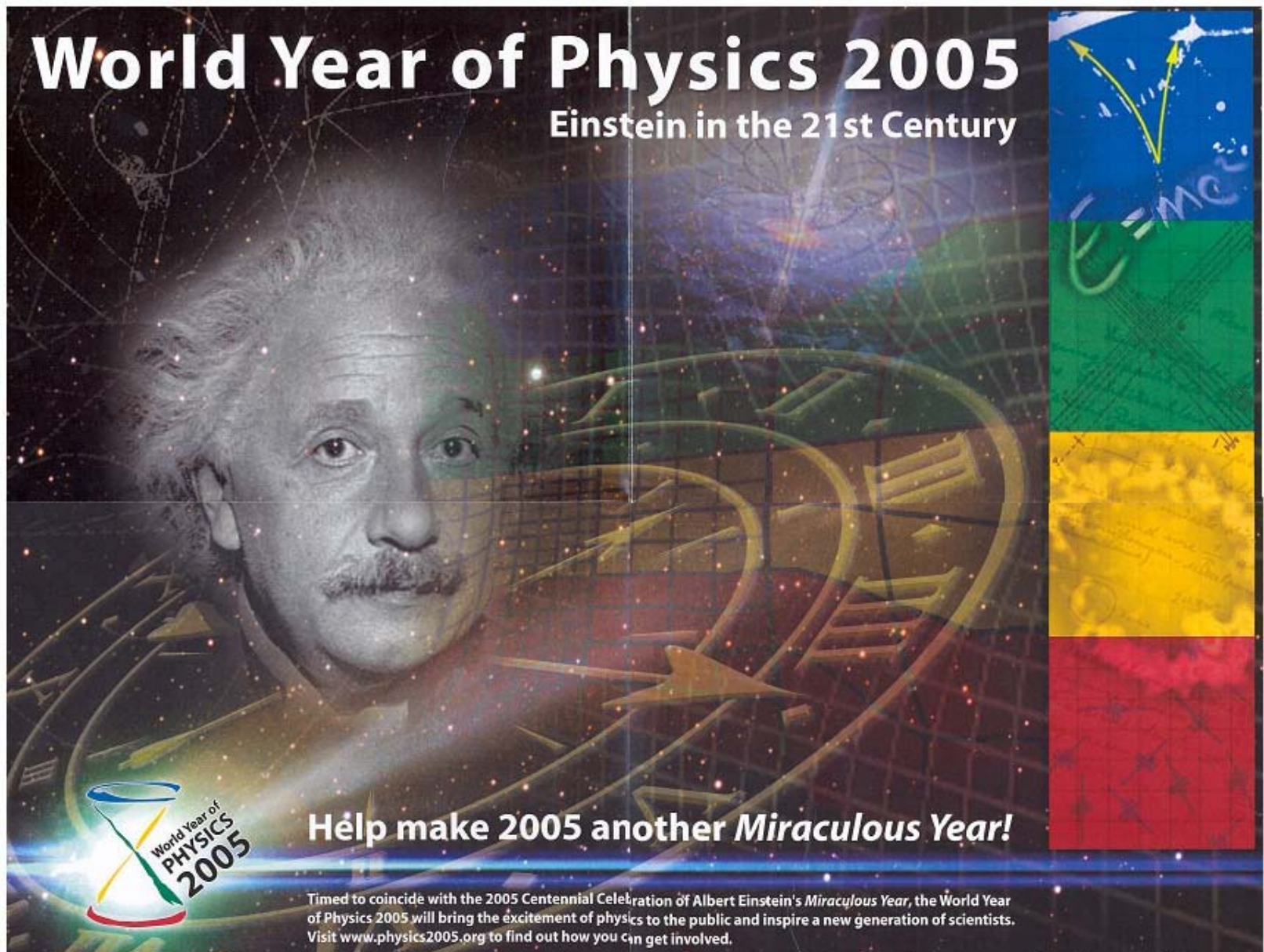
QUANTUM HALL EFFECT and VACUUM

A B S T R A C T

The topological mass term in the Euler-Heisenberg effective action for (2+1) dimensional spinor QED is studied by functional and canonical methods. The mass term is associated with a quantum Hall effect in the vacuum, and with a vacuum charge in the special case of a pure magnetic field. This charge is shown to become depleted at non-zero temperature.

QHE and the Einstein Year

(25th, 50th, and 100th anniversary)




The poster features a central portrait of Albert Einstein, with a large, glowing, golden-colored clock face superimposed over it. The clock face has Roman numerals and a large arrow pointing towards the right. The background is a dark, starry space with various physics-related graphics, including a blue and yellow arrow pointing upwards and to the right, and a green and yellow arrow pointing downwards and to the right. The right side of the poster is divided into four colored rectangular panels: blue, green, yellow, and red, each containing different physics-related imagery.

World Year of Physics 2005

Einstein in the 21st Century

Help make 2005 another *Miraculous Year!*

 World Year of PHYSICS 2005

Timed to coincide with the 2005 Centennial Celebration of Albert Einstein's *Miraculous Year*, the World Year of Physics 2005 will bring the excitement of physics to the public and inspire a new generation of scientists. Visit www.physics2005.org to find out how you can get involved.

QUANTUM HALL EFFECT and GRAVITATION

A Four-Dimensional Generalization of the Quantum Hall Effect

Shou-Cheng Zhang and Jiangping Hu

We construct a generalization of the quantum Hall effect, where particles move in four dimensional space under a $SU(2)$ gauge field. This system has a macroscopic number of degenerate single particle states. At appropriate integer or fractional filling fractions the system forms an incompressible quantum liquid. Gapped elementary excitation in the bulk interior and gapless elementary excitations at the boundary are investigated.

PhysicsWeb: The work by Shou-Cheng Zhang and Jianping Hu of Stanford University in California and Tsinghua University in China might even represent a small step towards one of the ultimate goals in theoretical physics - a quantum theory of gravity (S-C Zhang and J Hu 2001 *Science* 294 823).

Is the Quantum Hall Effect Influenced by the Gravitational Field?

Friedrich W. Hehl,^{1,2,*} Yuri N. Obukhov,^{1,3,†} and Bernd Rosenow^{1,‡}

¹*Institut für Theoretische Physik, Universität zu Köln, 50923 Köln, Germany*

²*Department of Physics and Astronomy, University of Missouri–Columbia, Columbia, Missouri 65211, USA*

³*Department of Theoretical Physics, Moscow State University, 117234 Moscow, Russia*

(Received 13 October 2003; published 26 August 2004)

Most of the experiments on the quantum Hall effect (QHE) were made at approximately the same height above sea level. A future international comparison will determine whether the gravitational field $\mathbf{g}(x)$ influences the QHE. In the realm of $(1 + 2)$ -dimensional phenomenological macroscopic electrodynamics, the Ohm-Hall law is metric independent (“topological”). This suggests that it does not couple to $\mathbf{g}(x)$. We corroborate this result by a microscopic calculation of the Hall conductance in the presence of a post-Newtonian gravitational field.

DOI: 10.1103/PhysRevLett.93.096804

PACS numbers: 73.43.Cd, 03.50.De, 04.20.-q, 73.43.Fj

QUANTUM HALL EFFECT and STRING THEORY

Higher-dimensional quantum Hall effect in string theory

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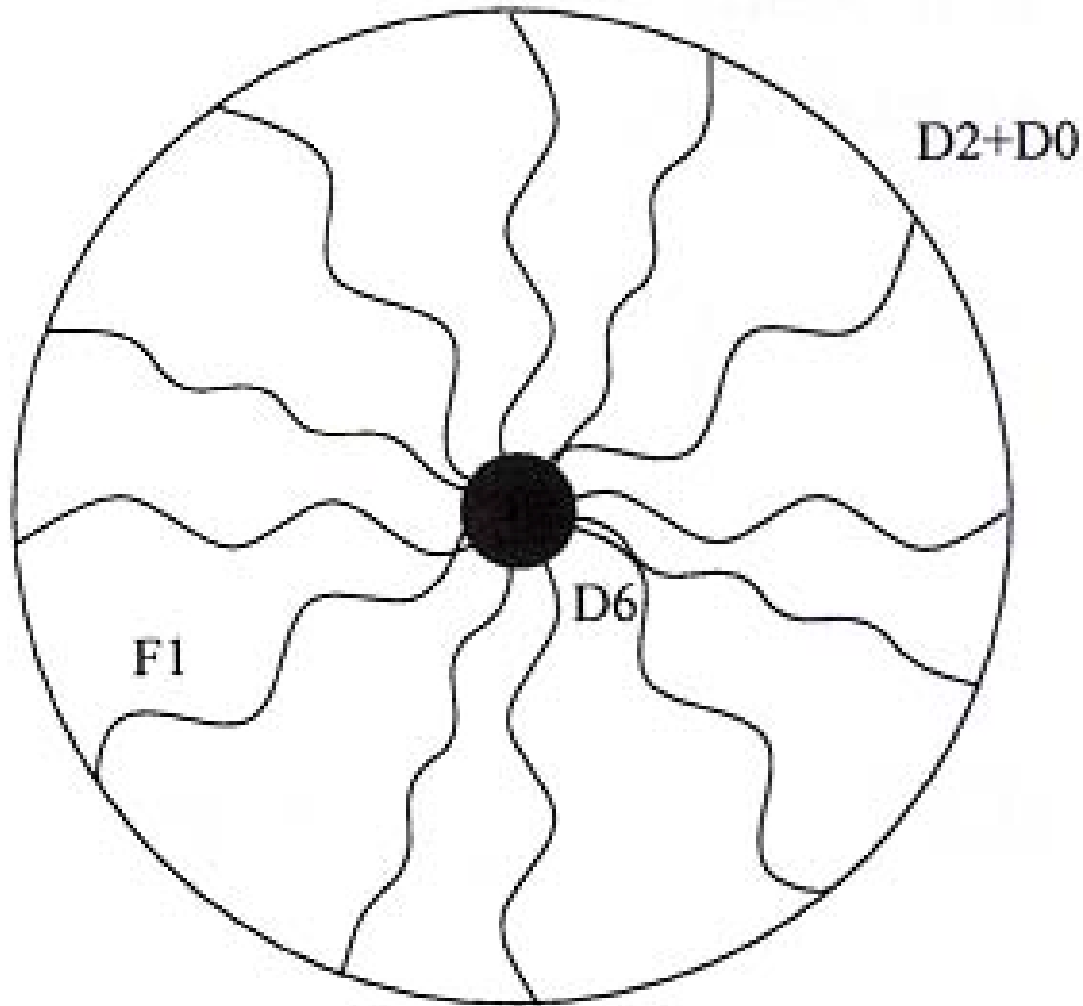


Fig1: This picture shows a string theory realization of the 2+1d **quantum Hall effect** on a two-sphere.

(from *M. Fabinger in Journal High Energy Physics*, 5 (2002) 037)

THE PHYSICAL REVIEW
AND
PHYSICAL REVIEW LETTERS

(PUBLISHED FOR THE AMERICAN PHYSICAL SOCIETY)

BROOKHAVEN NATIONAL LABORATORY, UPTON, LONG ISLAND, NEW YORK 11973

TELEPHONE (516) 345-2540
(516) 924-5533

OUR NEW ADDRESS:
1 RESEARCH ROAD
BOX 1000
RIDGE, NEW YORK 11961

June 25, 1980

Dr. K.v. Klitzing
Physikalisches Institut der
Universität Würzburg
D-9700 Würzburg
Federal Republic of Germany
Dear Dr. Klitzing:

The manuscript by

K.v. Klitzing, G. Dorda, and M. Pepper

entitled:

Realization of a resistance standard based on
fundamental constants

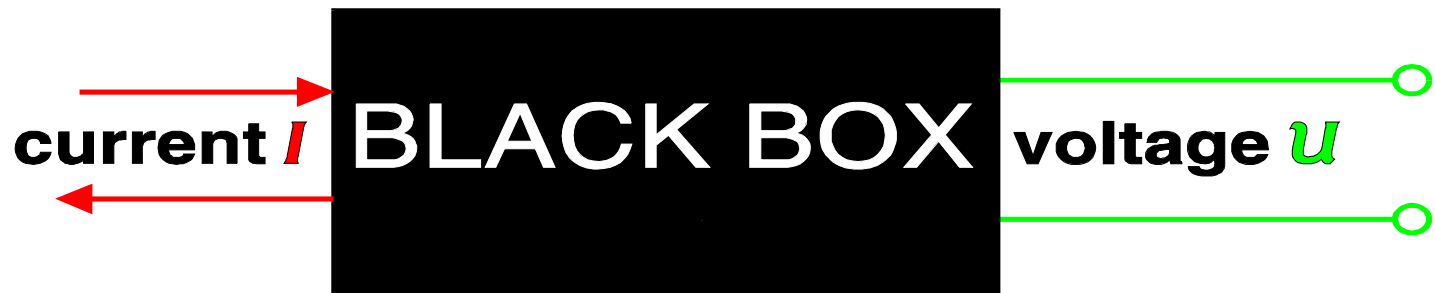
IN REPLY REFER TO →

LS1509

has been reviewed by our referee(s). On the basis of the resulting report(s), we judge that the paper is not suitable for publication in Physical Review Letters in its present form, but might be made so by appropriate revision. Pertinent criticism extracted from the report(s) is enclosed. While we cannot make a definite commitment, the probable course of action if you choose to resubmit is indicated below.

- () Acceptance, if the editors can judge that all or most of the criticism has been met.
- () Return to the original referee(s) for judgement.
- (✓) Submittal to new referee(s) for judgement.

FINAL RESULT OF QUANTUM HALL EFFECT (QHE)



(Hall-) Resistance $R_H = U/I$

The "BLACK BOX"

(MOSFET at low temperatures in high magnetic fields)
has always the resistance value $R_H = 25812,807 \text{ Ohm}$

Revised technical guidelines for reliable dc measurements of the quantized Hall resistance

F Delahaye¹ and B Jeckelmann²

¹ Bureau International des Poids et Mesures, Pavillon de Breteuil, F-92312 Sèvres Cedex, France

² Swiss Federal Office of Metrology and Accreditation, Lindenweg 50, CH-3003 Bern-Wabern, Switzerland

Received 30 May 2003

Published **OCTOBER 2003**

Online at stacks.iop.org/Met/40

Abstract

This paper describes the main tests and precautions necessary for both reproducible and accurate results in the use of the quantum Hall effect as a means to establish a reference standard of dc resistance having a relative uncertainty of a few parts in 10^9 .

QUANTIZED HALL RESISTANCE IN SI OHM (up to 1990)

CSIRO, Australia	25 812.809 (2) Ω
NPL, UK	25 812.809 (1) Ω
BNM-LCIE, France	25 812.802 (6) Ω
ETL, Japan	25 812.806 (6) Ω
NIST, USA	25 812.807 (1) Ω
VNIIM, Russia	25 812.806 (8) Ω
VSL, Netherland	25 812.802 (5) Ω
NRC, Canada	25 812.814 (6) Ω
EAM, Switzerland	25 812.809 (4) Ω
PTB, Germany	25 812.802 (3) Ω
NIM, China	25 812.805 (16) Ω
CSIRO/BIPM	25 812.809 (2) Ω
CSIRO/Japan	25 812.813 (2) Ω

BEST VALUE (1990): $R_K=25\,812.807\,(5)\,\Omega$

$R_{K-90}=25\,812.807\,000\,\Omega$

Recommendations Comité International des Poids et Mesures

(October 4-6, 1988)

recommends

- that 25 812,807 Ω exactly be adopted as a conventional value, denoted by R_{K-90} , for the von Klitzing constant, R_K ,
- that this value be used from 1st January 1990, and not before, by all laboratories which base their measurements of resistance on the quantum Hall effect,
- that from this same date all other laboratories adjust the value of their laboratory reference standards to agree with R_{K-90} ,
- that in the use of the quantum Hall effect to establish a laboratory reference standard of resistance, laboratories follow the most recent edition of the technical guidelines for reliable measurements of the quantized Hall resistance drawn up by the Comité Consultatif d'Electricité and published by the Bureau International des Poids et Mesures,

and is of the opinion

- that no change in this recommended value of the von Klitzing constant will be necessary in the foreseeable future.

<http://physics.nist.gov/>

**The NIST Reference on
Constants, Units, and Uncertainty**

Source: ~~1998~~²⁰⁰² CODATA
recommended values

*the conventional value is by
definition constant!*

von Klitzing constant

R_K in SI units

Value 25 812.807 ~~572~~⁴⁴⁹ Ω

Standard uncertainty 0.000 ~~095~~⁸⁶ Ω

Relative standard uncertainty ~~3.7~~³ $\times 10^{-9}$

Concise form ~~25 812.807 572(95) Ω~~
25 812.807 449 (86) Ω

conventional value of von Klitzing constant

R_{K-90}

Value 25 812.807 Ω

Standard uncertainty (**exact**)

Relative standard uncertainty (**exact**)

Concise form 25 812.807 Ω

This label on calibrated resistors indicate, that the calibration is based on the *conventional value* for the **von Klitzing constant R_{K-90}** fixed (without uncertainty) in 1990



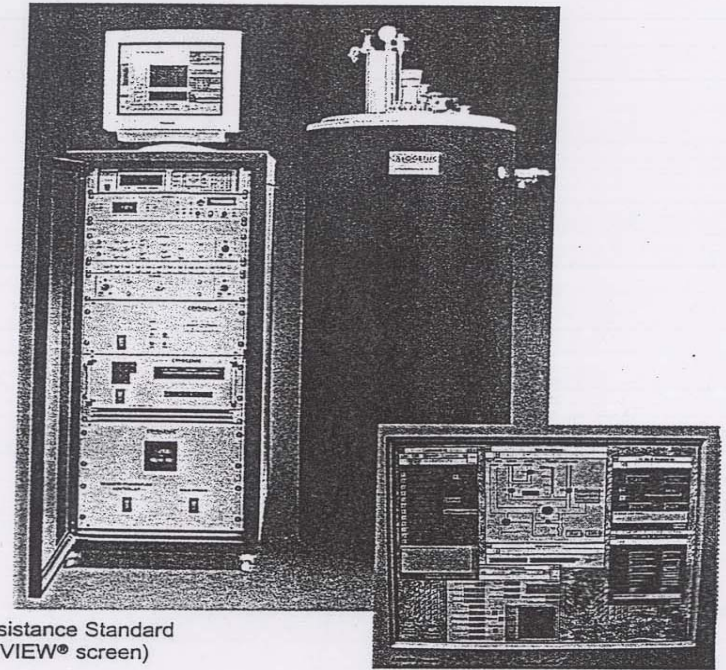
PRIMARY RESISTANCE STANDARD

QHR2000 A NEW STANDARD IN MEASUREMENT

EVERYONE IN THE WORLD
(if he spends about 300 T€ for
this equipment)

IS ABLE TO CALIBRATE
RESISTANCES WITH AN
UNCERTAINTY OF LESS
THAN 10^{-8}

**"The better choice for your Primary
Resistance Standard - QHR2000"**



Quantum Hall Resistance Standard
(Inset; typical LabVIEW® screen)

The QHR2000 is a primary resistance standard system developed by Cryogenic Ltd. based upon the Quantum Hall Effect. It allows calibration of a nominally 100Ω standard resistor against the von Klitzing constant with a precision of 10^{-8} .

The Cryogenic Current Comparator (CCC) used enables precision measurement and control to 10^{-9} . It may be used independently to carry out very accurate bridge circuit measurements.

CRYOGENIC
CRYOGENIC LIMITED

For further information please contact us at:
Unit 30, Acton Park Industrial Estate, The Vale,
London W3 7QE, UK
Tel: +44 181 743 6049 Fax: +44 181 749 5315
E-mail: cryogenic@cix.compulink.co.uk

® National Instruments

The QHR2000's principle features are:-

- Comparison of the 100Ω standard with R_K to 1 part in 10^8 .
- Precision comparison of 100Ω standard to resistances from 1Ω to $10k\Omega$.
- Portable CCC insert for independent use with low LHe consumption.
- LabVIEW® software for automated operation, measurement and analysis.
- 14 Tesla magnet at 4.2K allowing easy use of plateaux up to $n=2$.
- Fully shielded, a screened room is not required.

DC Quantum Hall - Resistance



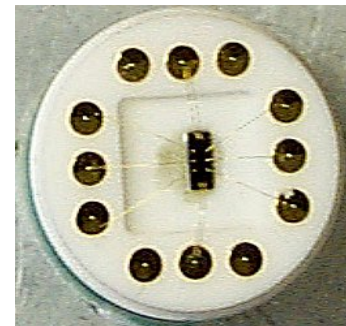
Primary Standard

14T Magnet

^3He Cryostat

CCC Bridge

DC samples from

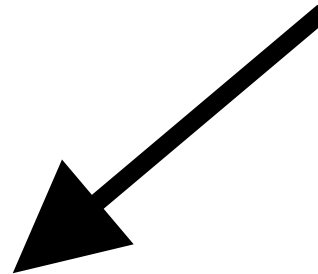
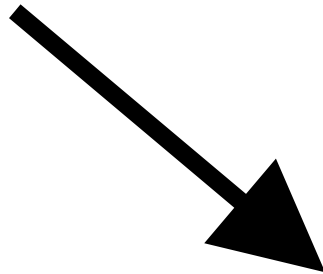
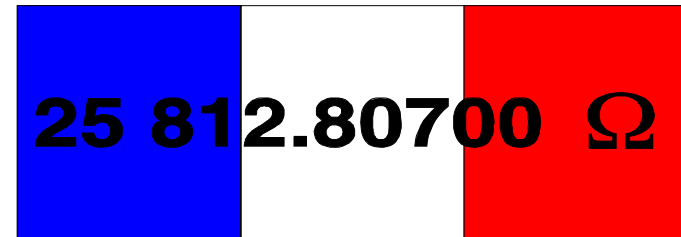


LEP, DFM
PTB, OFMET
NRC, ...

PTB



BIPM



100 Ω (?)

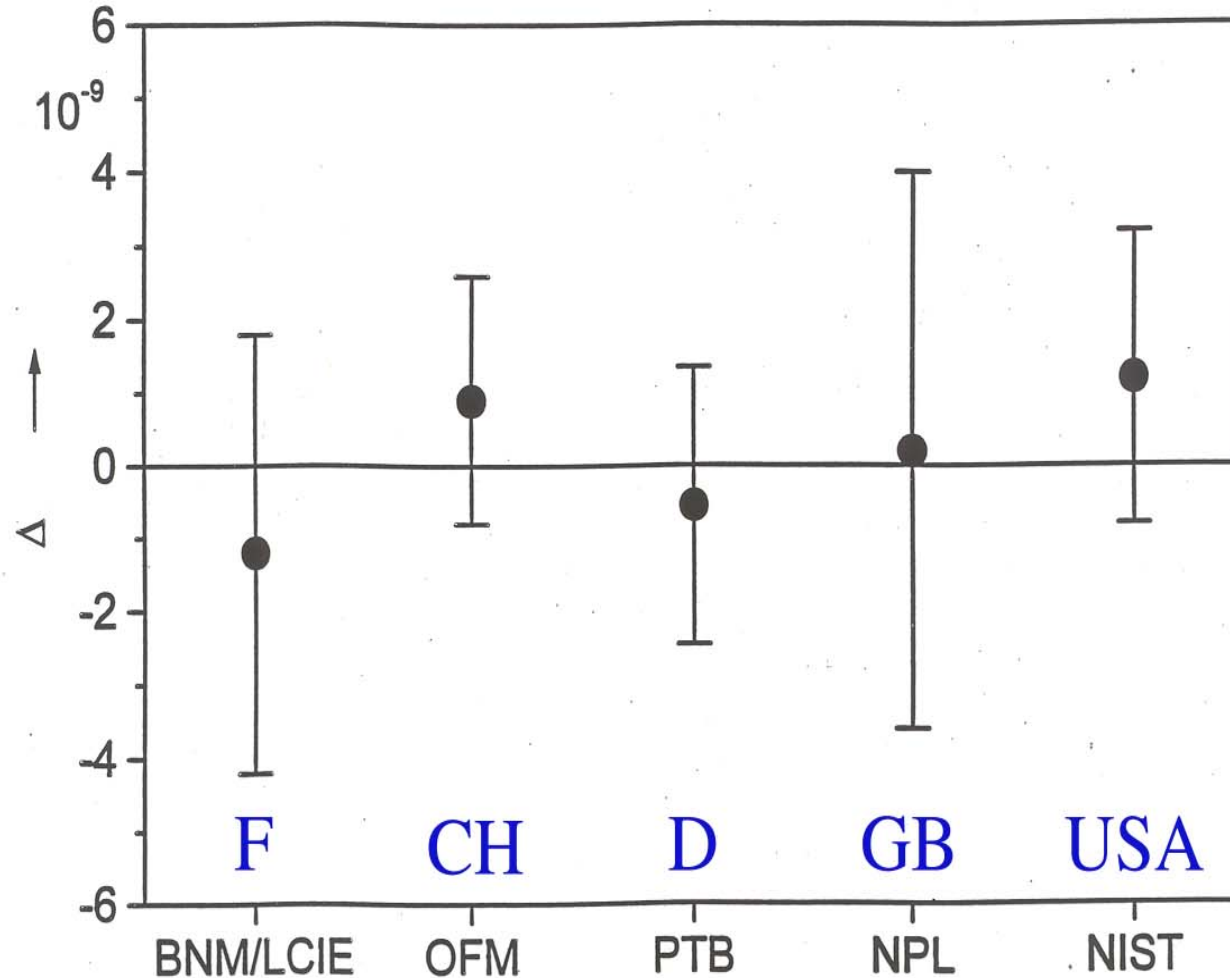
BIPM: R=100.001 729 39 Ω

PTB: R=100.001 729 33 Ω

**\uparrow ± 2 uncertainty
in SI units**

*Electrical resistances calibrated on the basis of the QHE
agree within an uncertainty of about $2 \cdot 10^{-9}$*

(but the resistance value in SI Ohm is only known within $2 \cdot 10^{-7}$)



CODATA *Recommended Values of the Fundamental Physical Constants*

J.Phys.Ref.Data, Vol.28,No.6, 1999

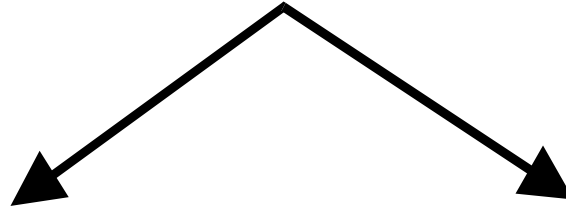
The theory of the QHE predicts, and the experimentally observed universality of R_K is consistent with the prediction, that

$$R_K = \frac{h}{e^2} = \frac{\mu_0 c}{2\alpha} \approx 25\,813\,\Omega,$$

Is this exact without any correction??

NEW RESISTOR WITH

$$R_K = h/e^2$$



DETERMINATION

$$\text{OF } R_K = h/e^2$$

IF A RESISTOR CALIBRATED IN
SI UNITS IS AVAILABLE

RESISTANCE STANDARD

(WITH FIXED R_{K-90})

SIMILAR TO THE APPLICATION
OF THE JOSEPHSON EFFECT

$\alpha^{-1} = 137.036..$
THE MOST IMPORTANT
FUNDAMENTAL CONSTANT

**fine
structure
splitting**

**Muonium
hyperfine
splitting**

**electron
magnetic
moment g_e**

QHE

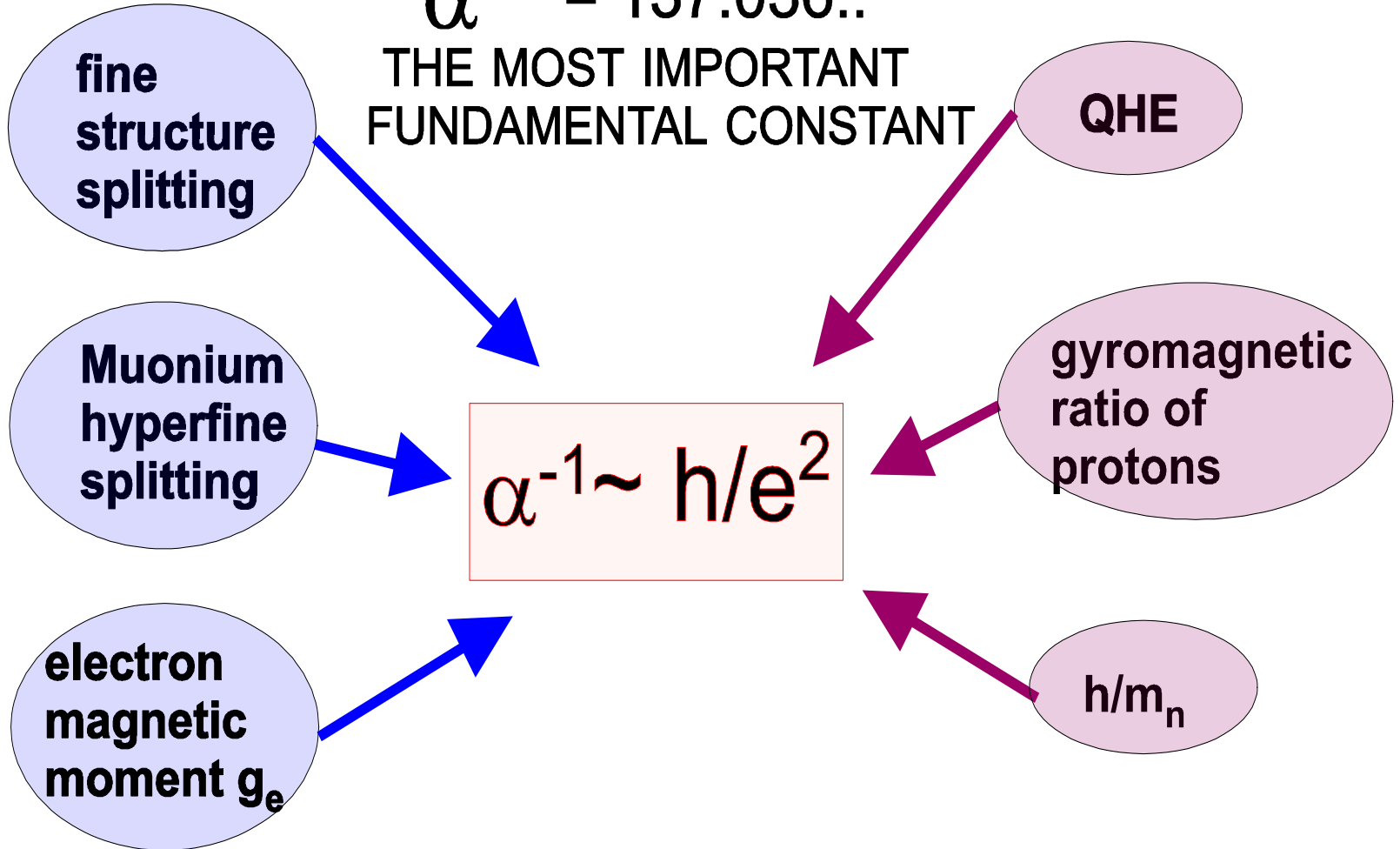
**gyromagnetic
ratio of
protons**

h/m_n

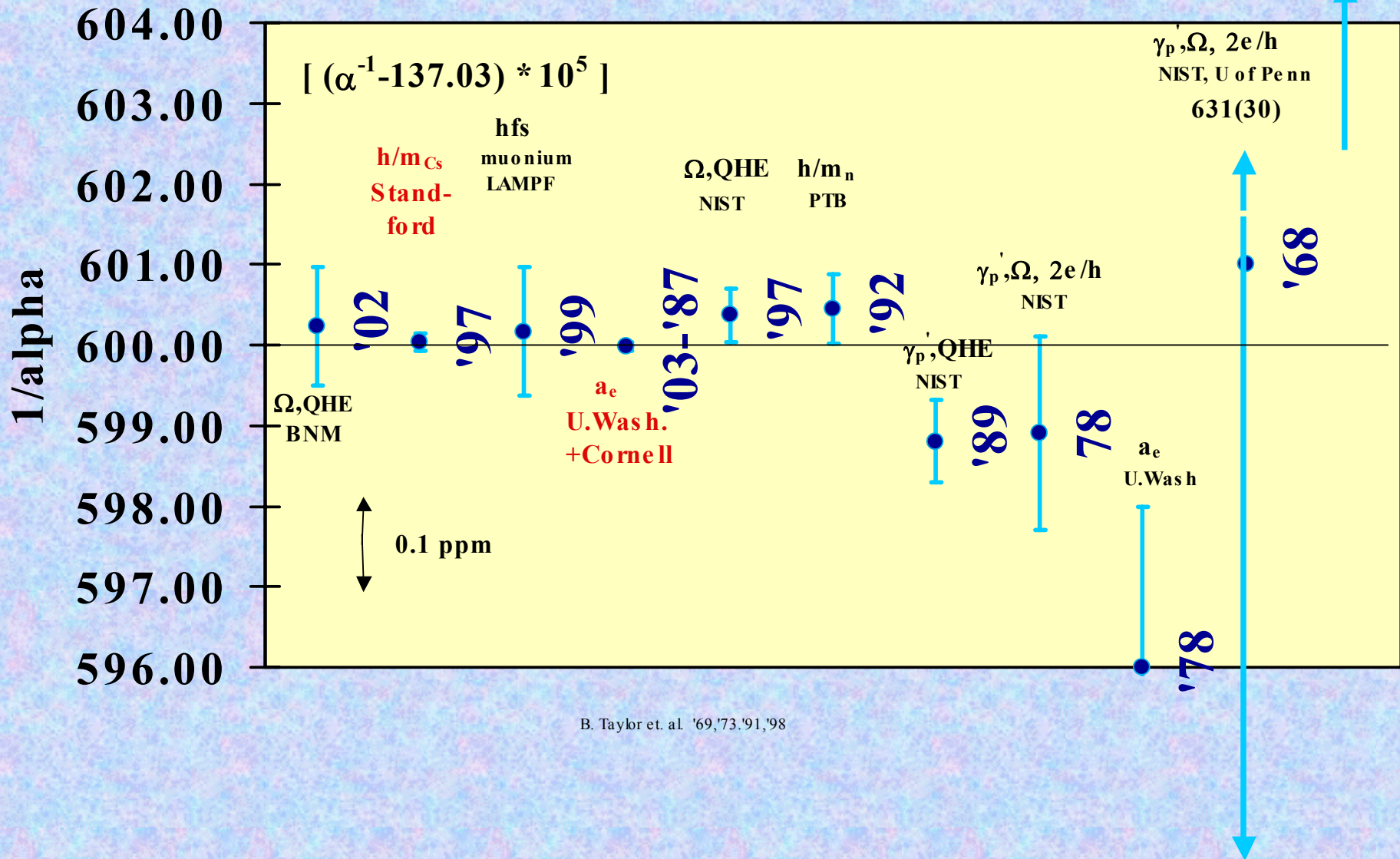
$$\alpha^{-1} \sim h/e^2$$

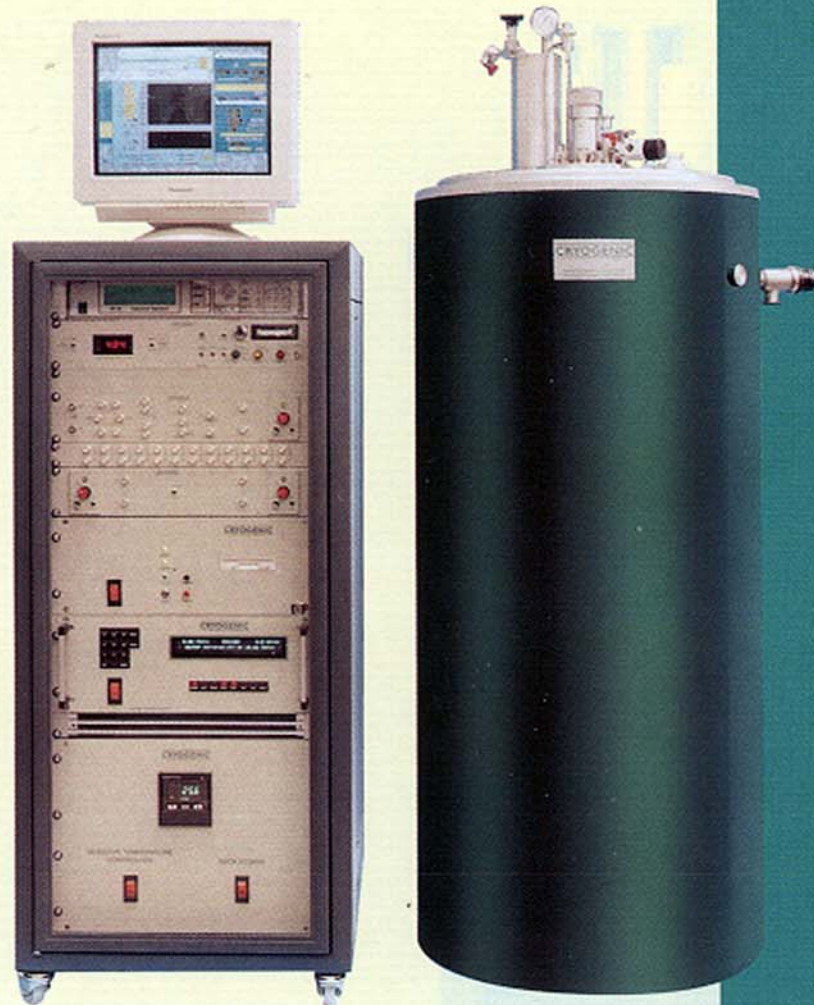
**QED-THEORY
NECESSARY**

**WITHOUT
QED**



Values of Fine-Structure-Constant



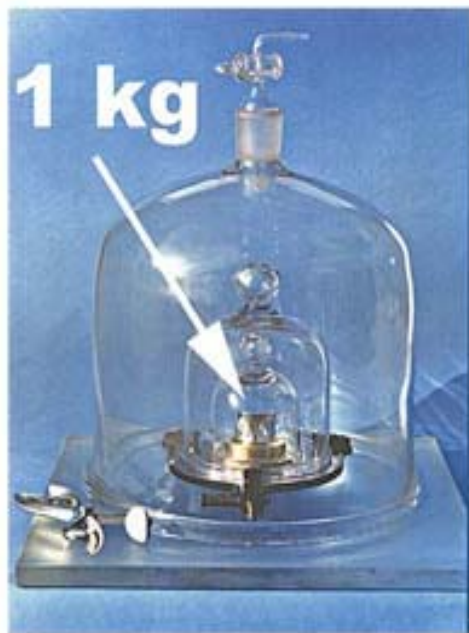


NEW QHR MAGNET FOR THE NPL

Cryogenic has been selected once again by the National Physical Laboratory (NPL) to design and manufacture a high field magnet complete with a low loss cryostat for Quantum Hall Metrology. **The magnet has been delivered for use as a Quantum Hall Resistance transfer standard. It will form part of a basic physics and fundamental constant experiment, which seeks to determine the kilogram in terms of electrical standards.** This follows a successful delivery of a similar project carried out for the Physikalisch-Technische Bundesanstalt (PTB) in Germany last year. The system is installed in a stainless steel cryostat and provides a 14 Tesla magnetic field.

Cryogenic have also supplied the NPL with a glass fibre helium cryostat with HTS leads to be used for their 100 Amp Cryogenic Current Comparator for precision metrology.

SI unit of mass

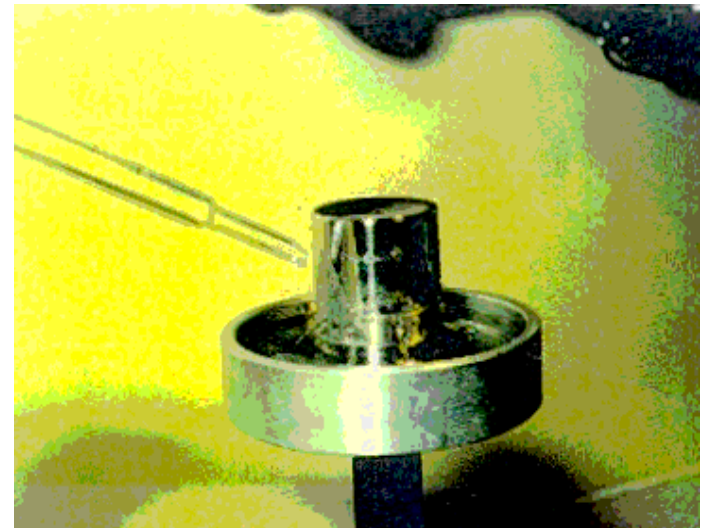


**Safe in
Paris**



“The Kilogram is equal to the mass of the International Prototype
of the Kilogram after cleaning and washing using the BIPM method.”

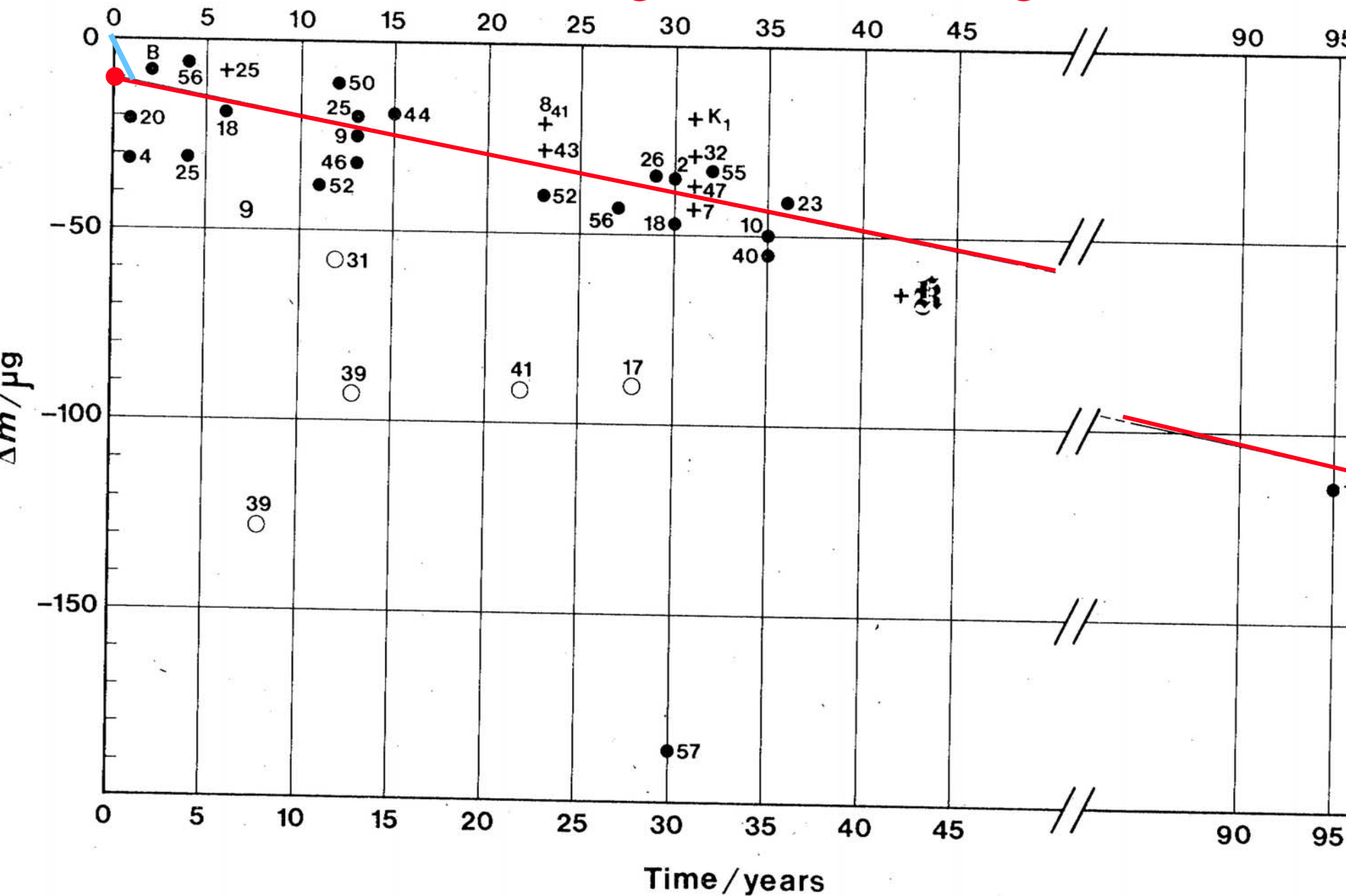
(CIPM, 1989)



BIPM Cleaning Method

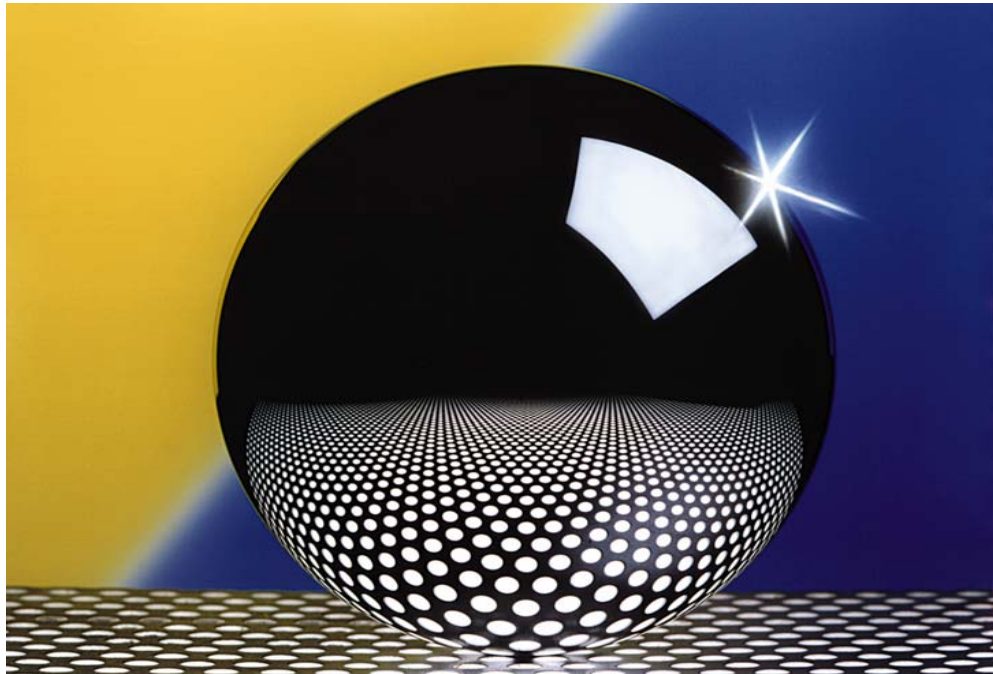
- Rub artifact with chamois cloth soaked in ether / alcohol mixture.
 - Wash in a jet of steam.

mass change after cleaning



Alternative realization of the unit of mass:

**The kilogram is a certain number of
silicon atoms**



Why not

$$*E=mc^2* \quad (\text{EINSTEIN})$$

together with

$$*E=h\nu* \quad (\text{PLANCK})$$

$$*m = h\nu/c^2*$$

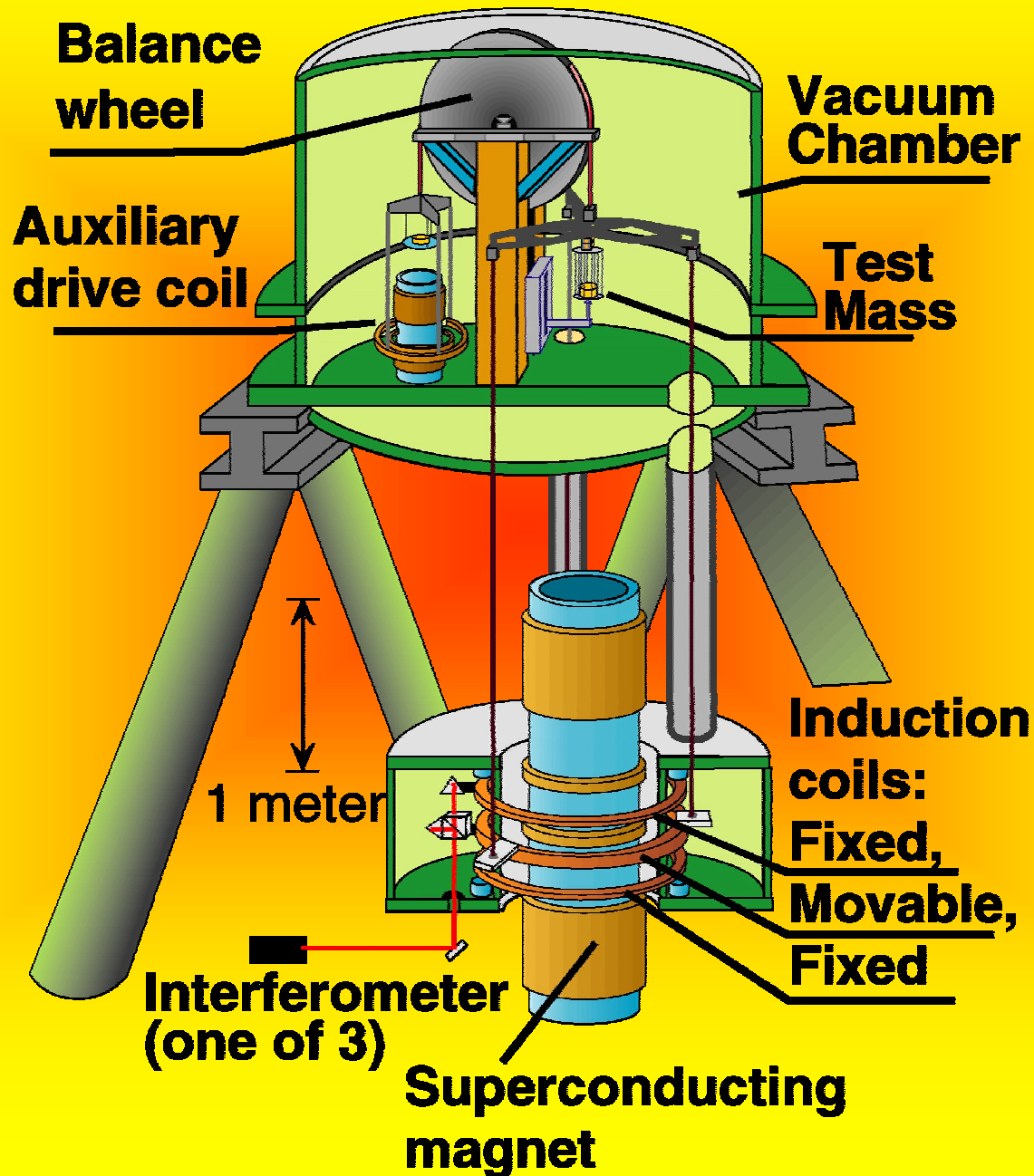
A new building for the Watt balance (using QHE)



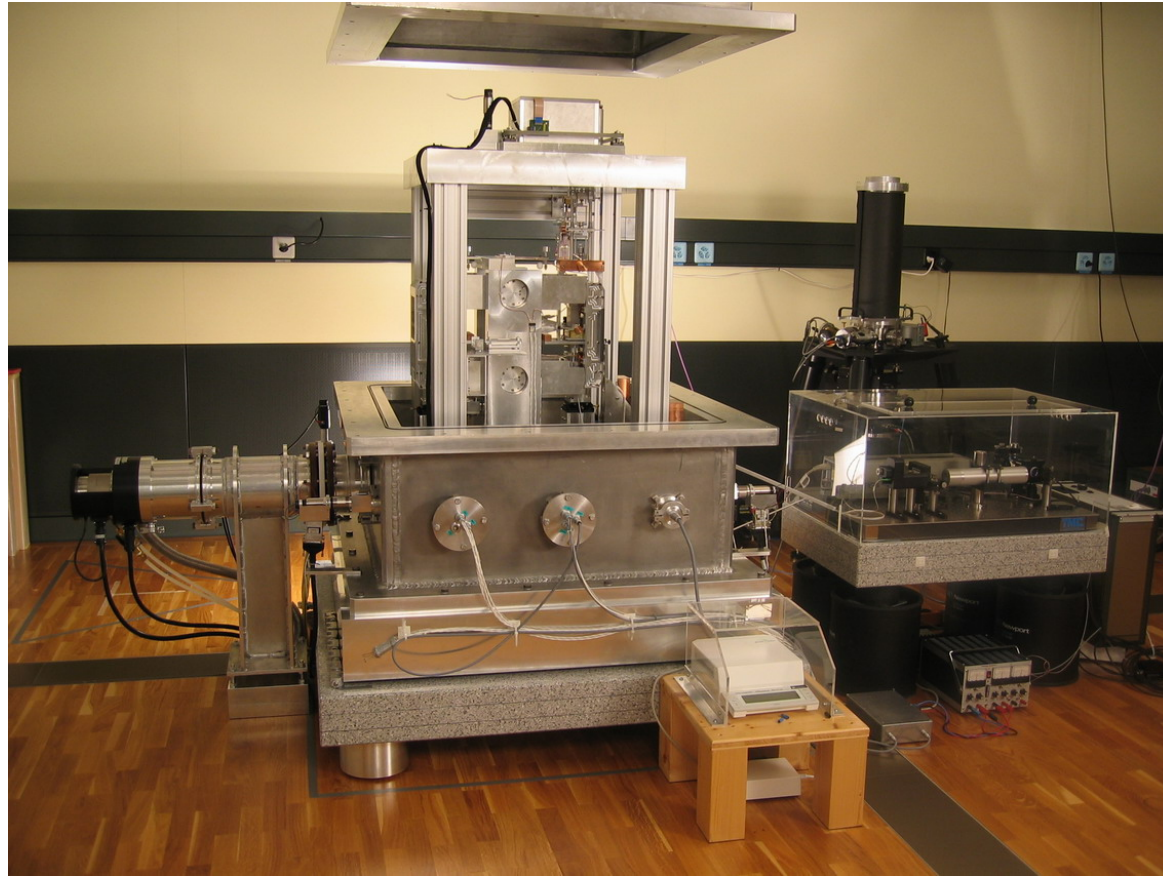
NIST

National Institute of Standards and Technology

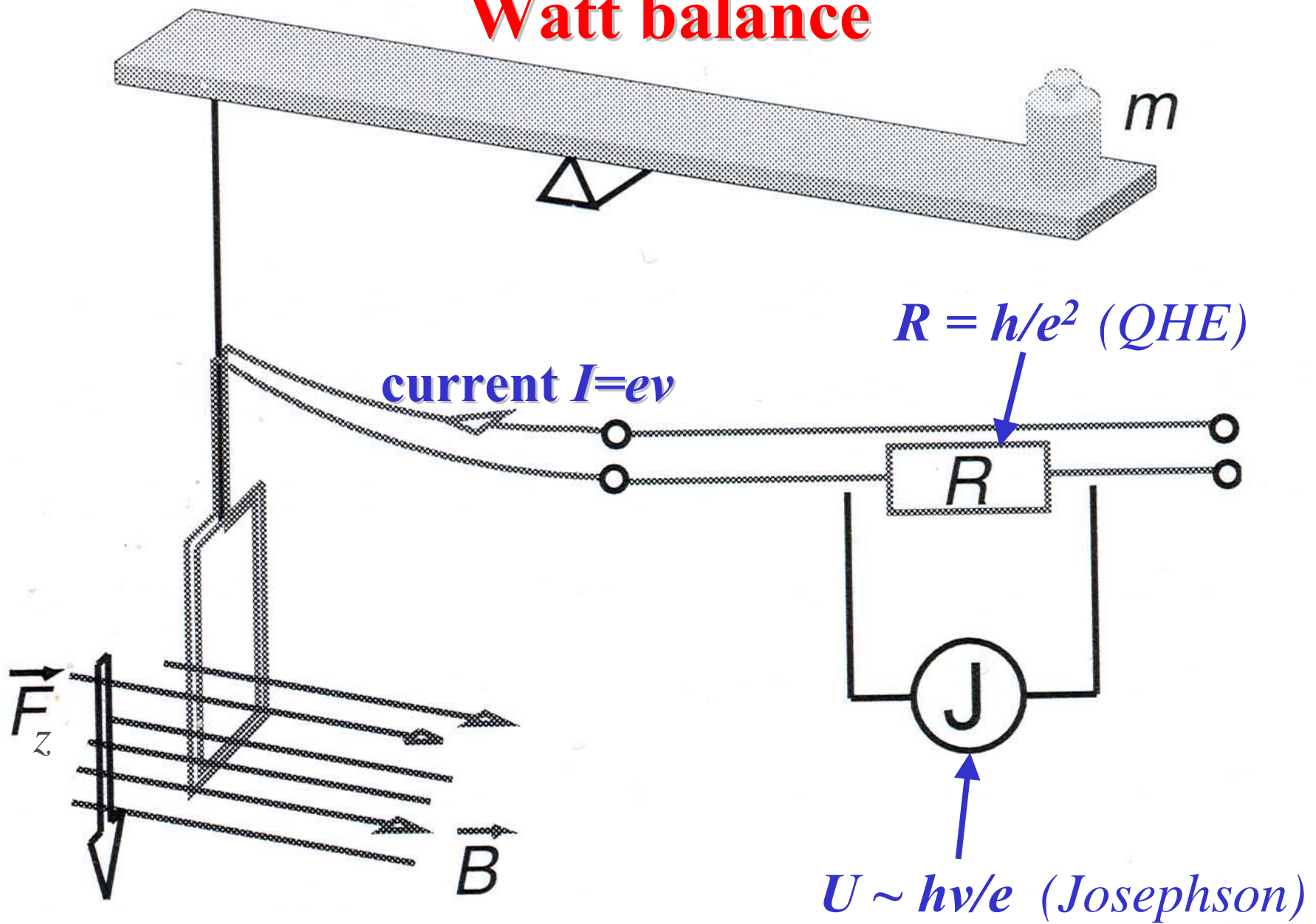
Technology Administration, U.S. Department of Commerce

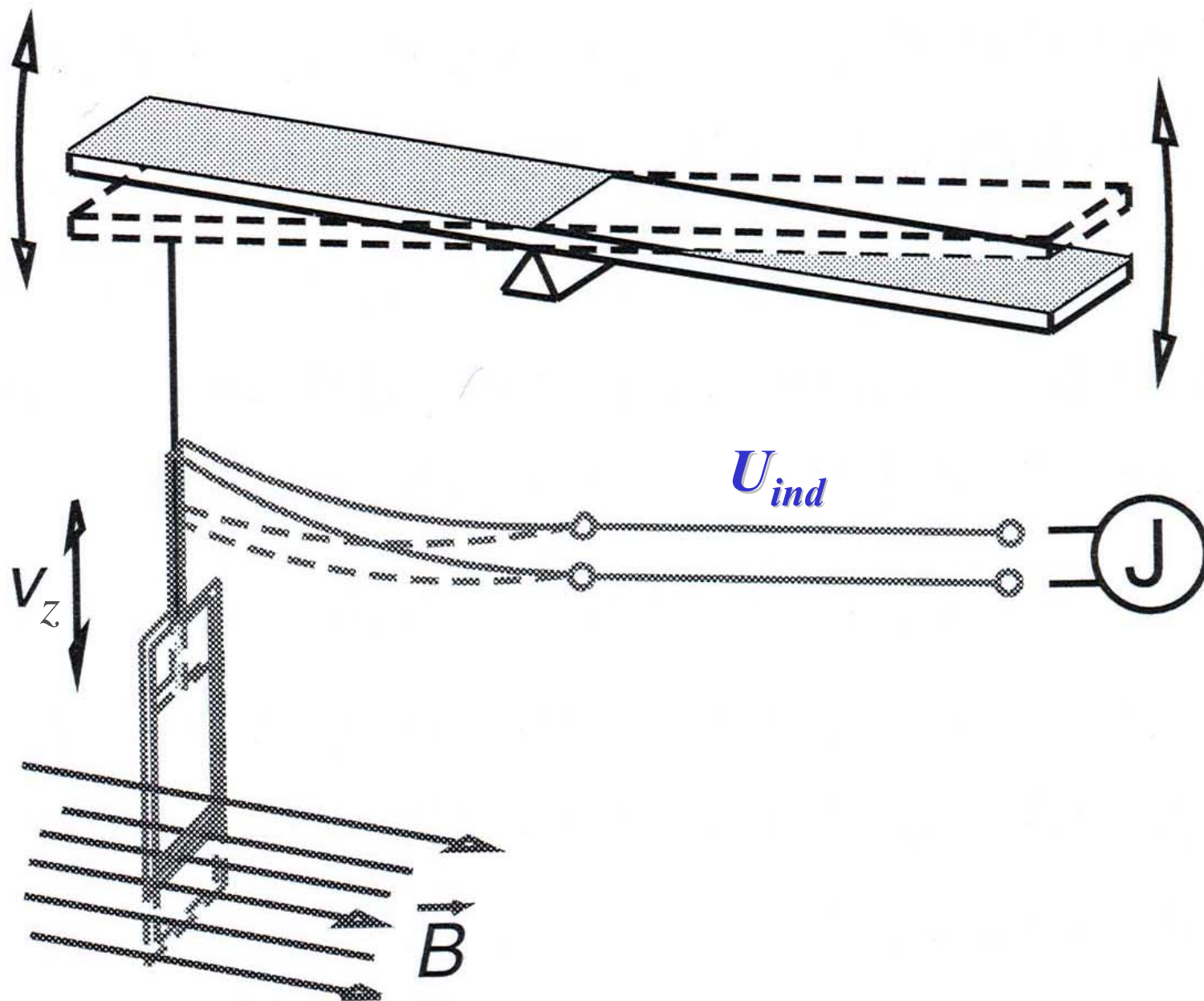


The **metas** watt balance (Switzerland)



Watt balance





$$F = -\partial\Phi/\partial z \cdot I$$

$$U_{ind} = -\partial\Phi/\partial z \cdot v$$

$$U_{ind} \cdot I = F \cdot v$$

$\sim \hbar/e$ $\sim e$ $m \cdot g$

The most inaccurate quantities in this equation are
the Planck constant \hbar and the mass m

$$\hbar \sim m$$



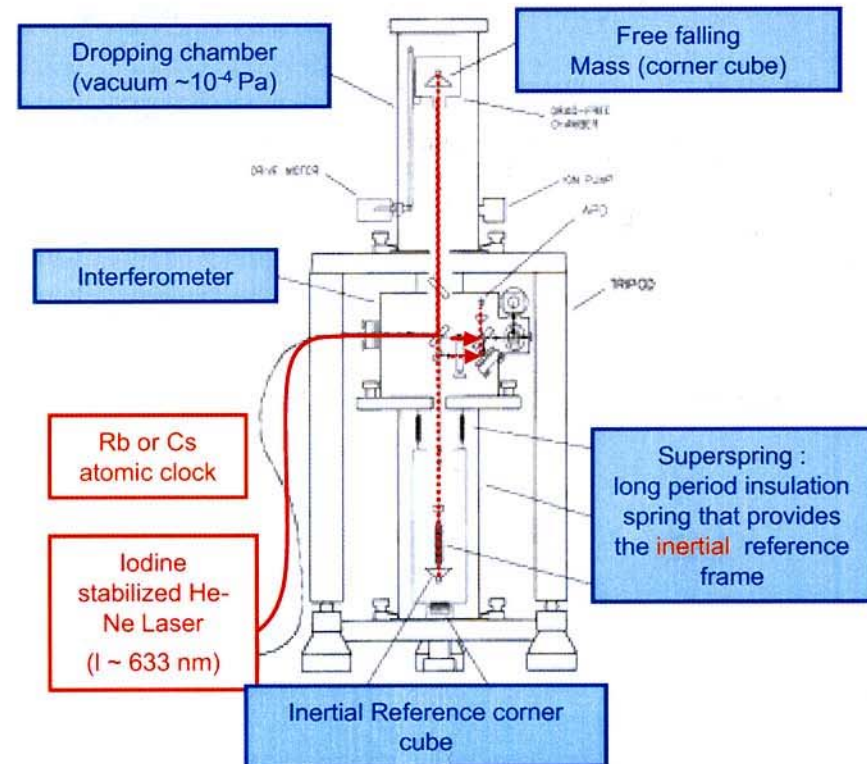
Absolute Gravimeter

(FG5 from Micro-g Solutions Inc.)

Free fall trajectory of an optical object in vacuum

Accuracy: $2 \times 10^{-8} \text{ m/s}^2$ (2 parts in 10^9)

$g = 9.780 \text{ m/s}^2$ at equator
 $g = 9.832 \text{ m/s}^2$ at north pole



Accurate Measurement of the Planck Constant

Edwin R. Williams,* Richard L. Steiner,* David B. Newell,* and Paul T. Olsen†

National Institute of Standards and Technology,‡ Gaithersburg, Maryland 20899

(Received 1 July 1998)

Using a moving coil watt balance, electric power measured in terms of the Josephson and quantum Hall effects is compared with mechanical power measured in terms of the meter, kilogram, and second. We find the Planck constant $h = 6.626\,068\,91(58) \times 10^{-34}$ J s. The quoted standard uncertainty (1 standard deviation estimate) corresponds to $(8.7 \times 10^{-8})h$. Comparing this measurement to an earlier measurement places an upper limit of 2×10^{-8} /yr on the drift rate of the SI unit of mass, the kilogram. [S0031-9007(98)07164-6]

PACS numbers: 06.20.Jr, 06.20.Fn, 06.30.Dr

TABLE I. Fundamental constants improved by this measurement and values used to calculate them. The International Committee for Weights and Measures, CIPM, adopted the indicated values in 1990 [2]. u_r means relative standard uncertainty.

Constant	Symbol	Value	Unc. u_r (10^{-8})
Planck constant	h	$6.626\,068\,91(58) \times 10^{-34}$ J s	8.7 this work
Josephson constant (SI)	$K_J = 2e/h$	483 597.892(21) GHz/V	4.4 this work
Electron mass	m_e	$9.109\,382\,11(80) \times 10^{-31}$ kg	8.8 this work
Proton mass	m_p	$1.672\,621\,62(15) \times 10^{-27}$ kg	8.9 this work
Avogadro constant	N_A	$6.022\,141\,84(52) \times 10^{23}$ mole ⁻¹	8.7 this work
Elementary charge	e	$1.602\,176\,48(7) \times 10^{-19}$ C	4.4 this work
Josephson constant	K_{J-90}	483 597.9 GHz/V	exact (CIPM)
von Klitzing constant	R_{K-90}	25 812.807 Ω	exact (CIPM)
1/(fine-structure constant)	$1/\alpha$	137.035 999 93(52)	0.38 ^a
Rydberg constant	R_∞	$10\,973\,731.568\,639(91)$ m ⁻¹	0.000 83 ^b
Electron's atomic mass	m_e/m_u	0.000 548 579 911 1(12)	0.021 ^c

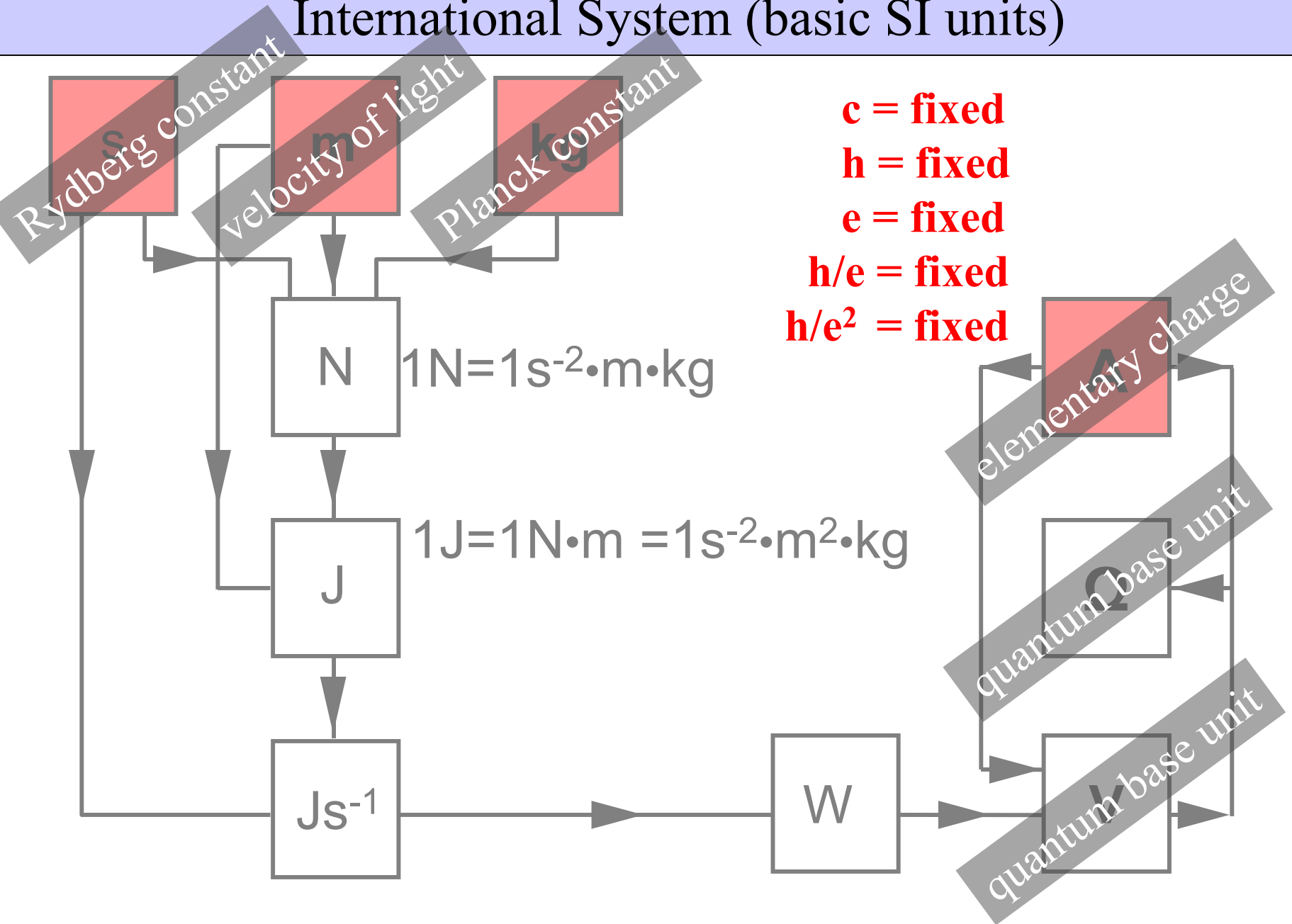
^aReference [3]. ^bReference [4]. ^cReference [5].

A possibility for a new definition of the kilogram:

The **kilogram** is the mass, which by comparison
of mechanical and electrical power results
in a value of the **Planck constant of**
 $h=6.626\ 068\ 91 \times 10^{-34}$ Js (exact).

(electrical power: $U^2/R \sim h$)

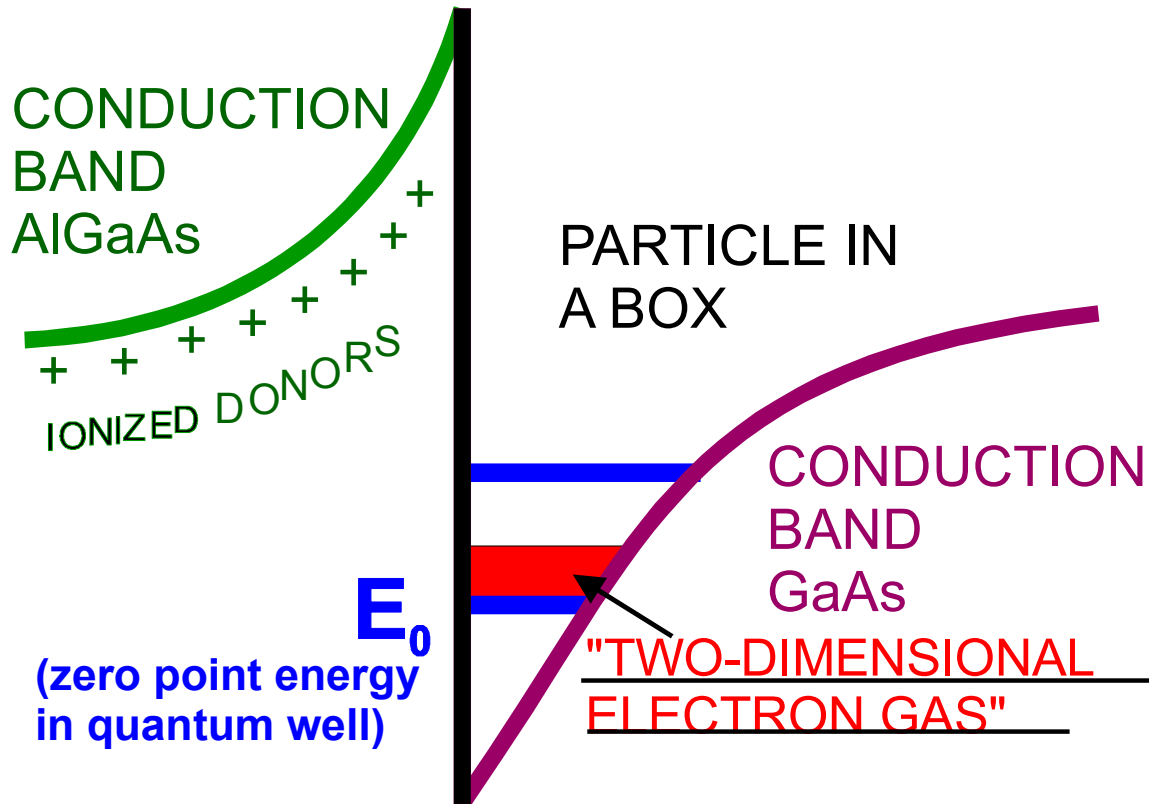
International System (basic SI units)



Physics of the QHE

- a) two-dimensional electron gas (2DEG)
- b) electrons in strong magnetic field
- c) disorder
- d) edge phenomena
- e) FQHE

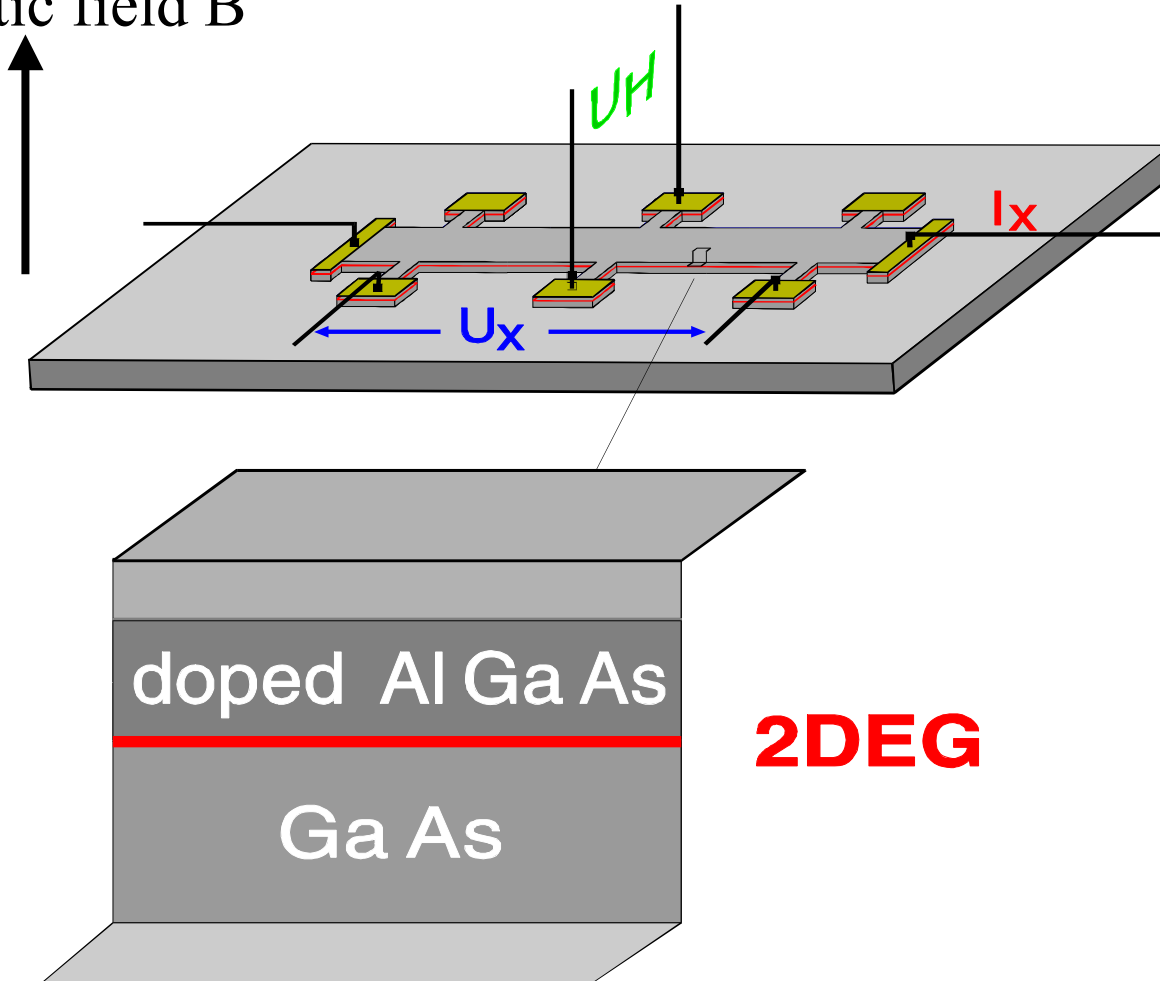
2DEG = **2-D**imensional **E**lectronen **G**as = HEMT, TEGFET



ENERGY OF "FREE" ELECTRONS IN A QUANTUM WELL

$$E = E_0 + \text{kinetic energy of motion in the interface plane}$$

magnetic field B

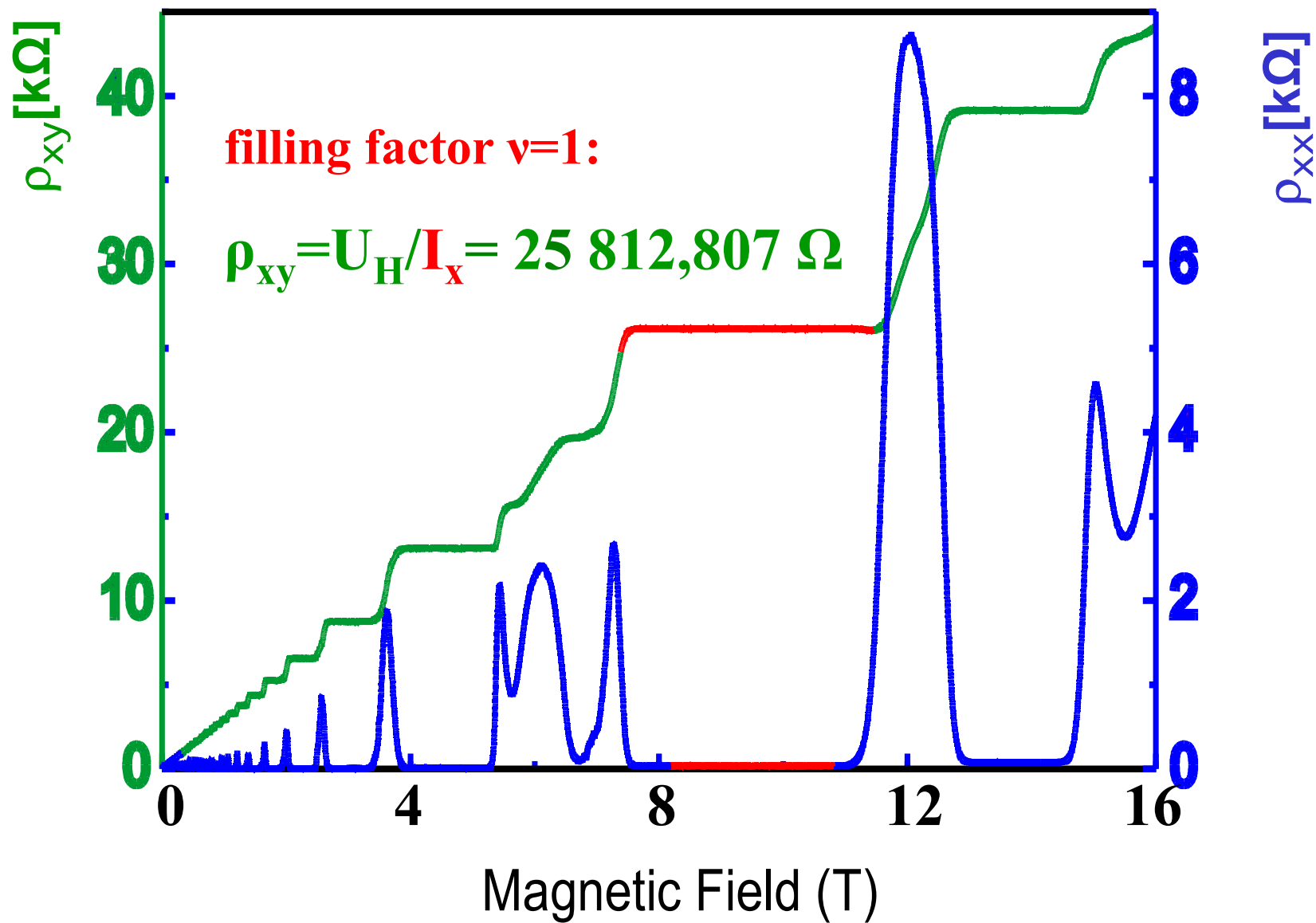


doped AlGaAs

GaAs

2DEG

Typical device used for QHE experiments



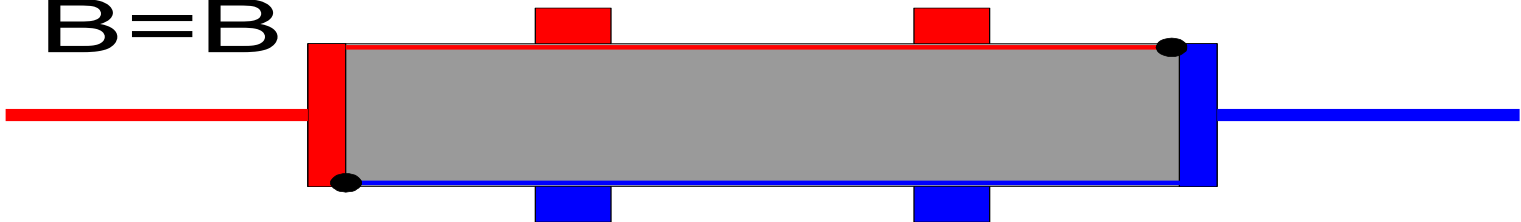
POTENTIAL DISTRIBUTION

$B=0$

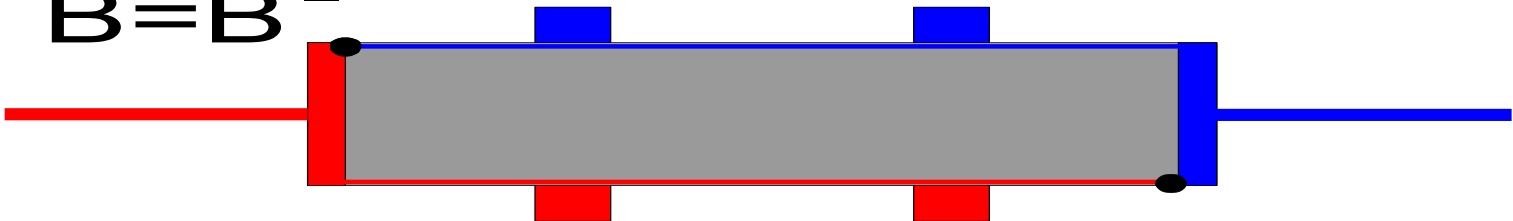


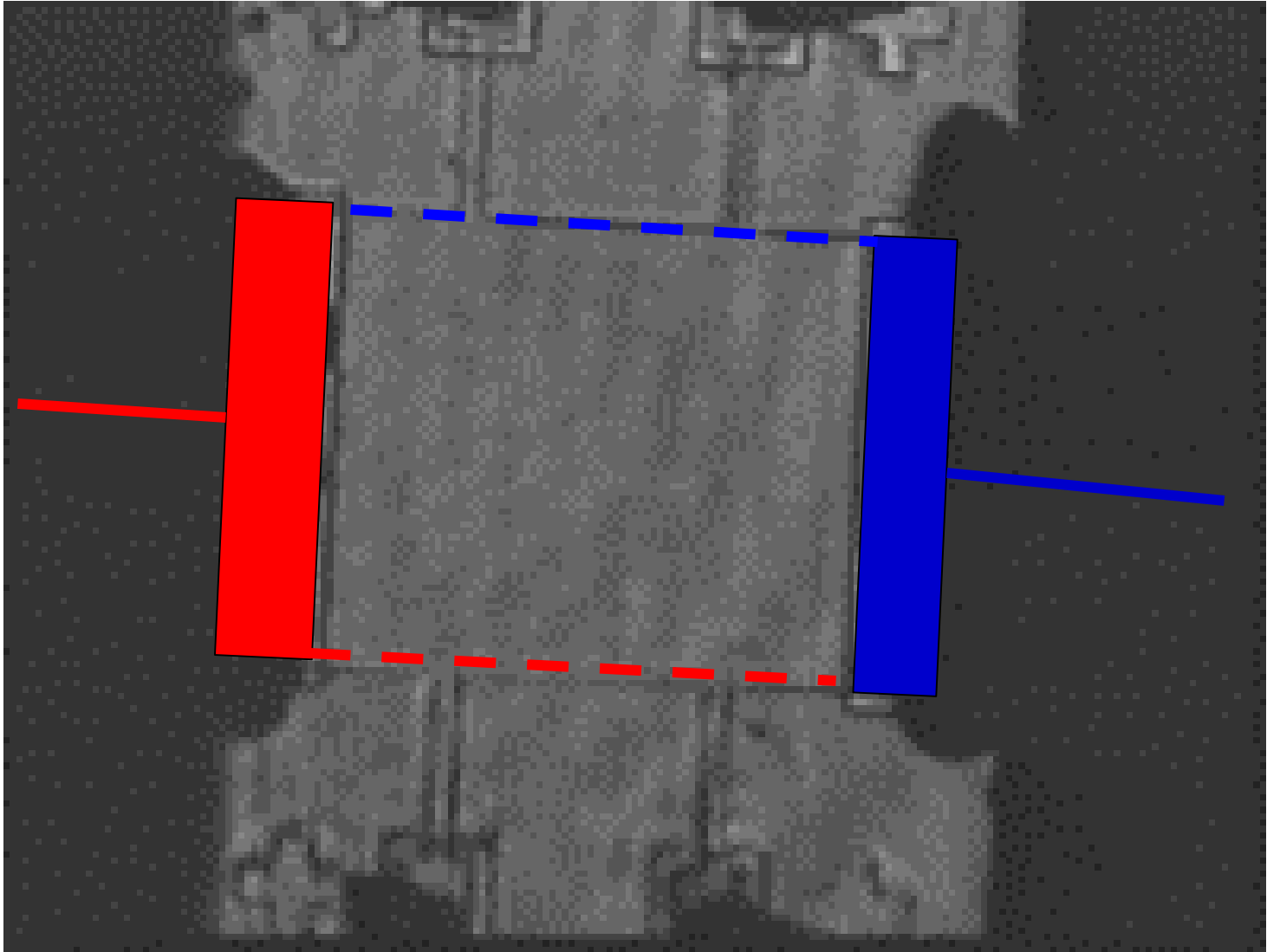
Quantum Hall Effect

$B=B^+$

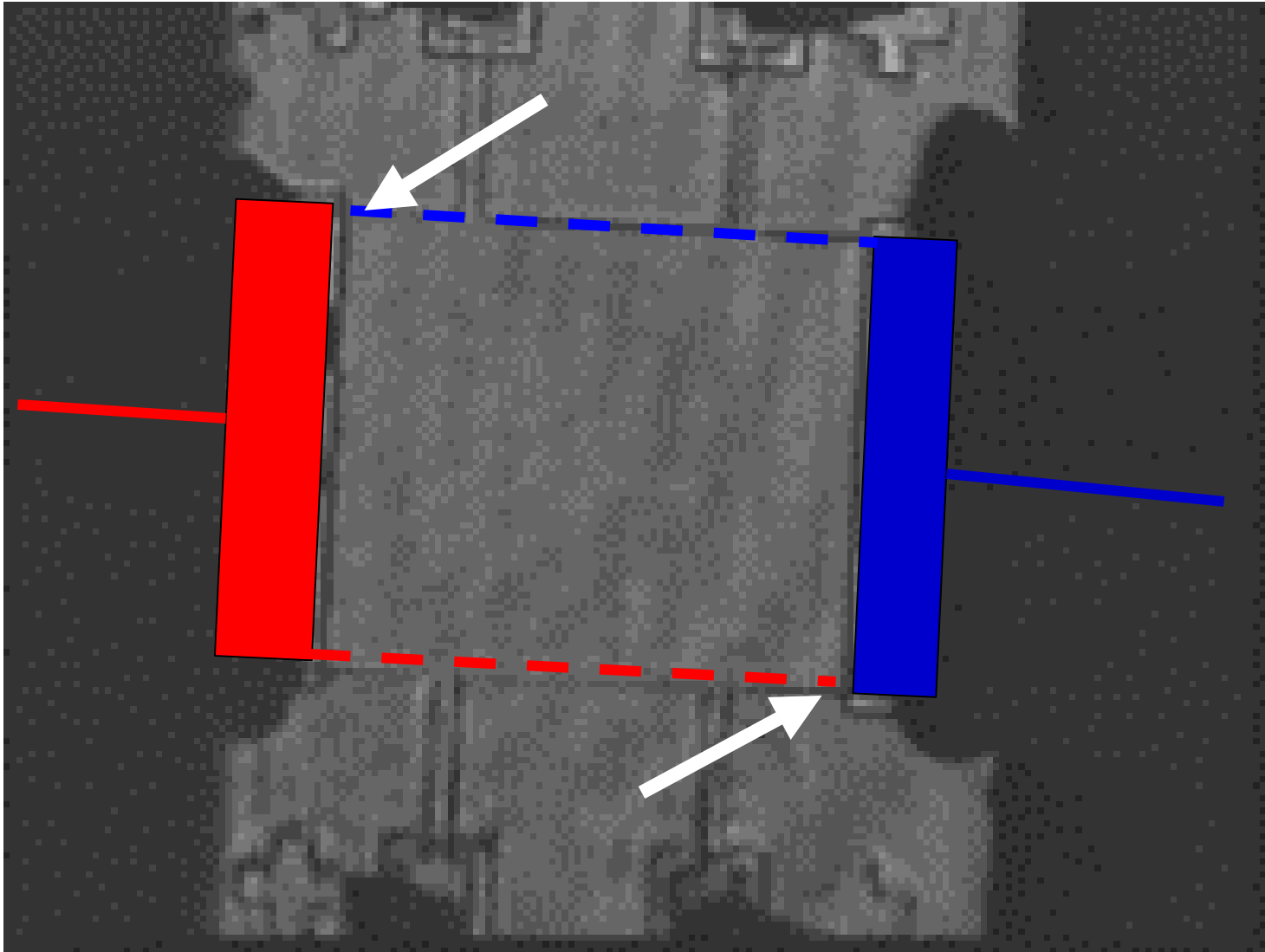


$B=B^-$





W. Dietsche and coworkers, MPI-FKF



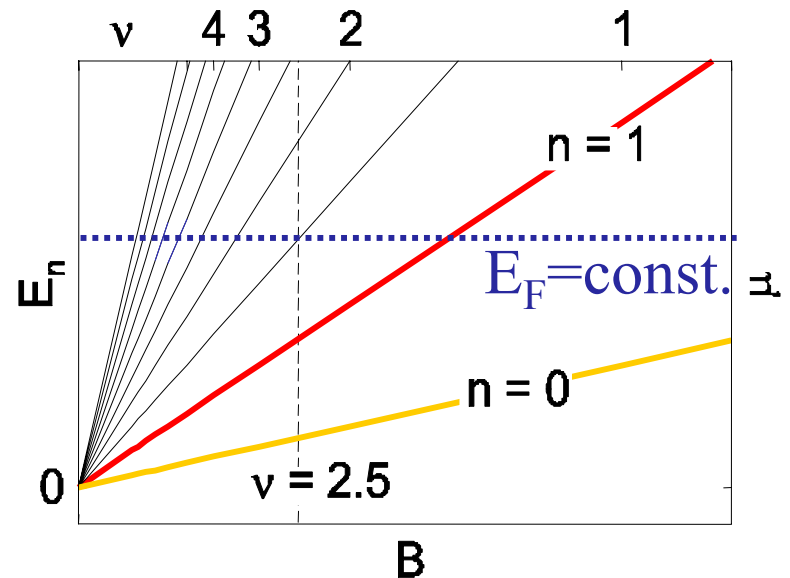
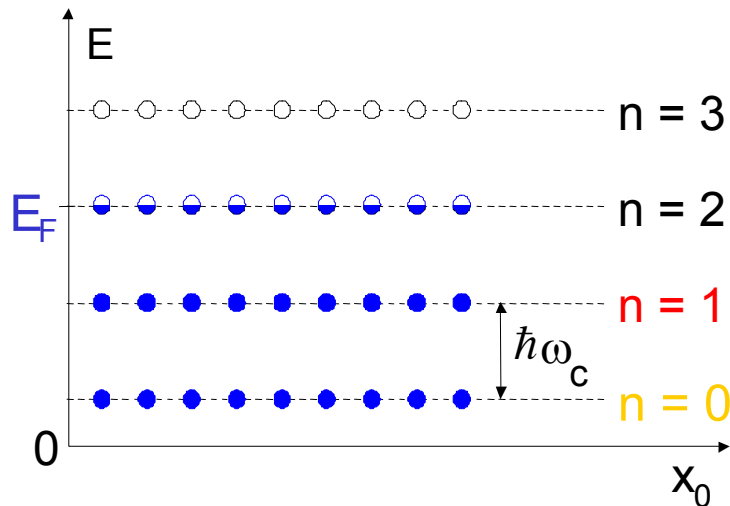
W. Dietsche and coworkers, MPI-FKF

PHYSICS OF QHE

Energy Gaps (e.g. cyclotron energy $\hbar\omega_c$)

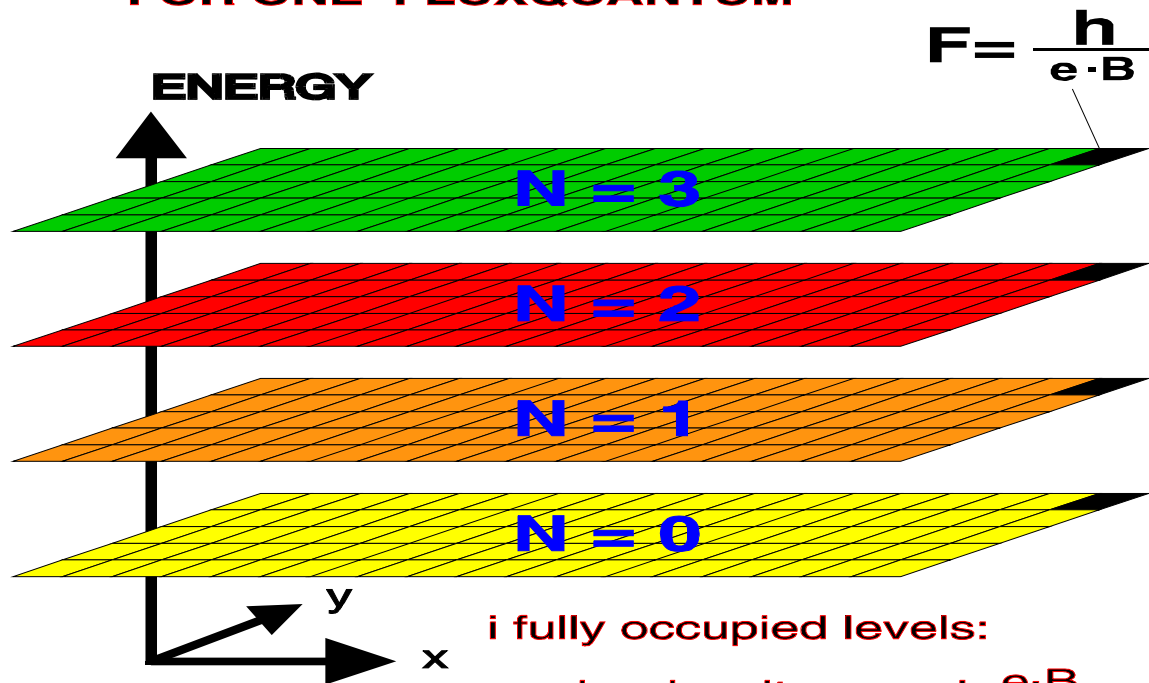
Homogeneous 2DES

(no spin, no edges, no disorder, no el.-el. interaction)



Each electronic state
 $E(N,s)$ occupies in real
 space the area $F = \frac{h}{e \cdot B}$
 (flux $F \cdot B = h/e$)

**FILLING FACTOR =
 NUMBER OF ELECTRONS
 FOR ONE FLUXQUANTUM**



i fully occupied levels:
 carrier density $n_s = i \cdot \frac{e \cdot B}{h}$

HALLEFFECT: $U_H = \frac{B}{n_s \cdot e} \cdot I = \frac{h}{i \cdot e^2} \cdot I$

Explanation of QHE

(Deutsches Museum Bonn)

Discrete energy levels for two-dimensional electron system (size quantization) in strong magnetic fields (Landau quantization)

Classical Hall effect if an integer number i of energy levels is fully occupied with electrons:

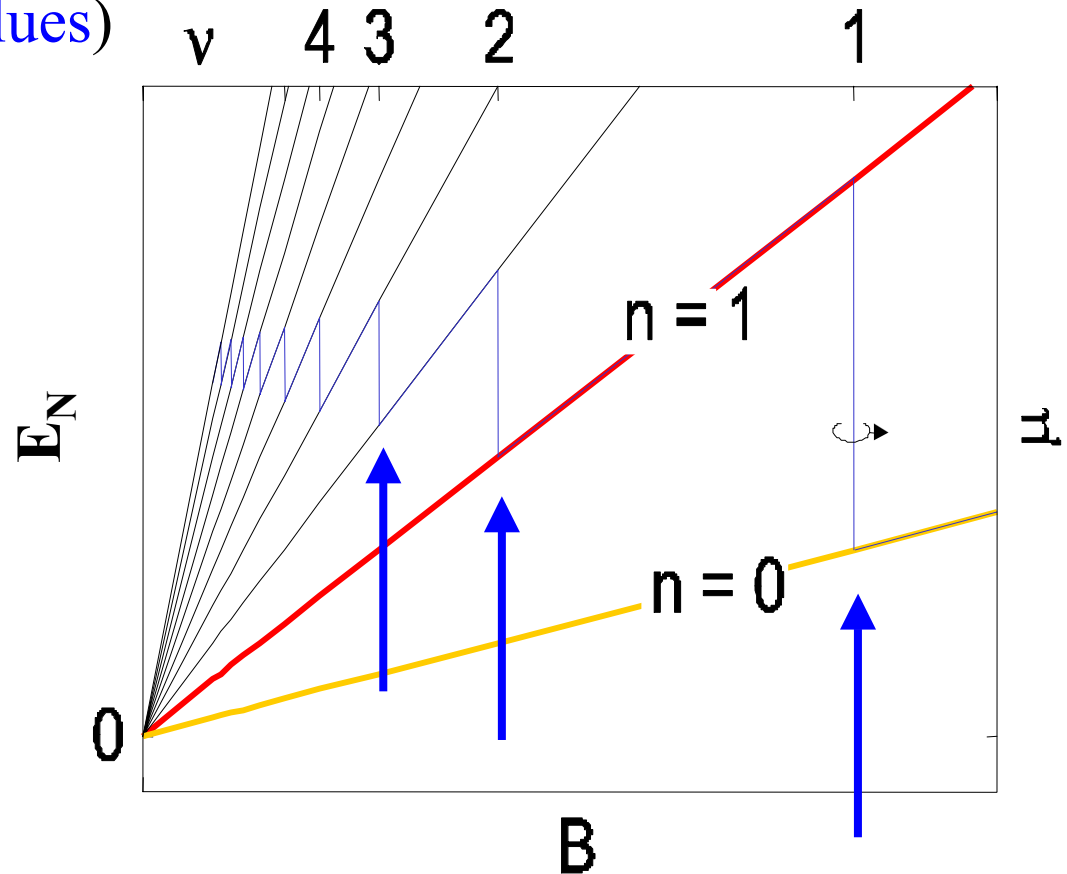
$$U_H = \frac{h}{i \cdot e^2} \cdot I$$

(useful for Ph.D. examination with correct result but
INCORRECT DEVIATION!)

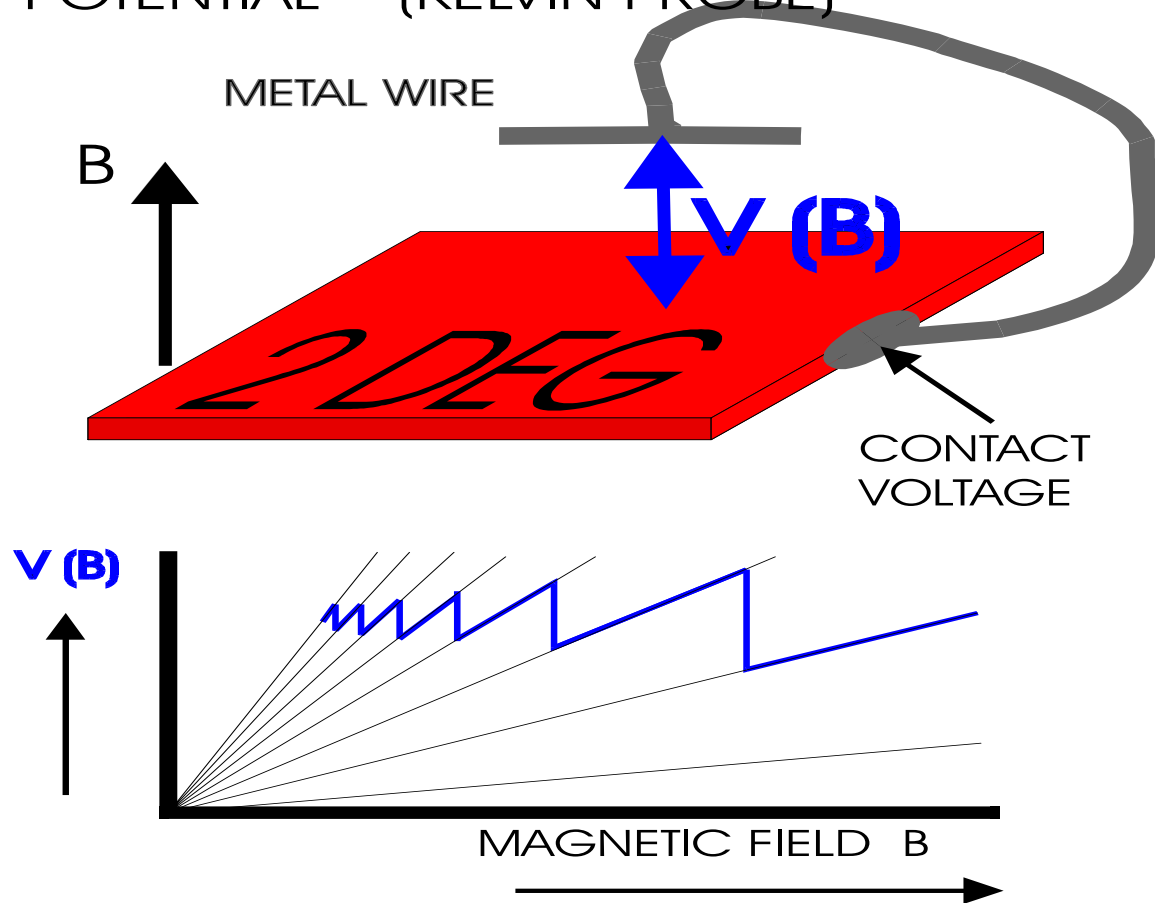
PROBLEMS:

#1: **NO** quantum Hall **plateaus** since Fermi energy jumps (the condition of **fully occupied Landau level** is fulfilled **only for very special magnetic field values**)

#2: Real samples with finite size have **NO GAPS** in the energy spectrum!

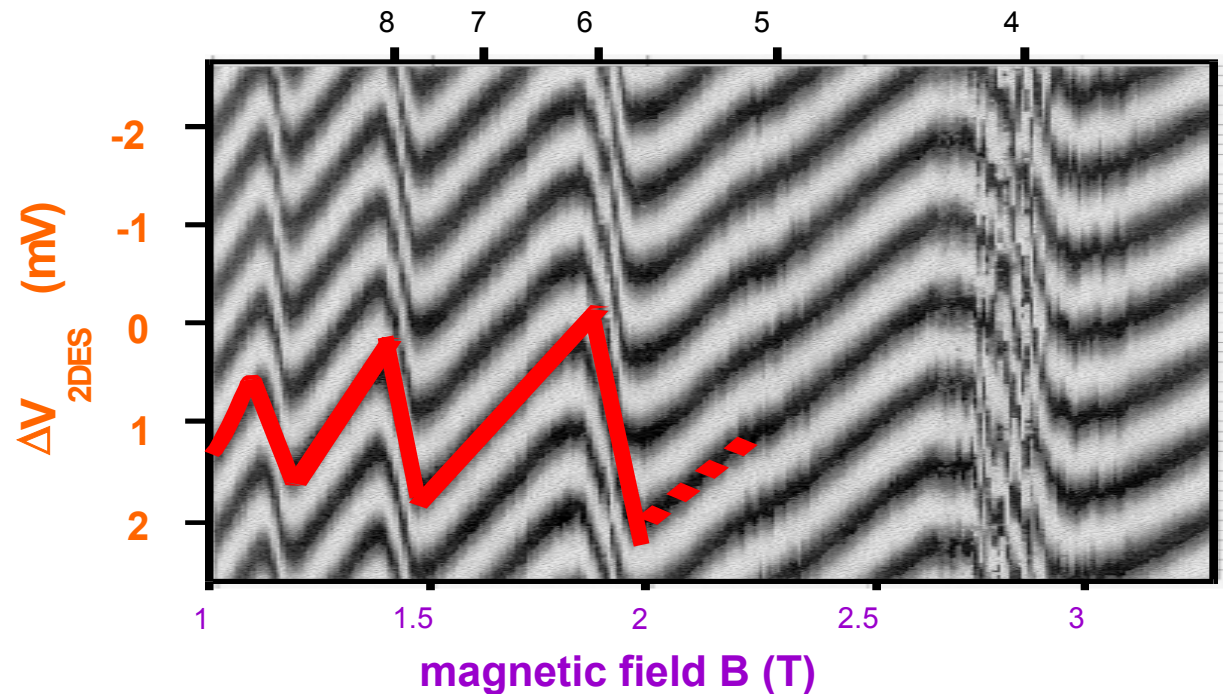
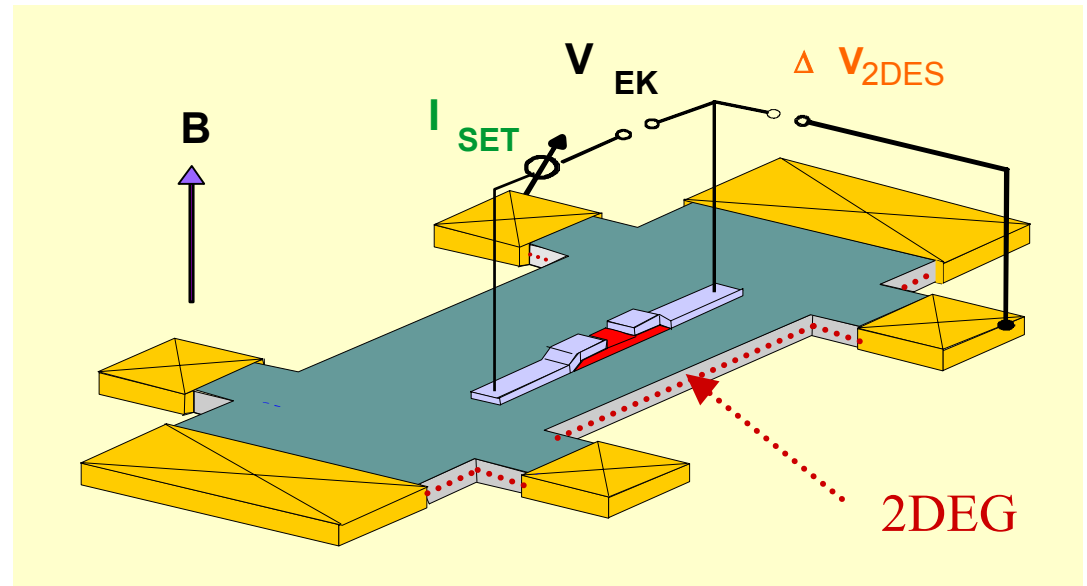


THERMODYNAMIC EQUILIBRIUM:
CONSTANT ELECTROCHEMICAL
POTENTIAL (KELVIN PROBE)



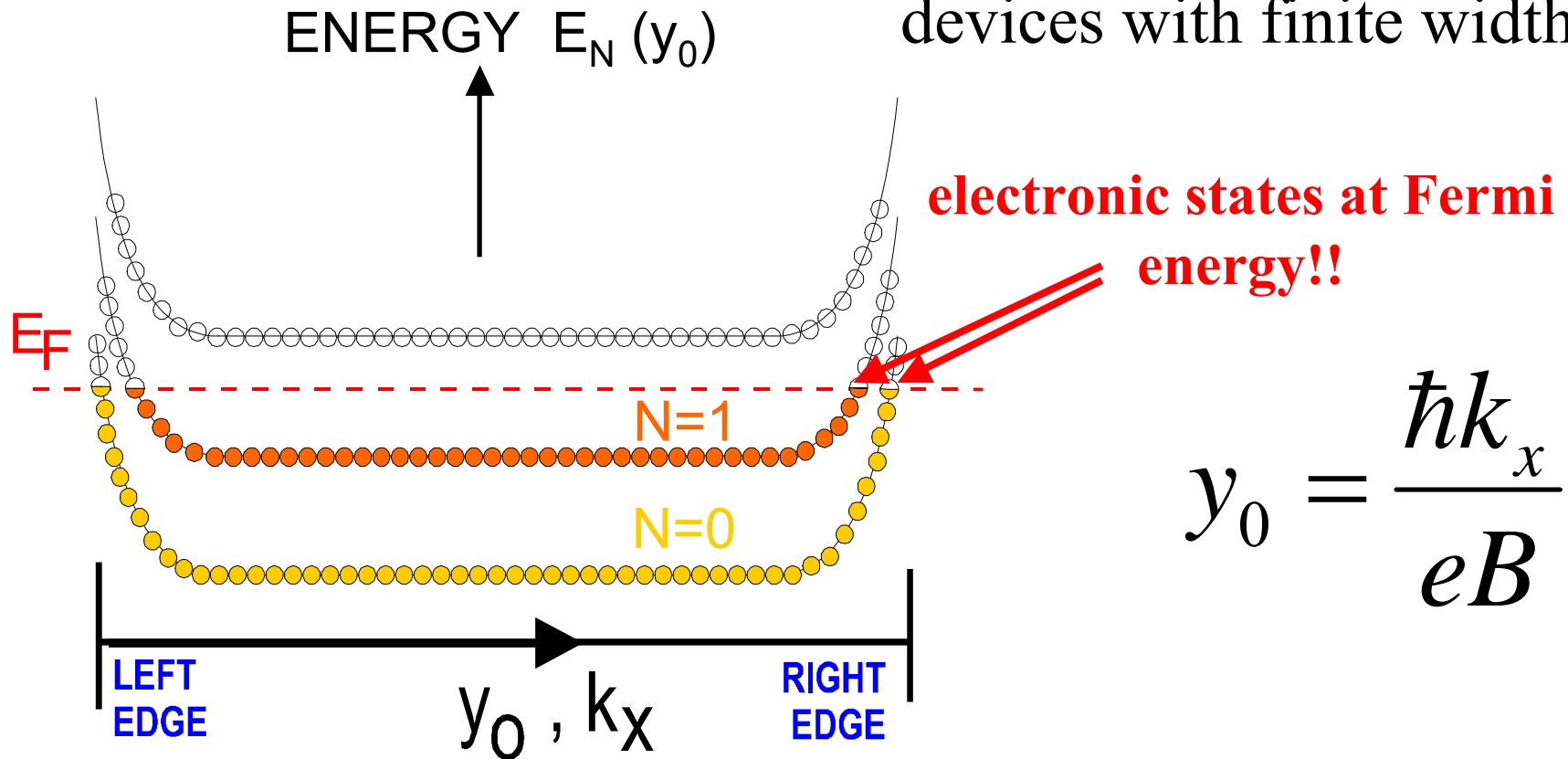
Single Electron Transistor (SET)

as an extremely sensitive
electrometer for measurements
on a 2DEG



Problem #2

NO energy gaps for real devices with finite width

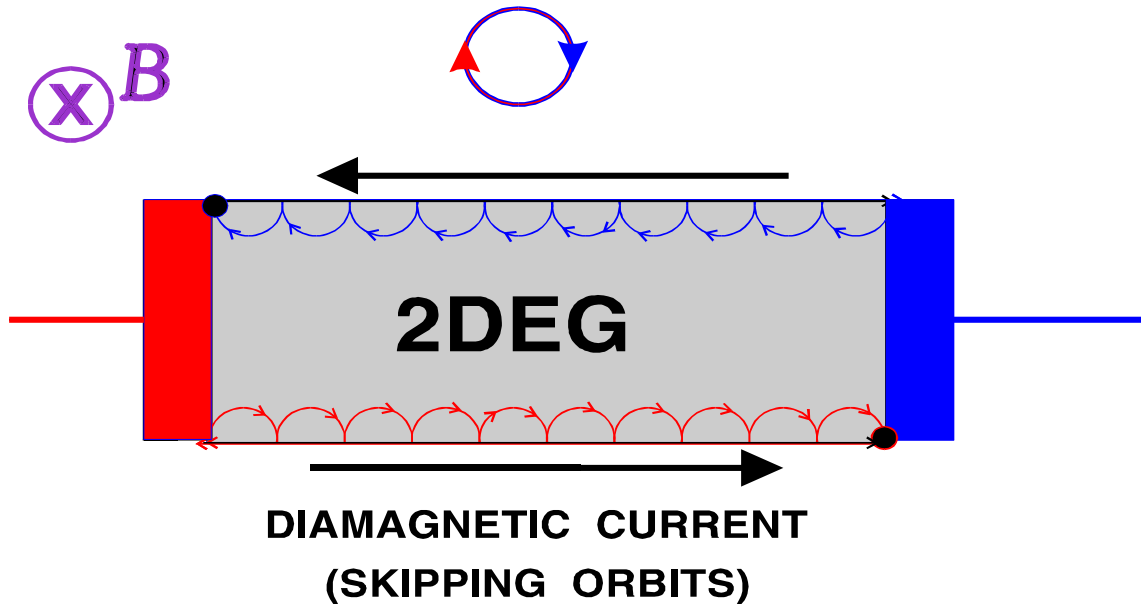


$$y_0 = \frac{\hbar k_x}{eB}$$

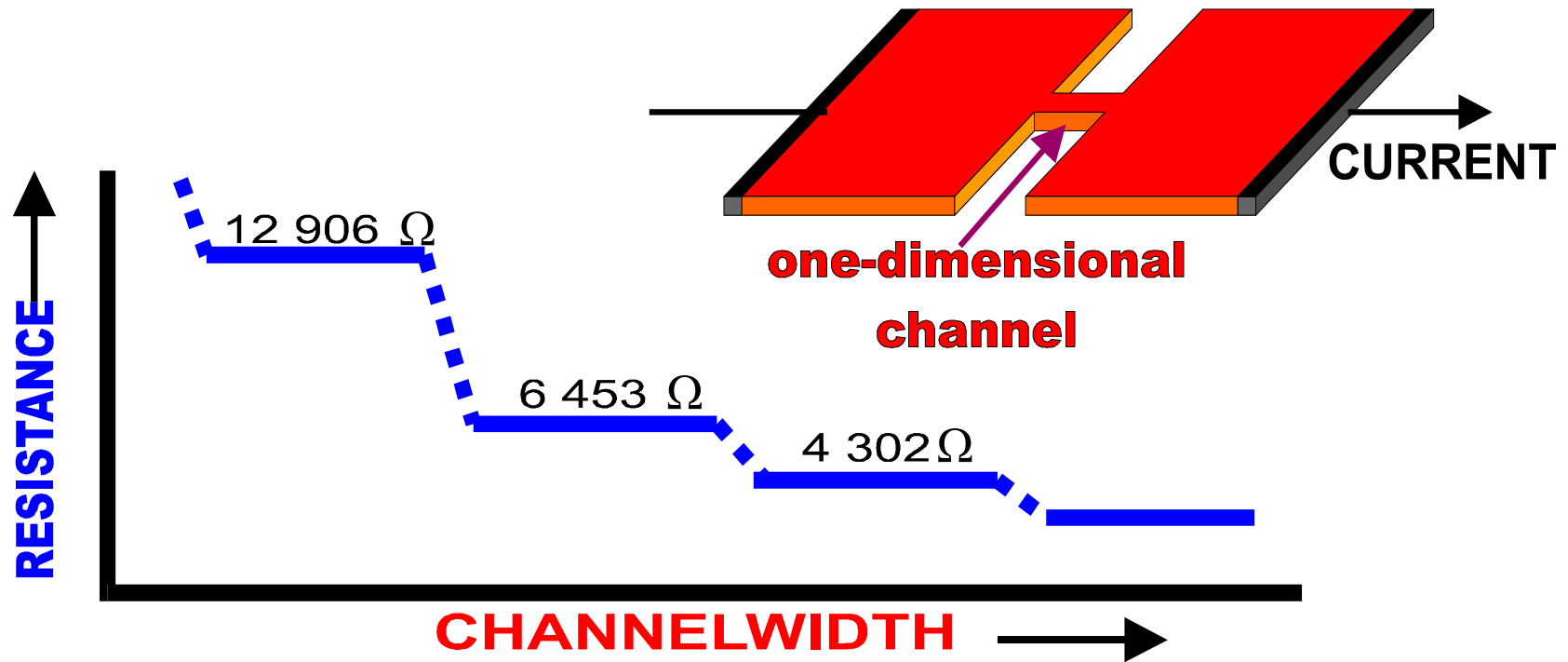
$$\Psi_{N,y_0} \propto e^{ik_x x} \cdot \Phi_N(y - y_0)$$

2DEG IN THE QHE-REGIME
CORRESPONDS TO AN IDEAL
ONE - DIMENSIONAL SYSTEM
WITHOUT SCATTERING
(EDGE CHANNELS)

Classical cyclotron motion:

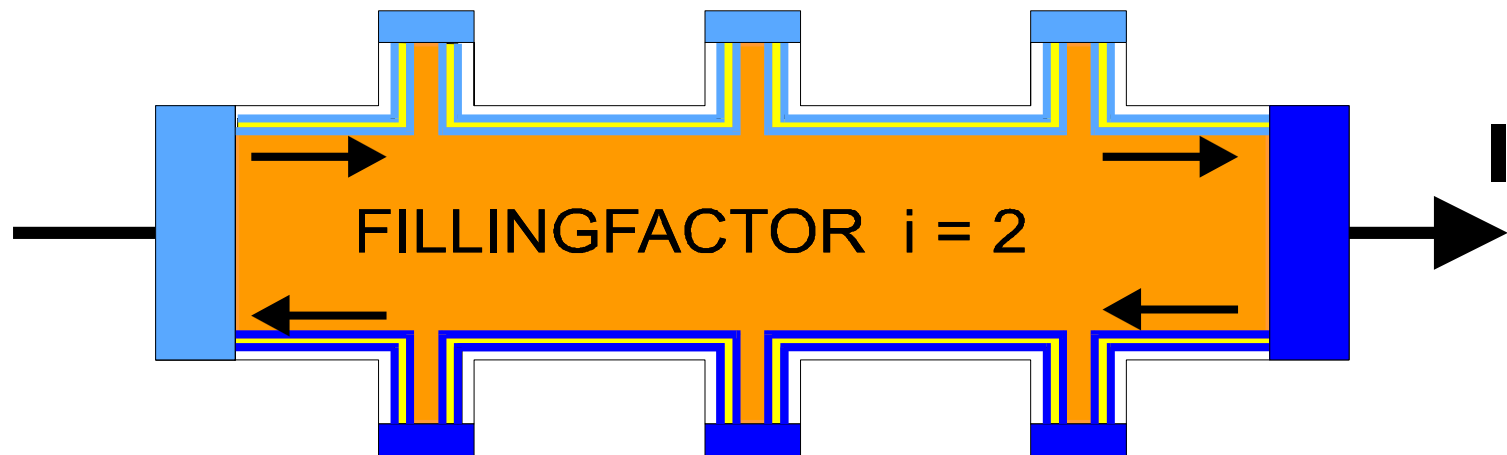


THE ELECTRICAL RESISTANCE OF A CONSTRICTION IS DETERMINED BY THE NUMBER OF ONE-DIMENSIONAL CHANNELS
(each channel contributes to the conductance with $2e^2/h$)



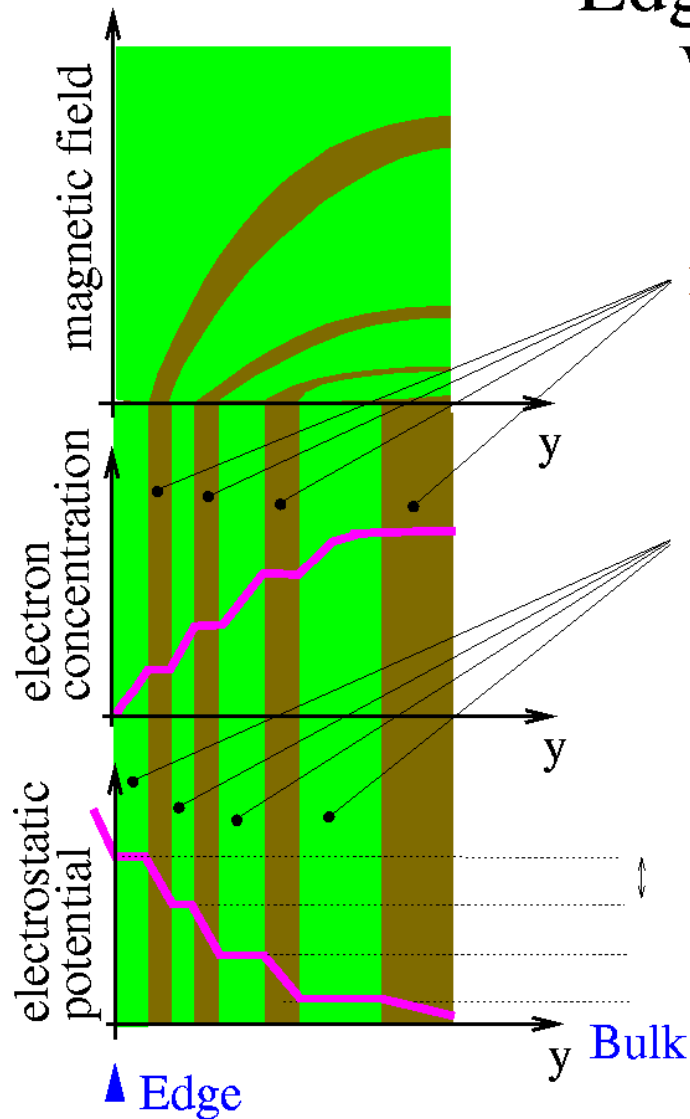
LANDAUER BÜTTIKER FORMALISM

UNDER QUANTUM HALL CONDITIONS



NO BACKSCATTERING!

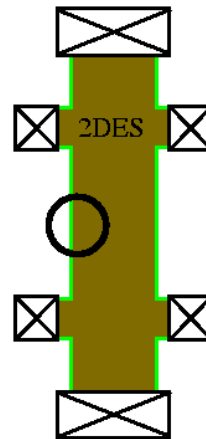
Edge Strips Evolving With Magnetic Field



incompressible strips

- not conducting
- electrical isolating
- not screening

compressible strips



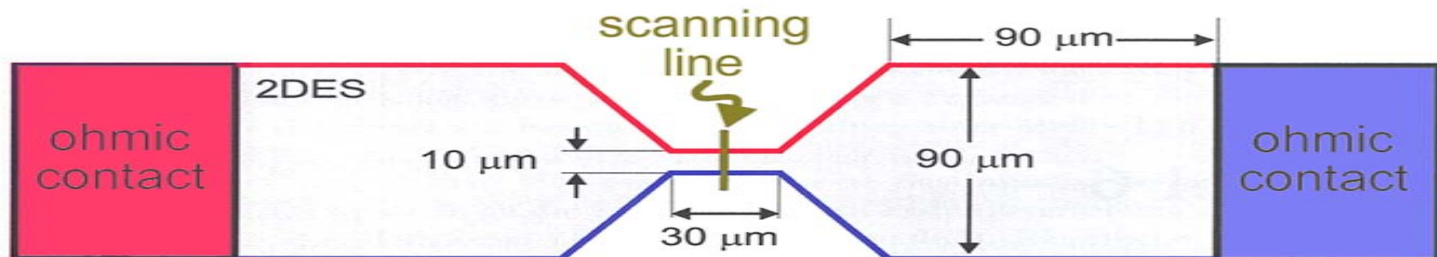
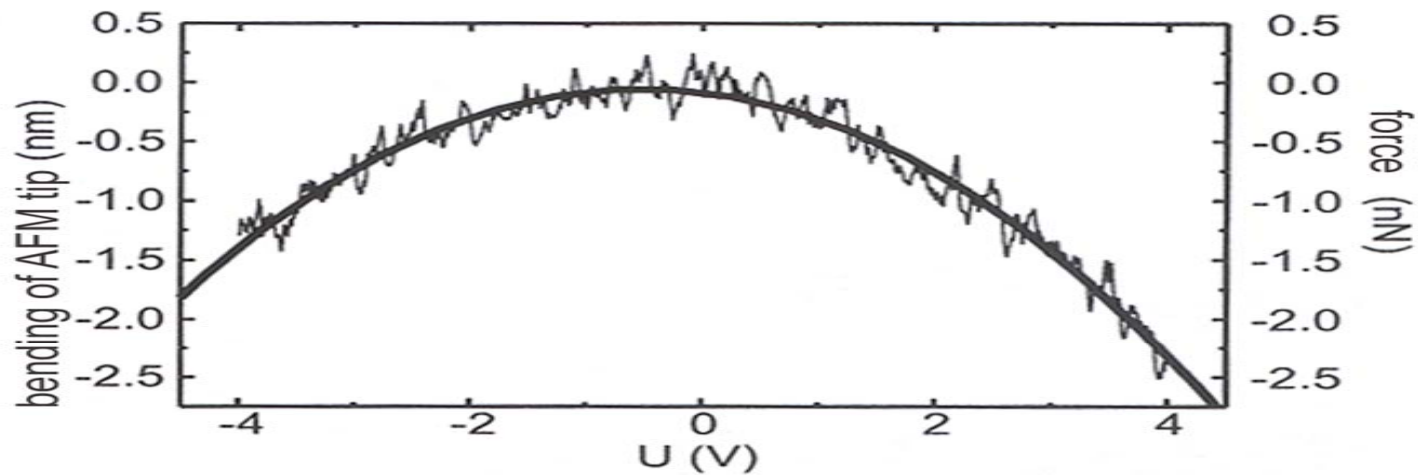
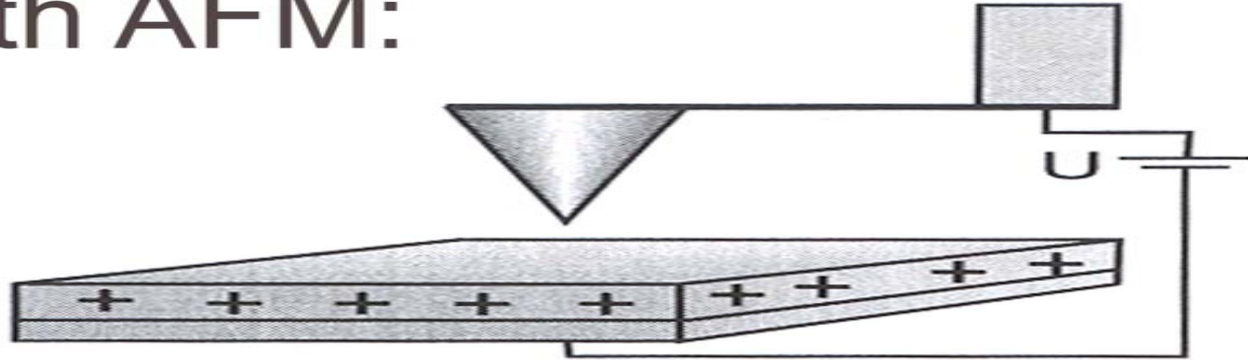
K. Lier and R.R. Gerhardtts,
Phys. Rev. B 50, 7757 (1994).

Chklovskii, Shklovskii, Glazman,
Phys. Rev. B 46, 4026 (1992).

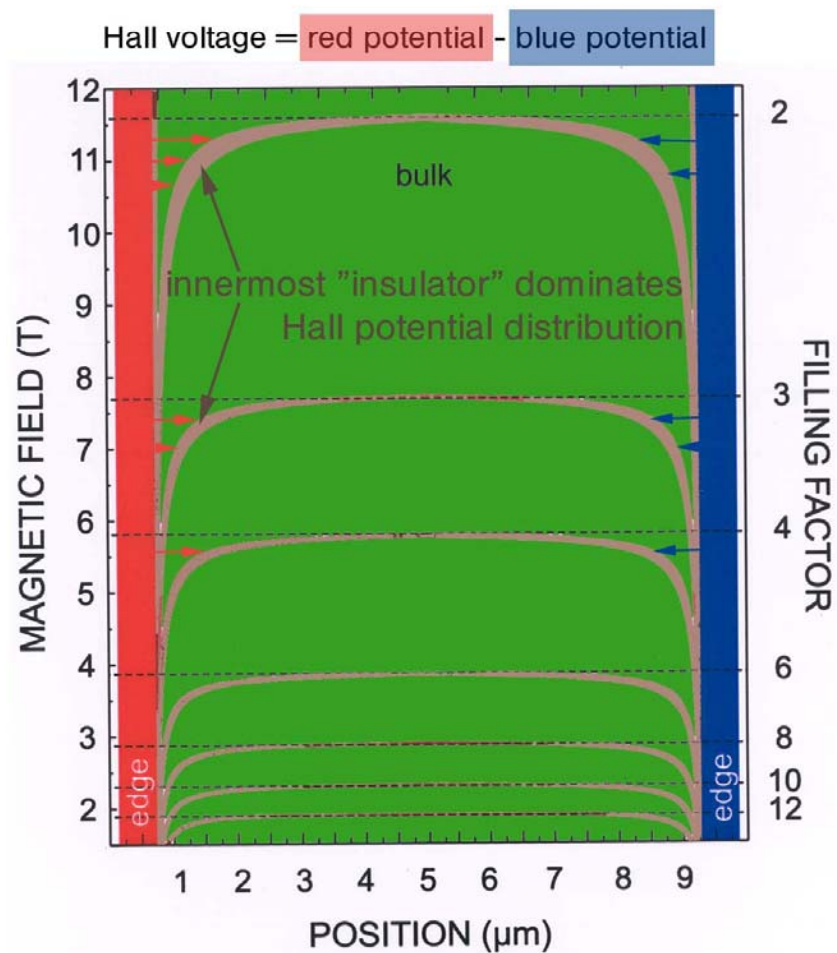
Chklovskii, Matveev, and Shklovskii
Phys. Rev. B 47, 12605 (1993).

more than 100 nm!!

Locally resolved potential with AFM:

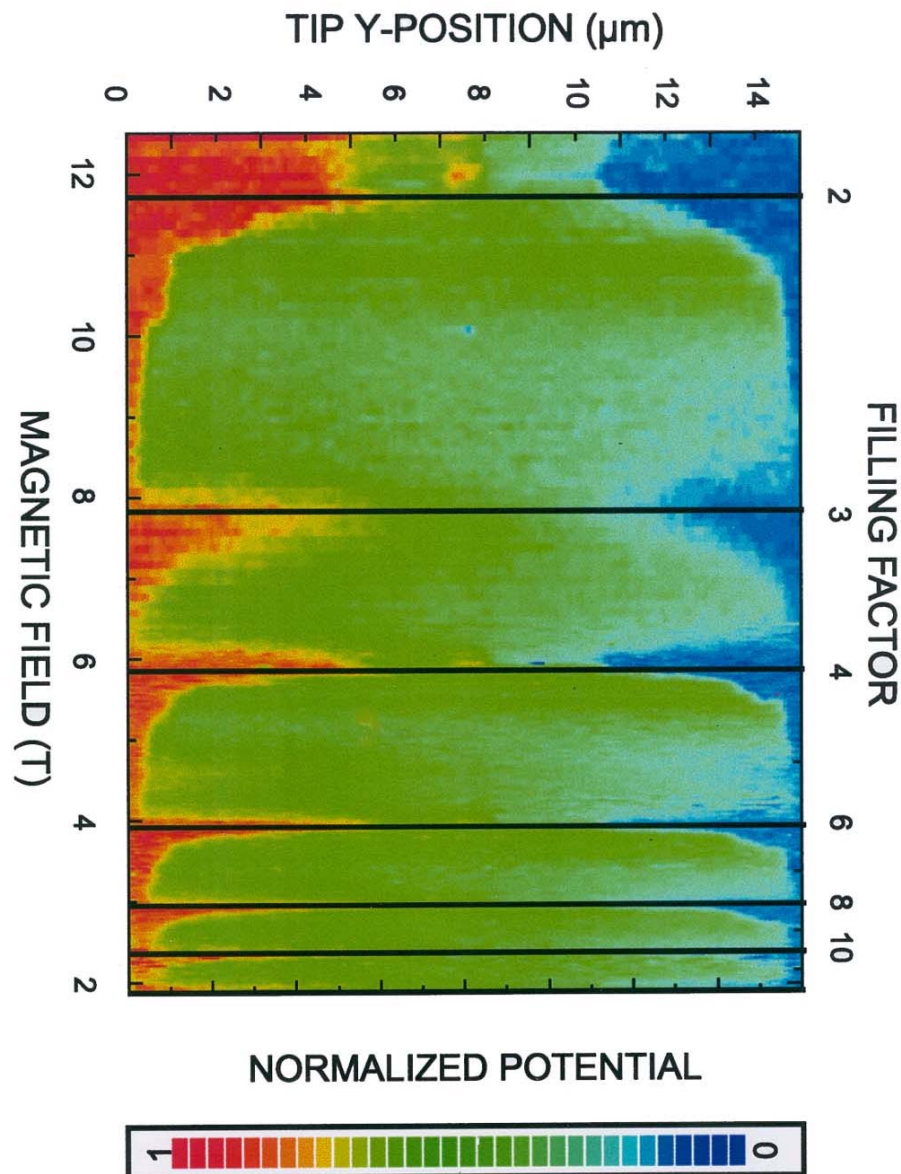


POSITION OF **INCOMPRESSIBLE**
(= INSULATING) REGIONS AS A
FUNCTION OF MAGNETIC FIELD

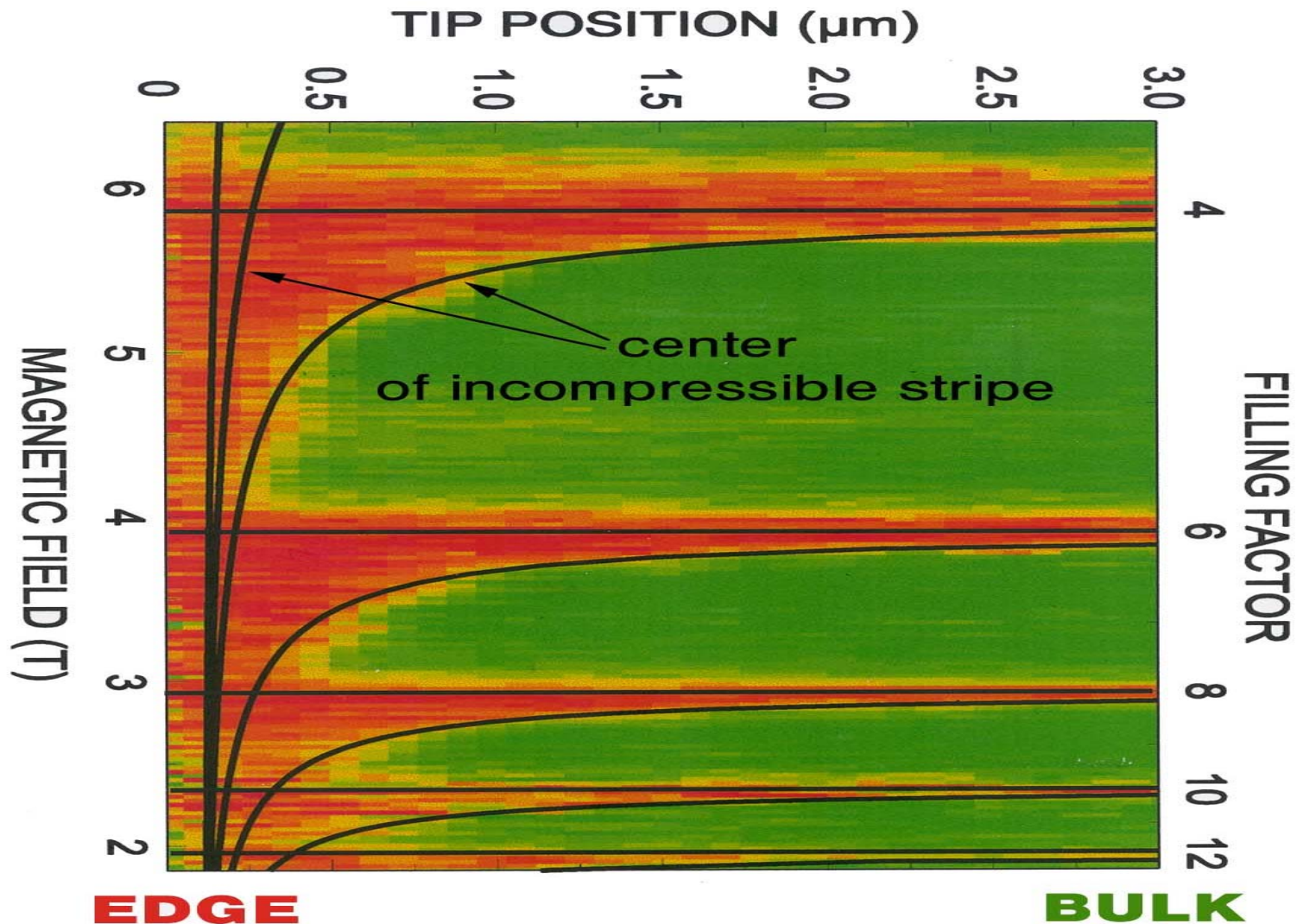


AFM-Measurement of the Hall Potential

(E. Ahlswede, J Weis, P. Weitz)

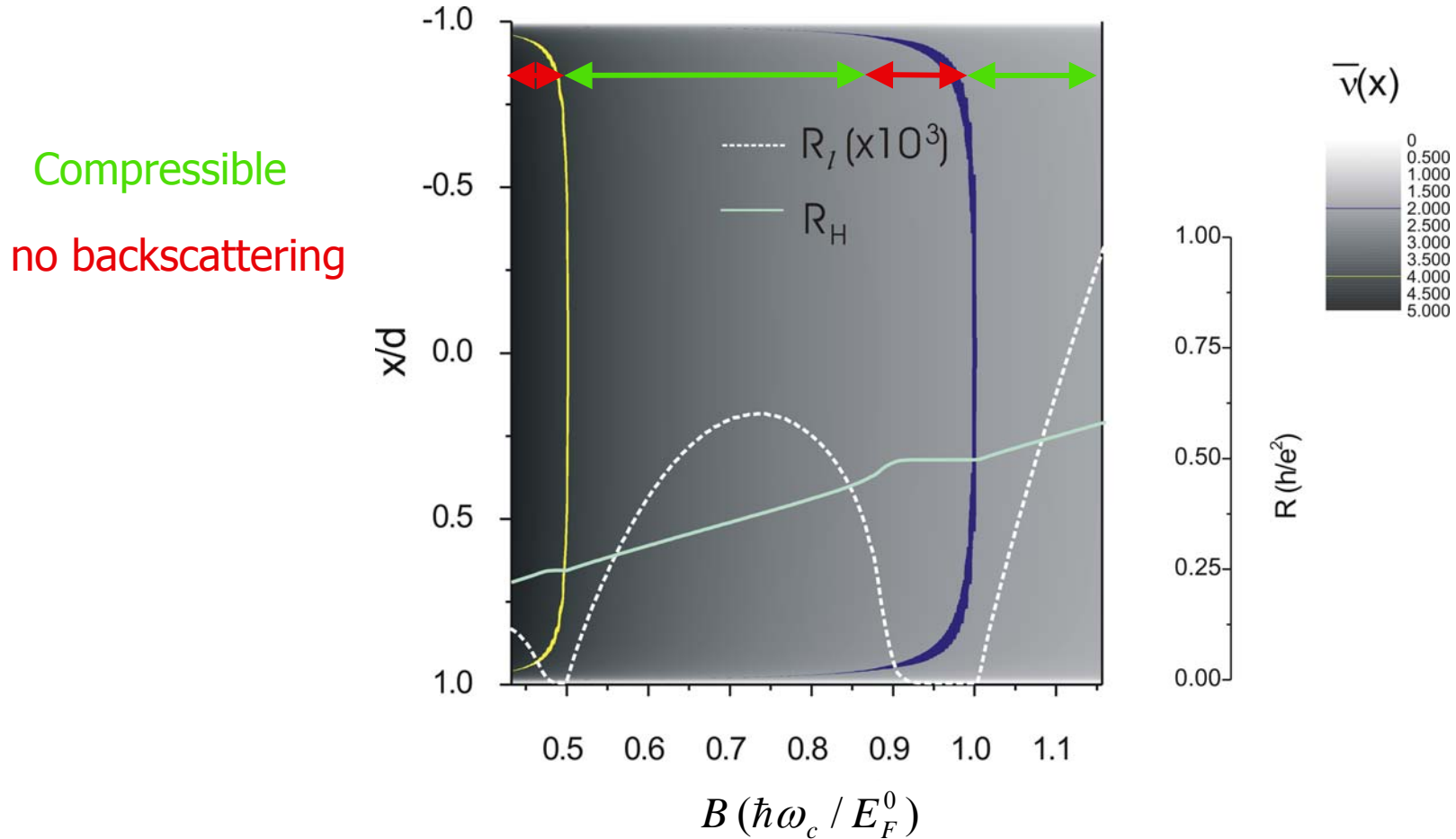


HALL POTENTIAL DISTRIBUTION CLOSE TO THE EDGE



Calculation for an ideal system with finite size

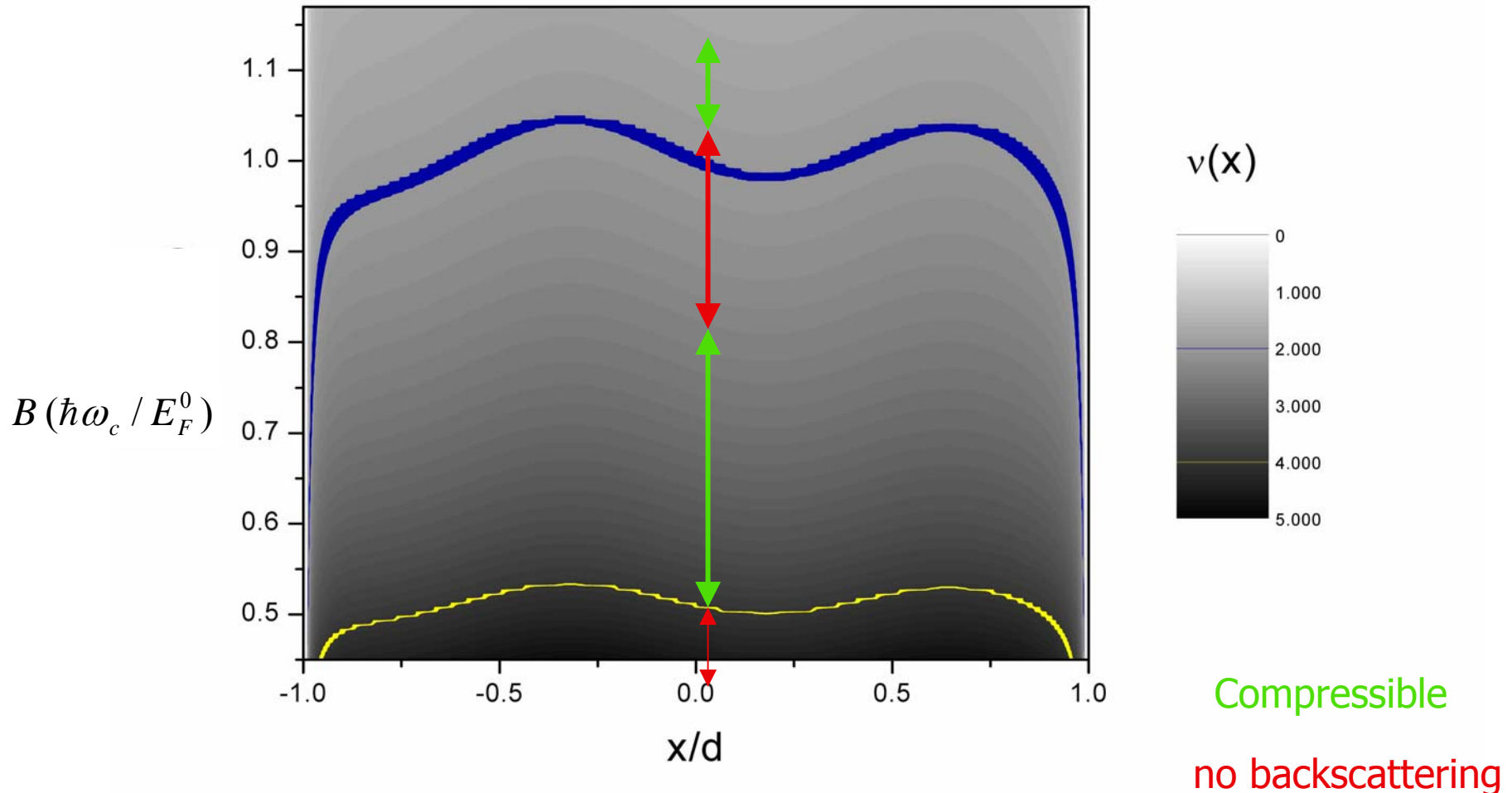
(*R. Gerhardt, A. Siddiki*)

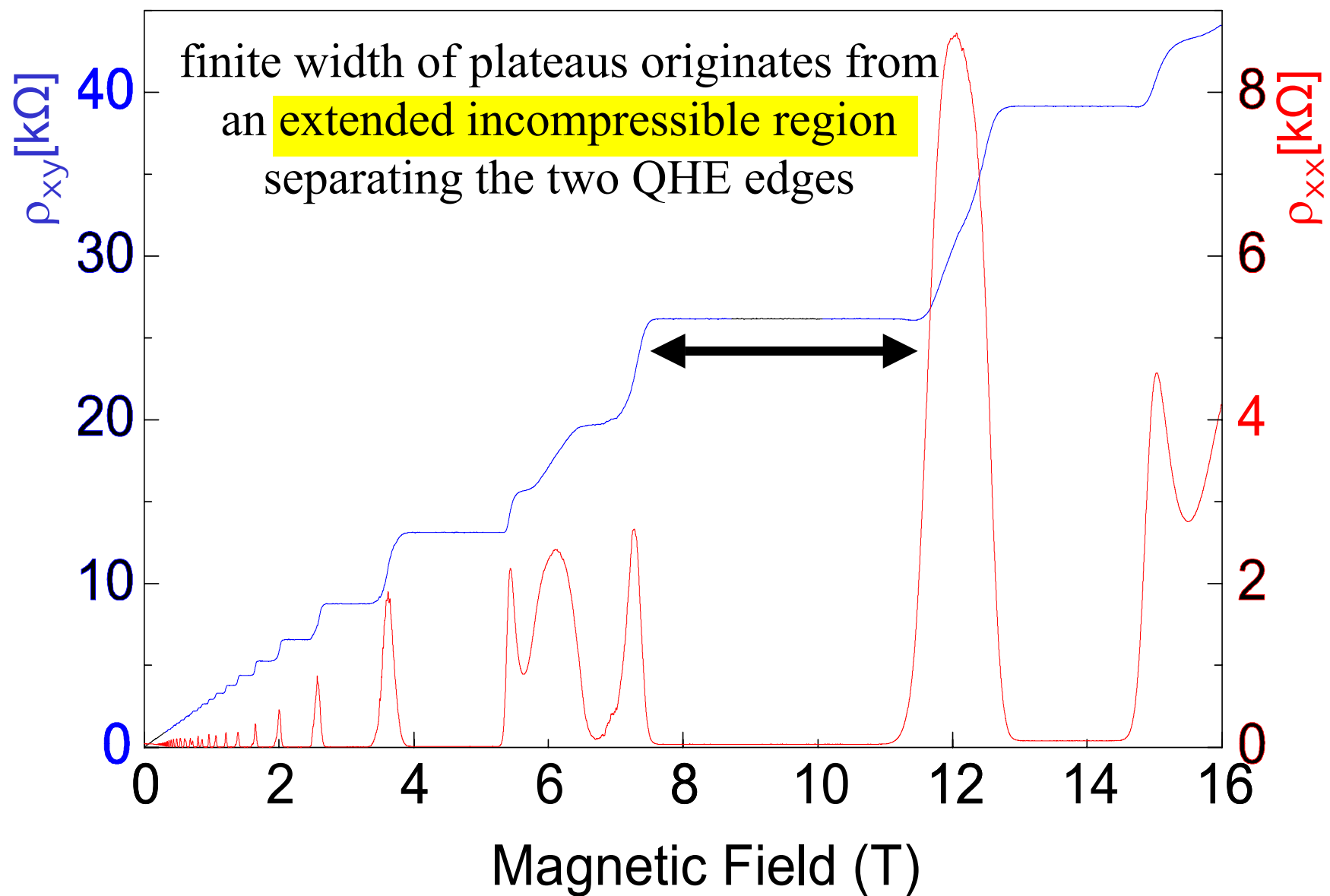


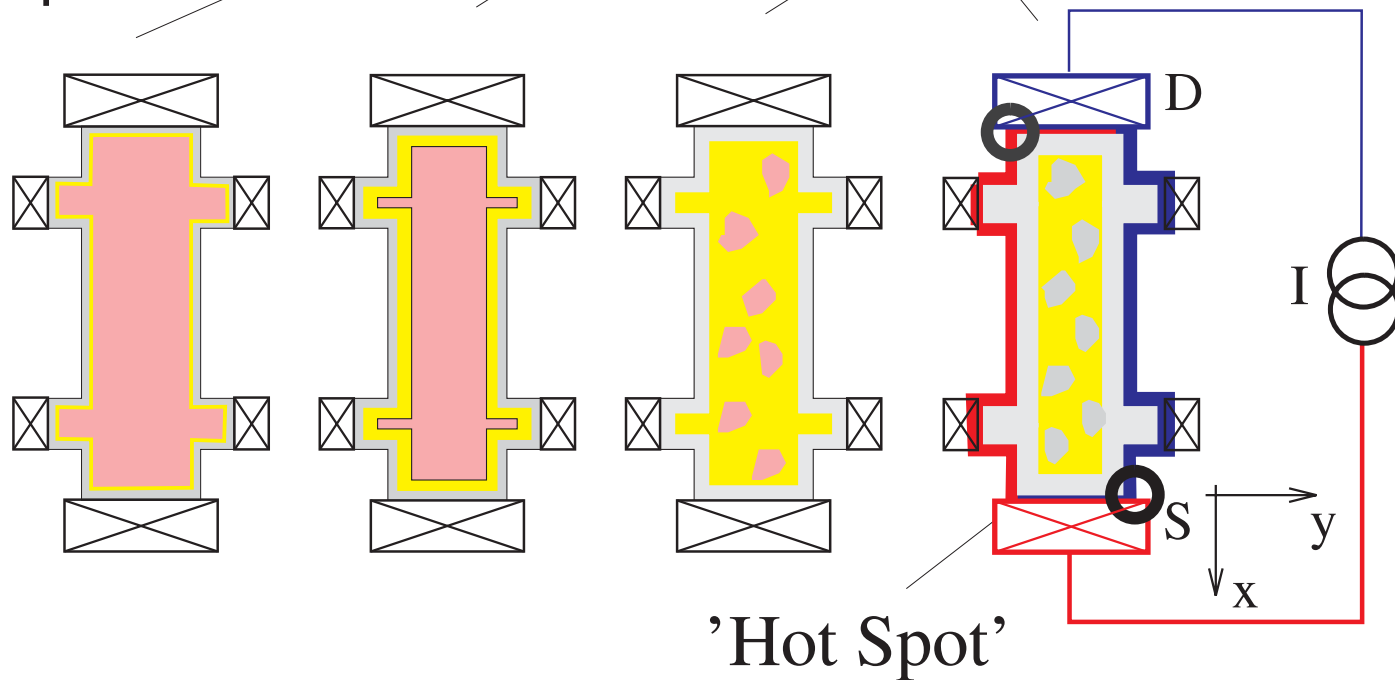
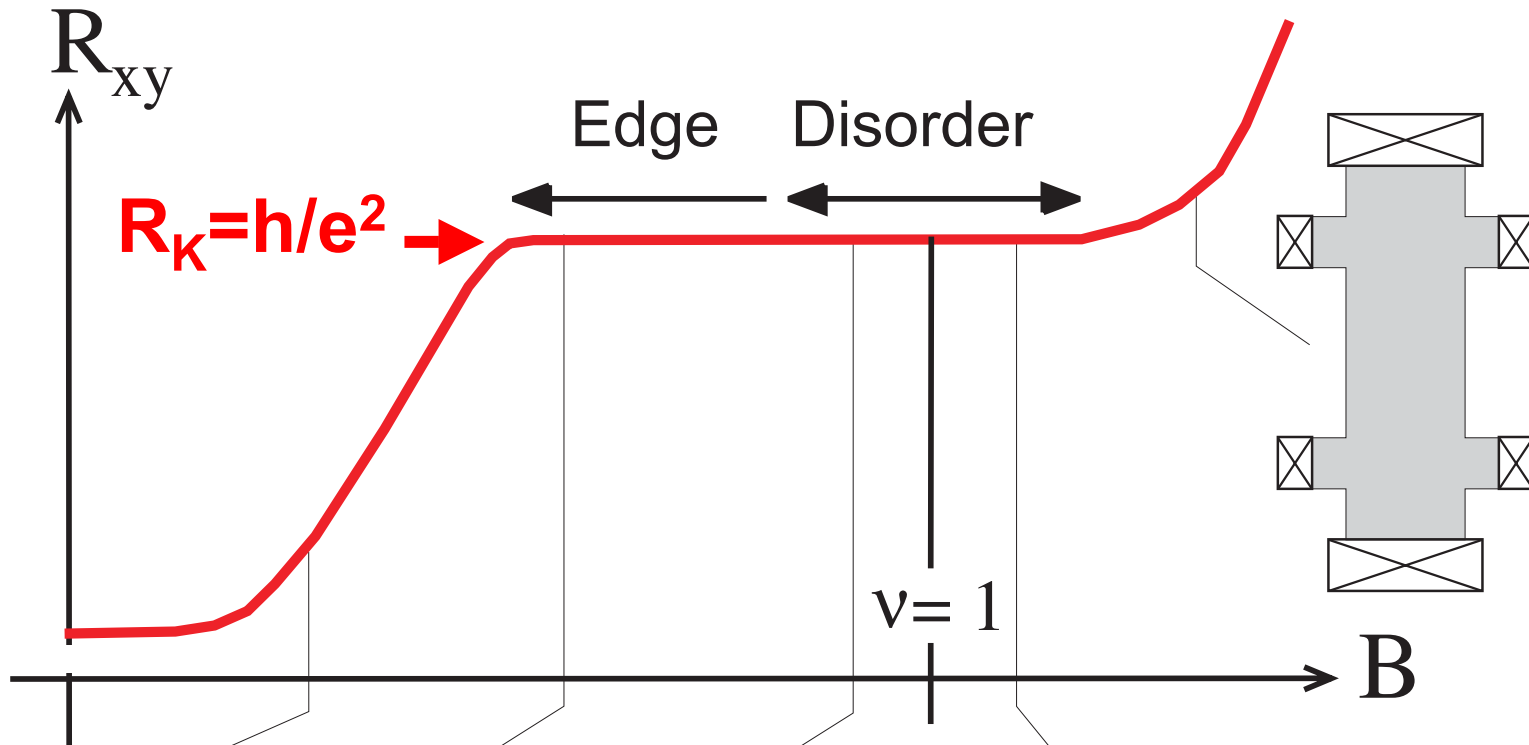
Theory with one-dimensional disorder

(R.Gerhardts, A.Siddiki)

15 μm sample with some random disorder



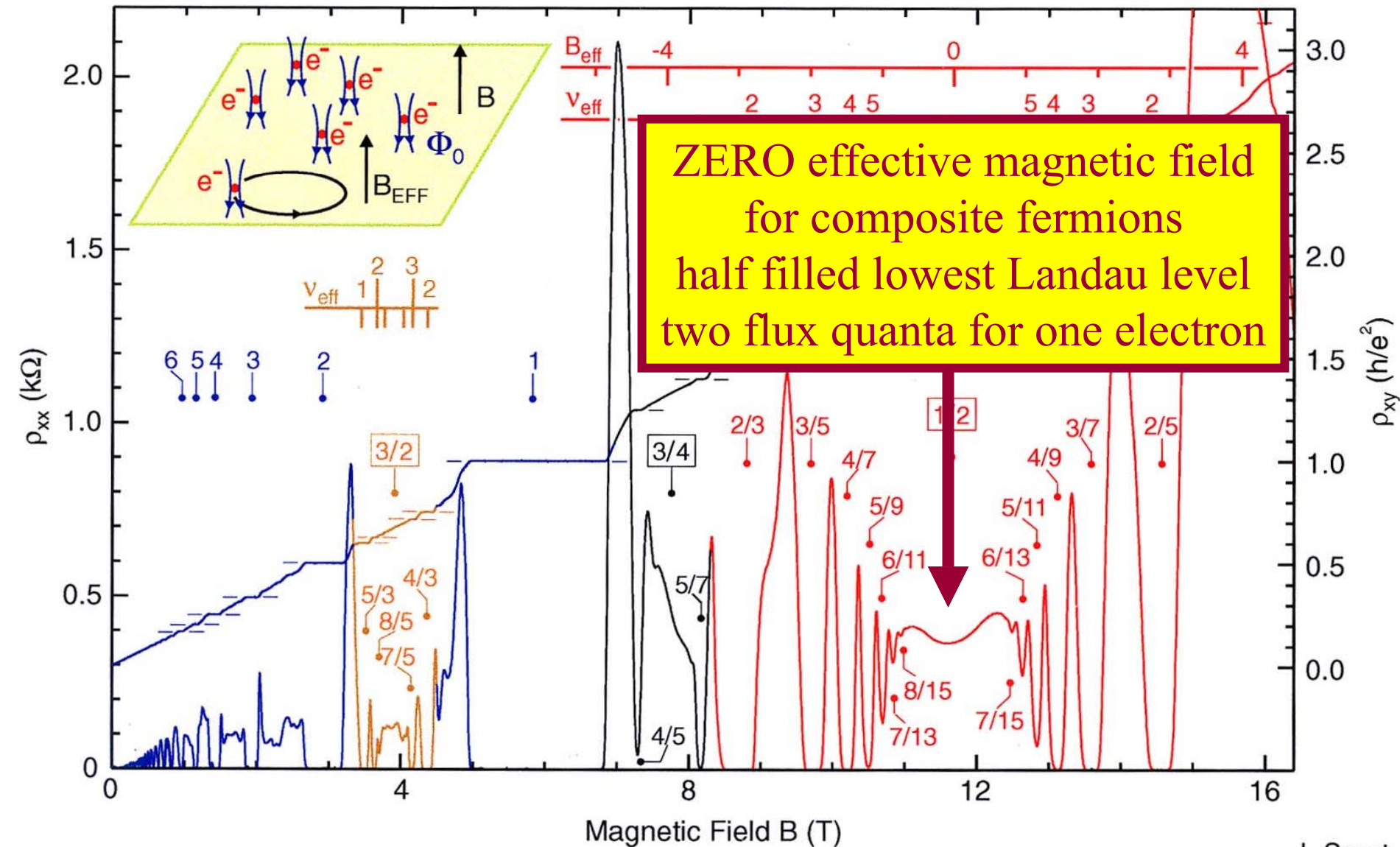




NEW ENERGY GAPS DUE TO ELECTRON-ELECTRON INTERACTION

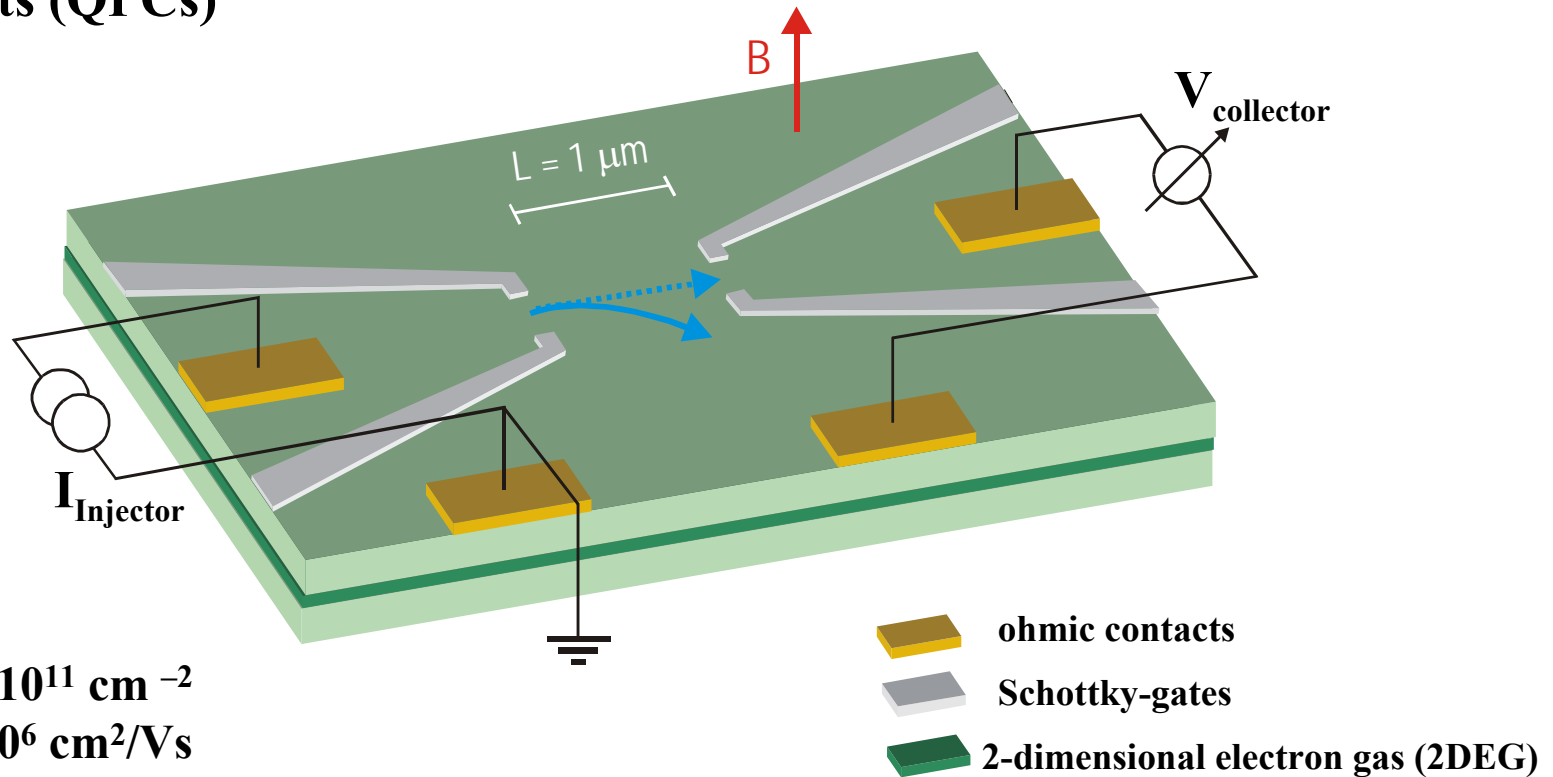
(fractional quantum Hall effect)

Similarity between IQHE and FQHE

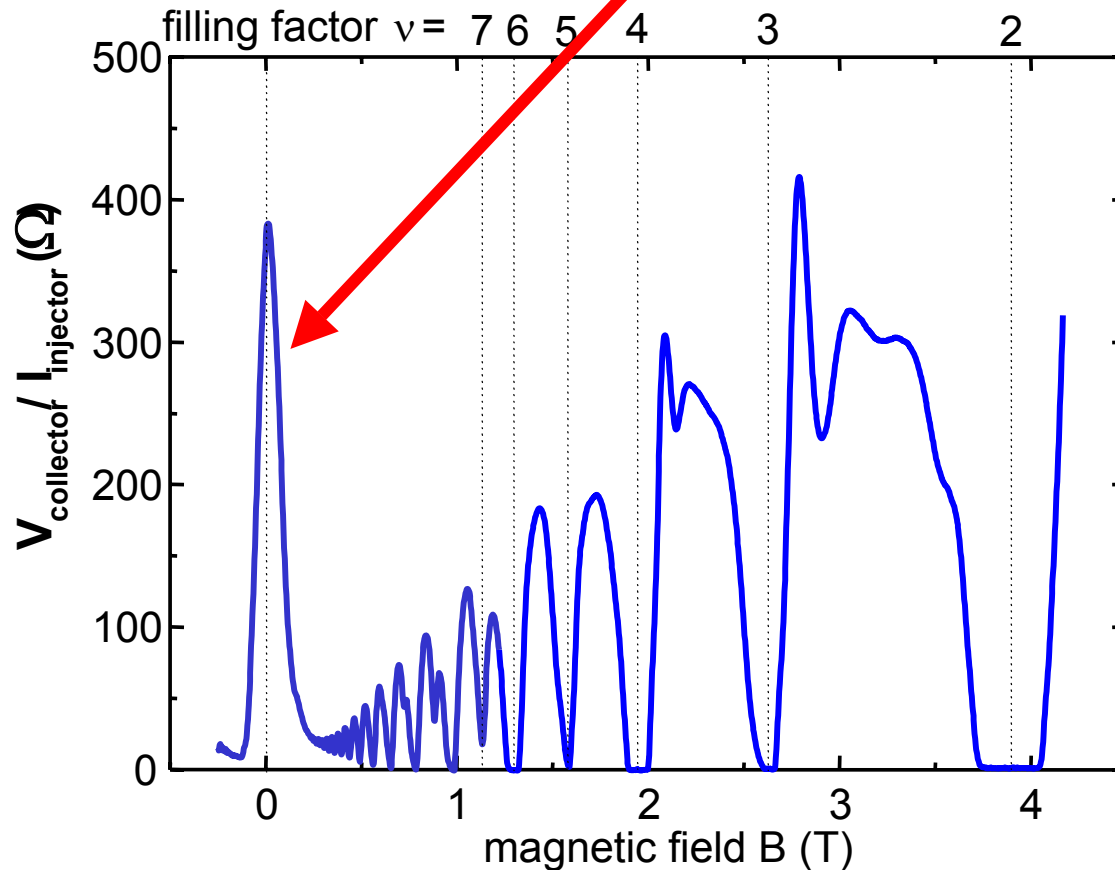


Ballistic transport – electrons and Composite Fermions

- high mobility 2-dimensional electron gas with long mean free path forms at the interface of an GaAs/AlGaAs heterostructure
- lateral surface Schottky-gates define two opposing Quantum-Point-Contacts (QPCs)



Ballistic transport of electrons

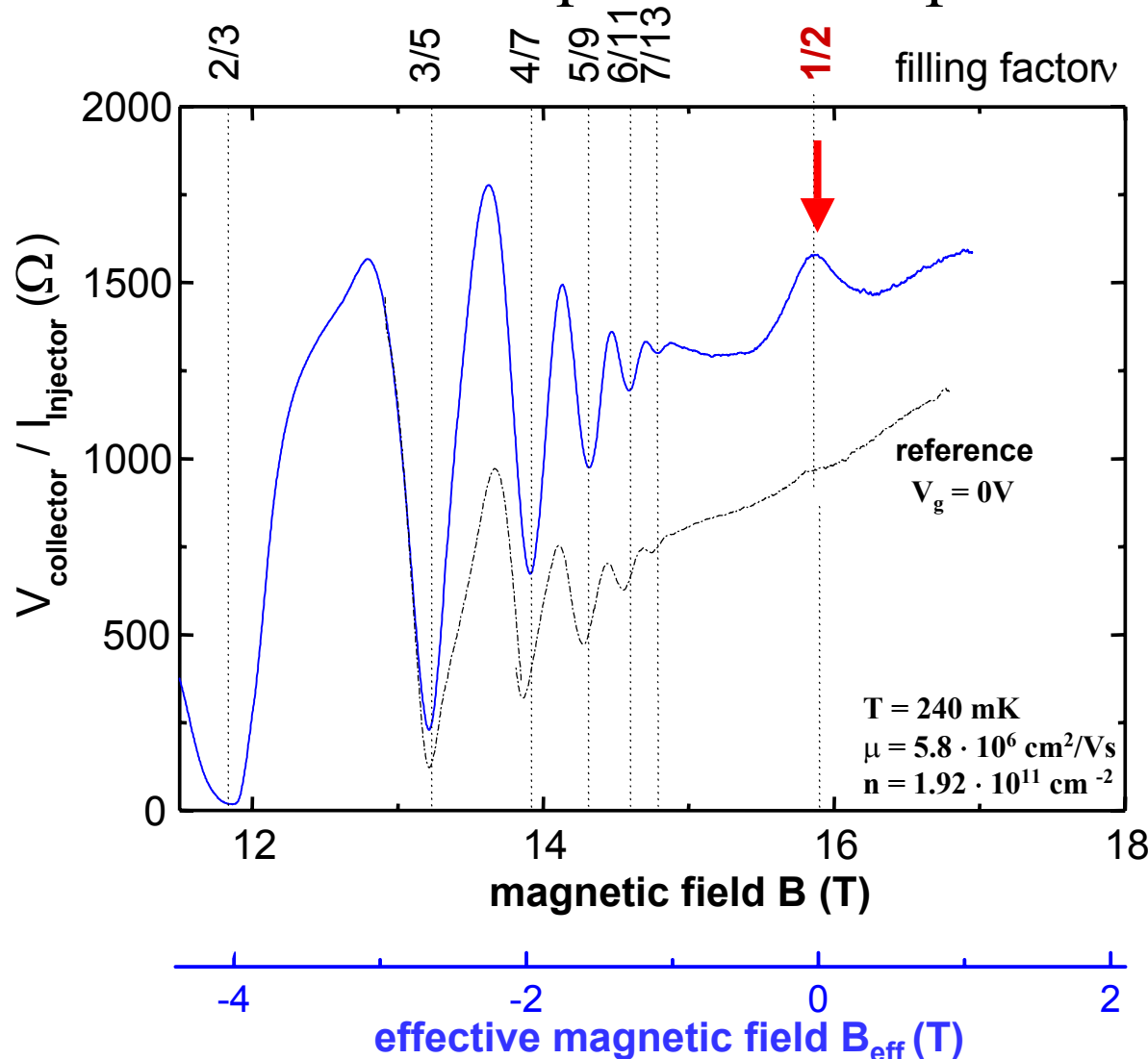


- at $B = 0$ straight, ballistic transport of electrons occurs from the injector to the collector Quantum-Point-Contact
- away from $B = 0$ Shubnikov-deHaas oscillations and the Quantum Hall Effect develop

$T = 240 \text{ mK}$
 $\mu = 5.8 \cdot 10^6 \text{ cm}^2/\text{Vs}$
 $n = 1.92 \cdot 10^{11} \text{ cm}^{-2}$

SIMILAR OBSERVATIONS IN STRONG MAGNETIC FIELDS (16 Tesla) ?

Ballistic transport of Composite Fermions (CFs)

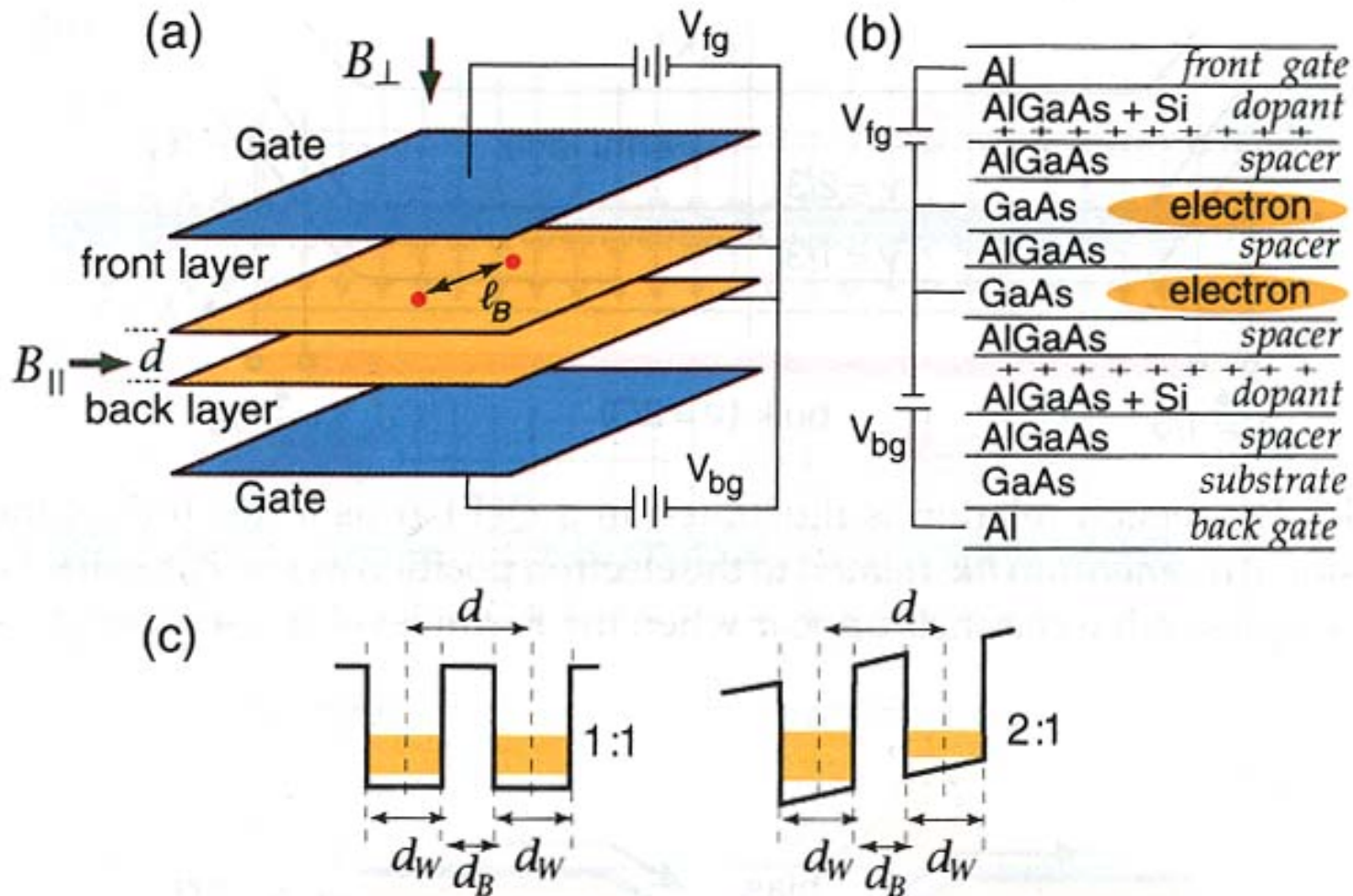


- CFs experience **effective magnetic field B_{eff}** , dramatically different from external field B
- existence of a Fermi sea of CFs at $B_{\text{eff}} = 0$ and Landau levels containing CFs at $B_{\text{eff}} \neq 0$
- Fractional Quantum Hall Effect of electrons can be viewed as Integer Quantum Hall Effect of CFs

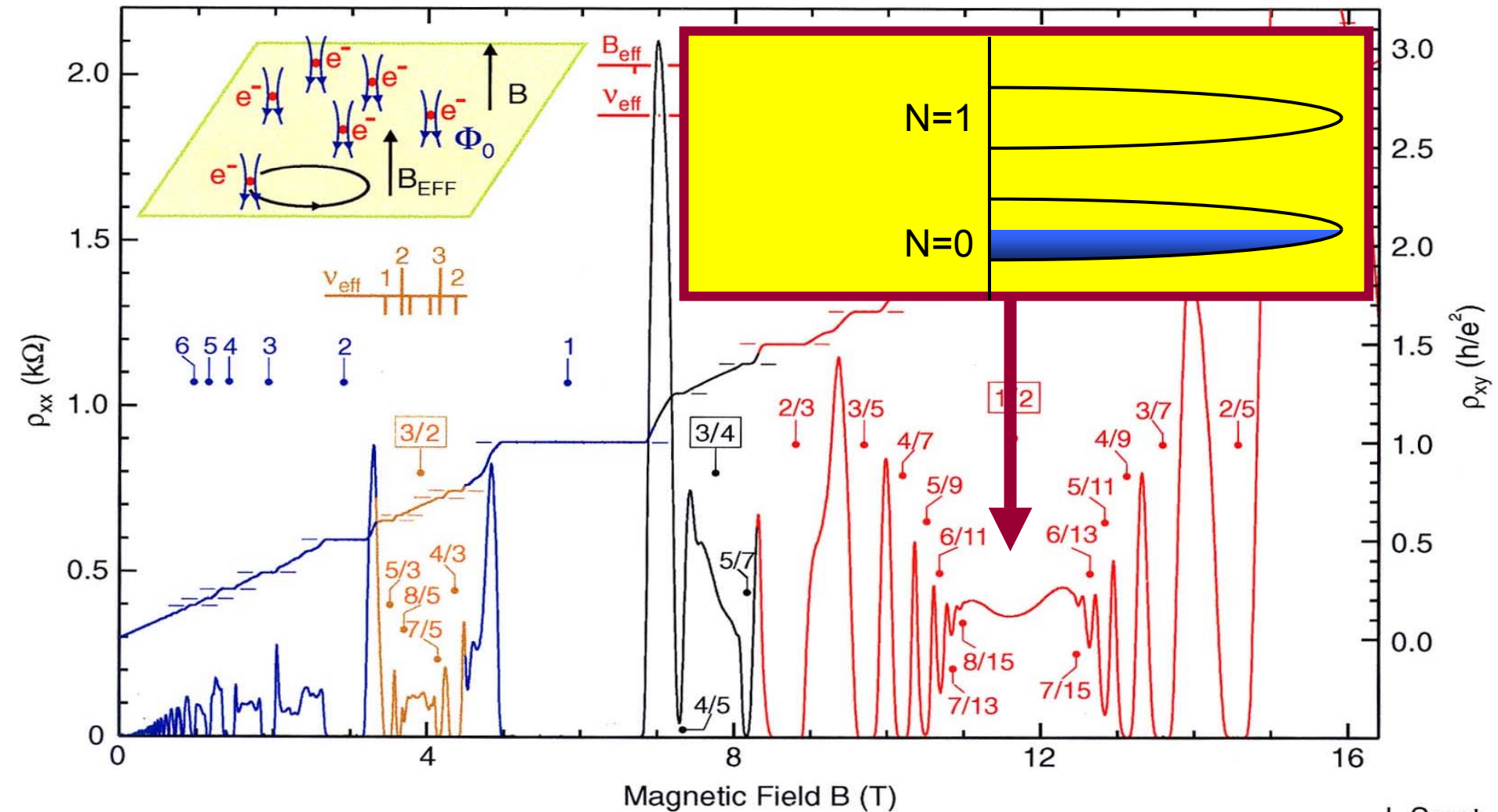
(Jörn Göres, J. Smet)

$$B_{\text{eff}} = B - 2 \Phi_0 n$$

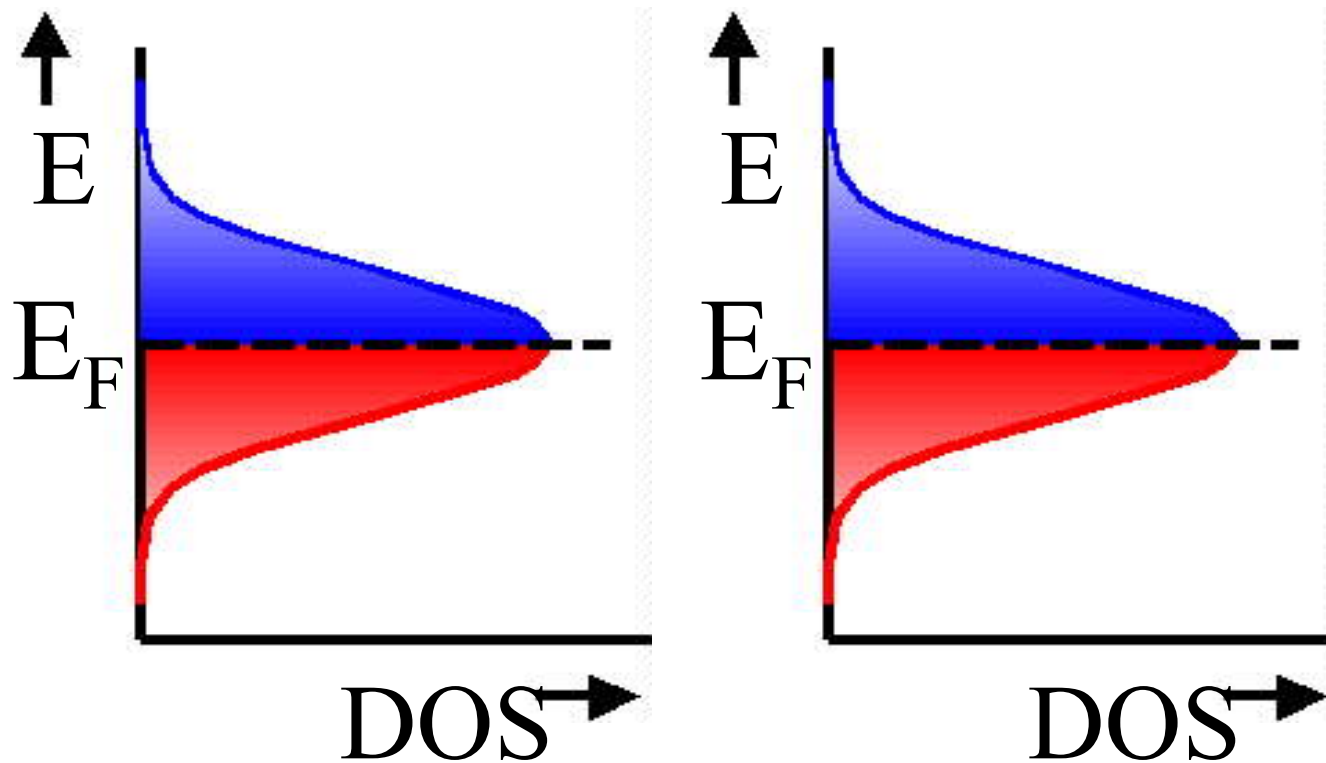
New QHE-phenomena for double-layer system



Integer (fractional) QHE

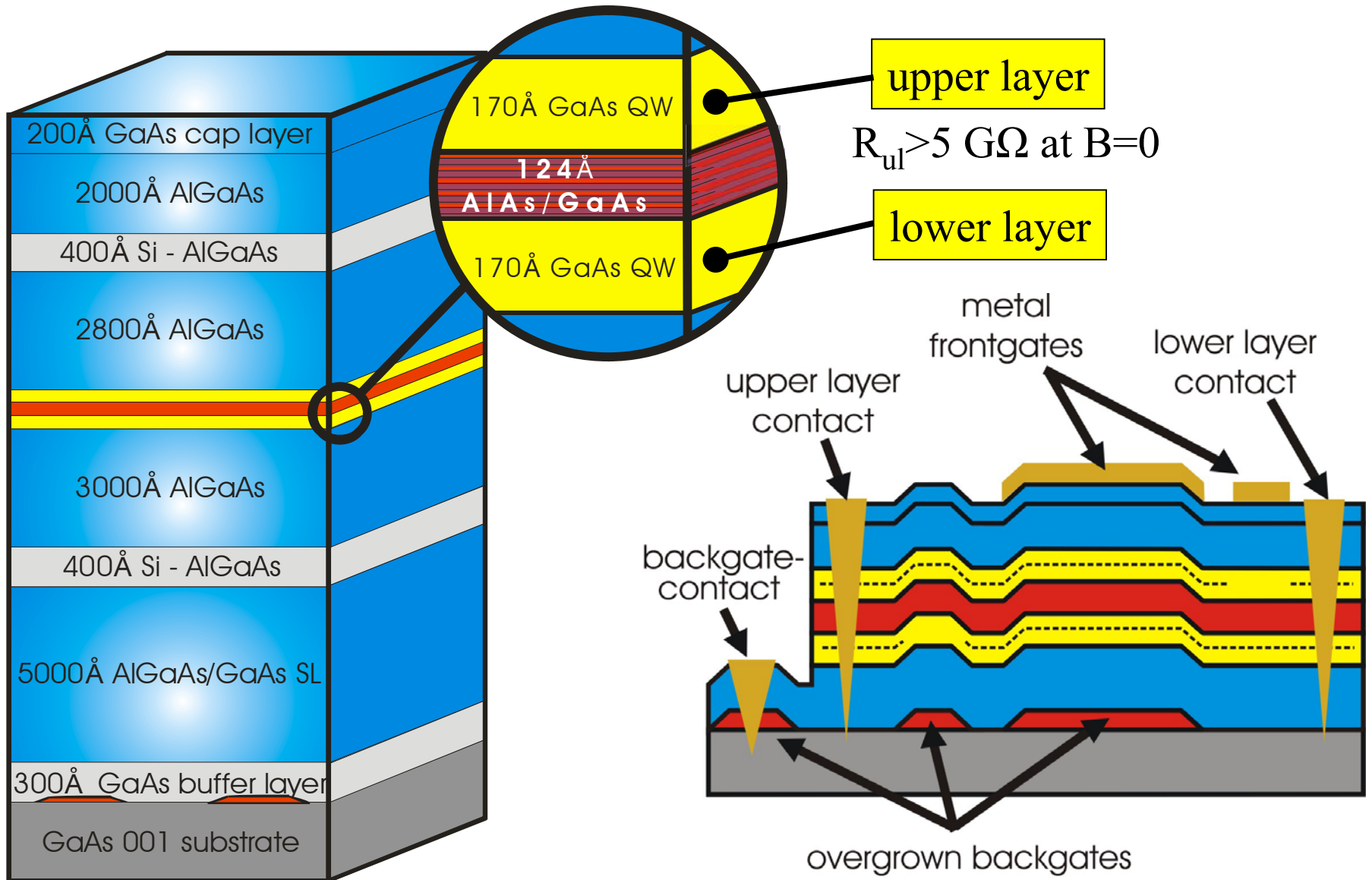


Coulomb interaction between two layers with half-filled bands!?

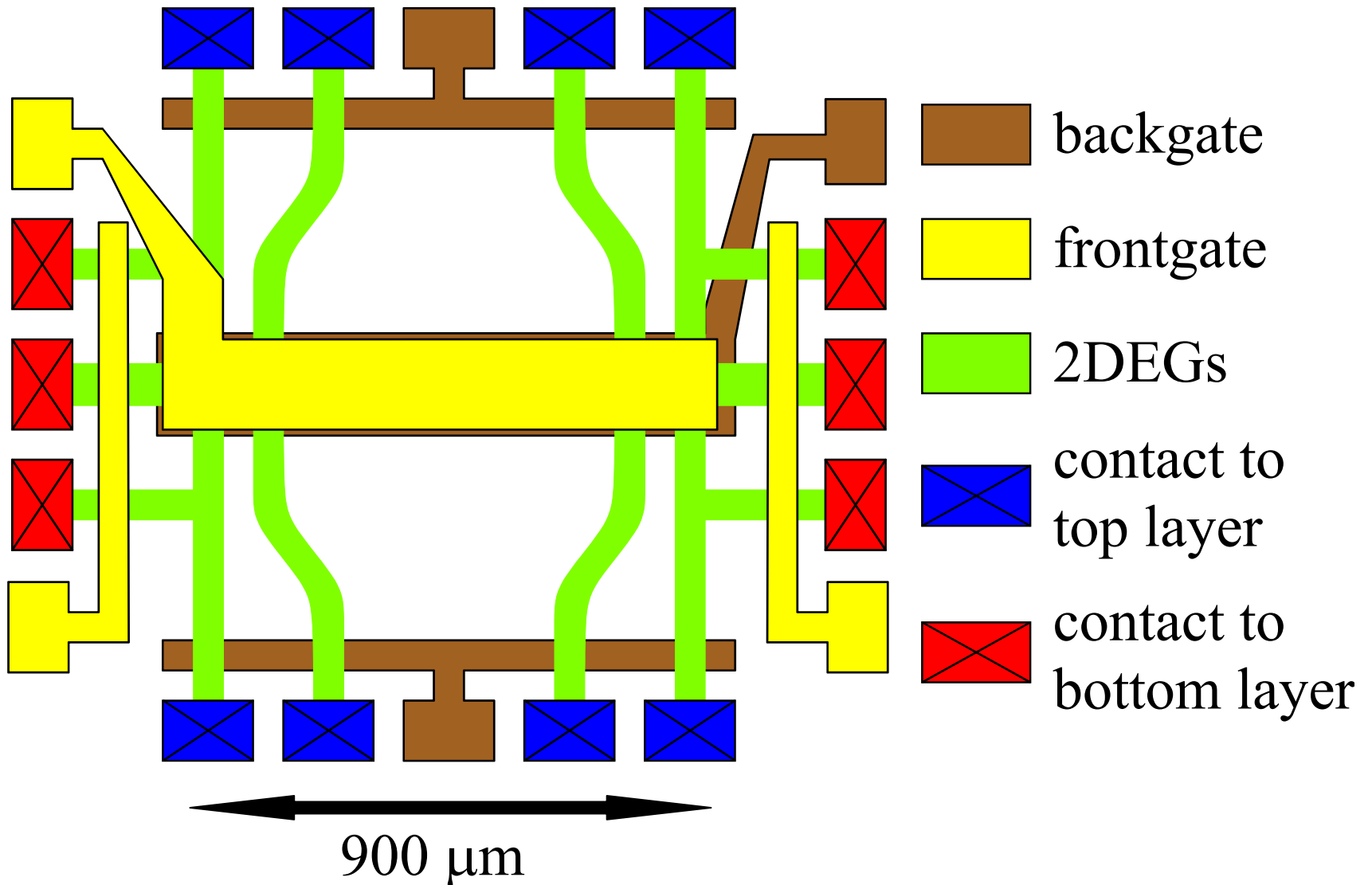


**Important parameter: distance d between the two layers
relative to the distance l_B between electrons within a layer**

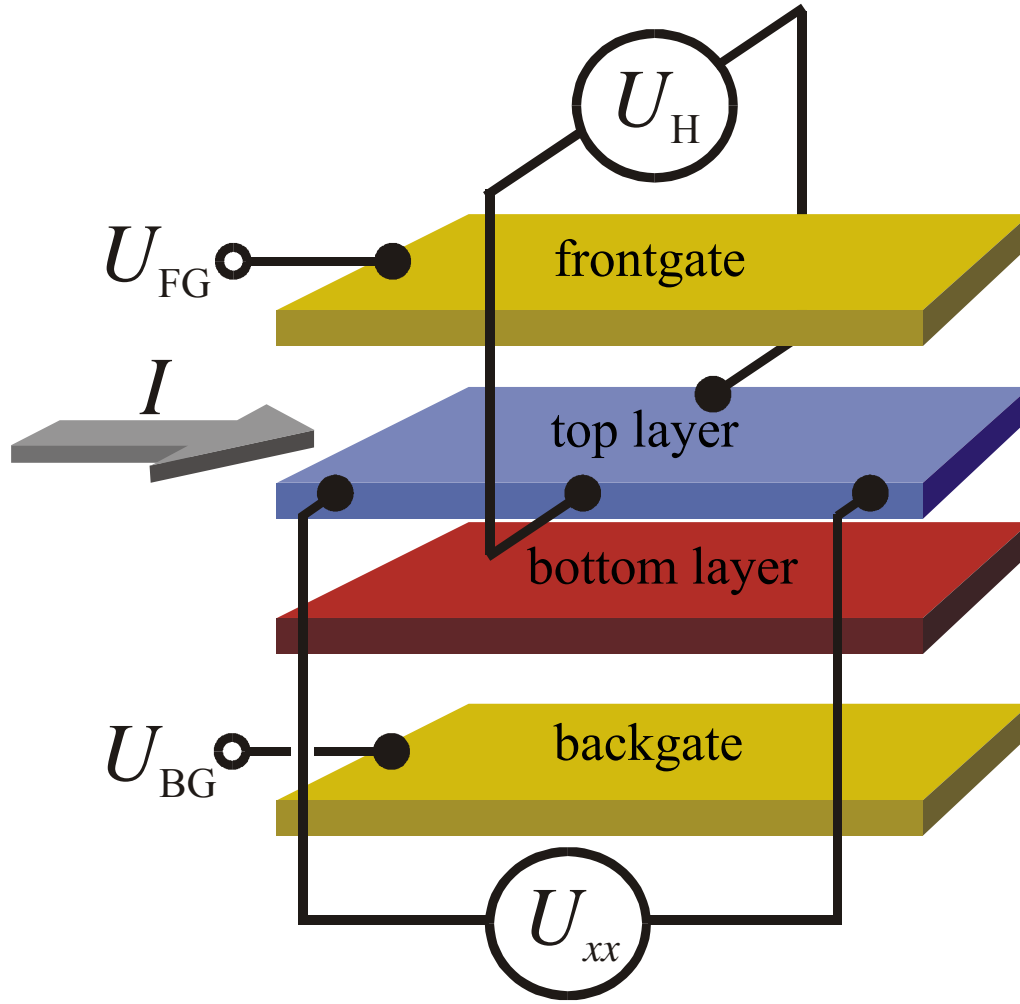
double layer system with separate electrical contacts (*group Dietsche*)



Double Layer Hall Device with separate contacts



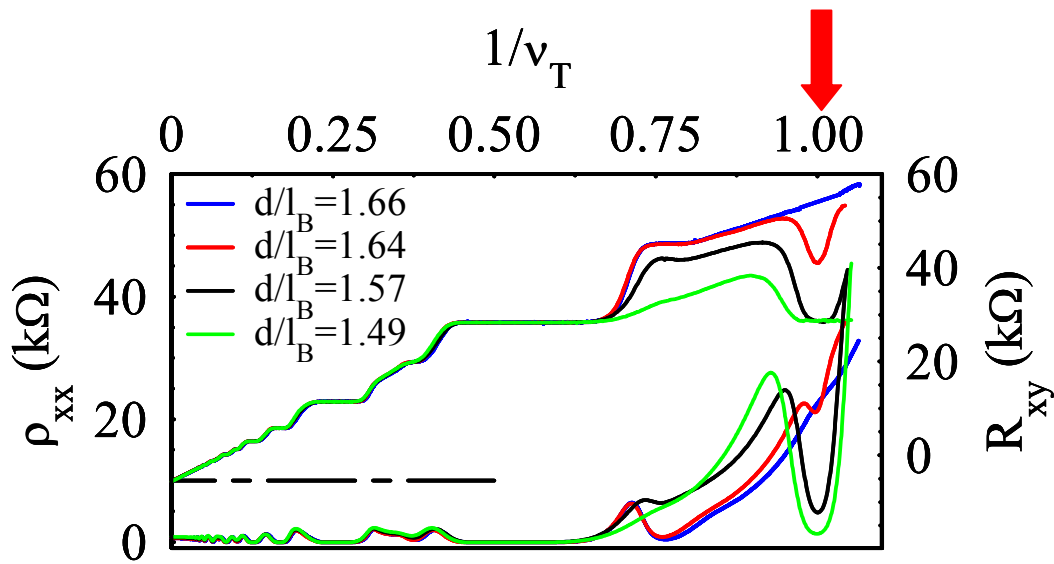
Bilayer el-el Systems



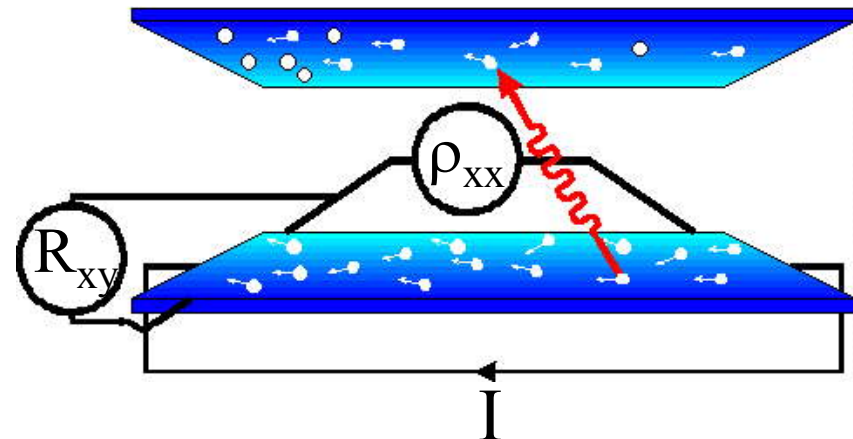
Au frontgate
20 nm GaAs
40 nm AlGaAs:Si
60 nm AlGaAs
15 nm GaAs
22 nm AlGaAs
15 nm GaAs
80 nm AlGaAs
40 nm AlGaAs:Si
300 nm superlattice
<i>n</i>+ backgate

Variation of d/l_B

(*R. Wiersma, S. Lok, S. Kraus, W. Dietsche*)

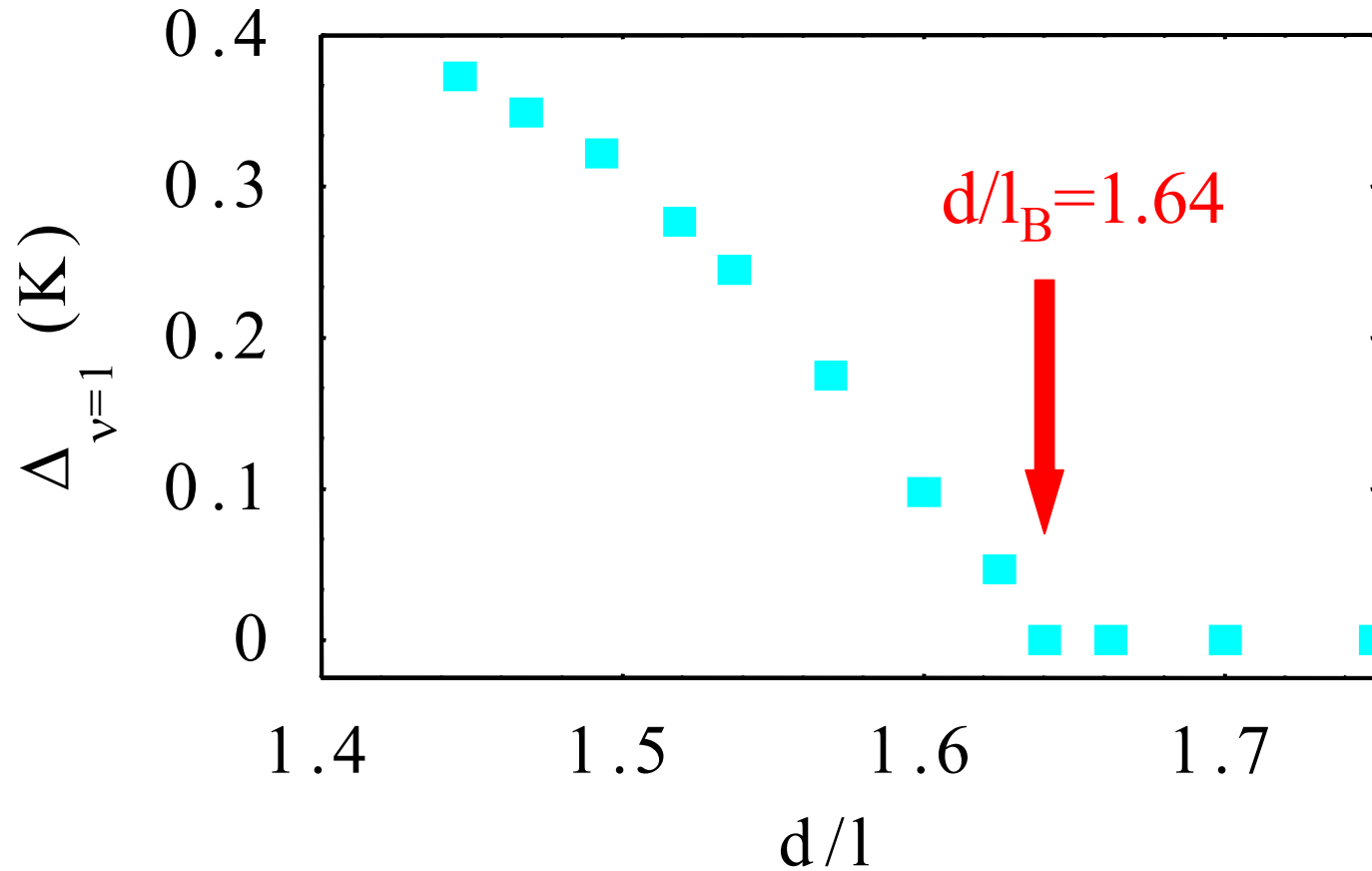


REDUCTION OF d/l_B
= smaller carrier density

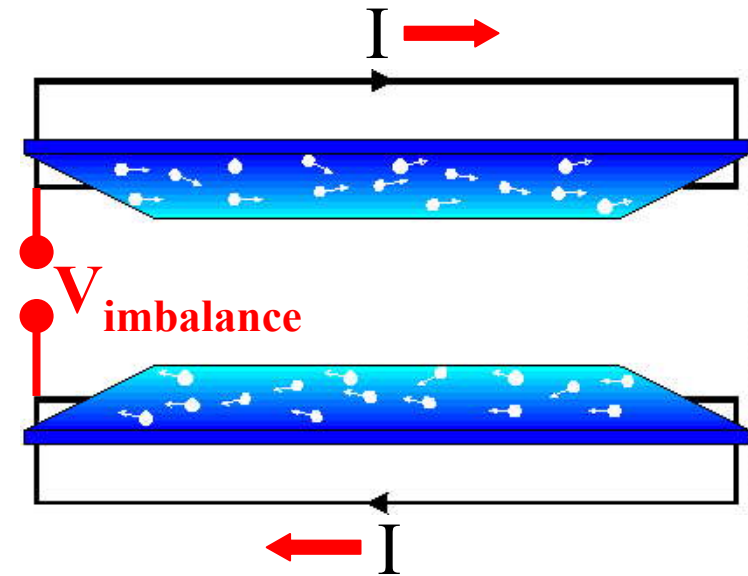
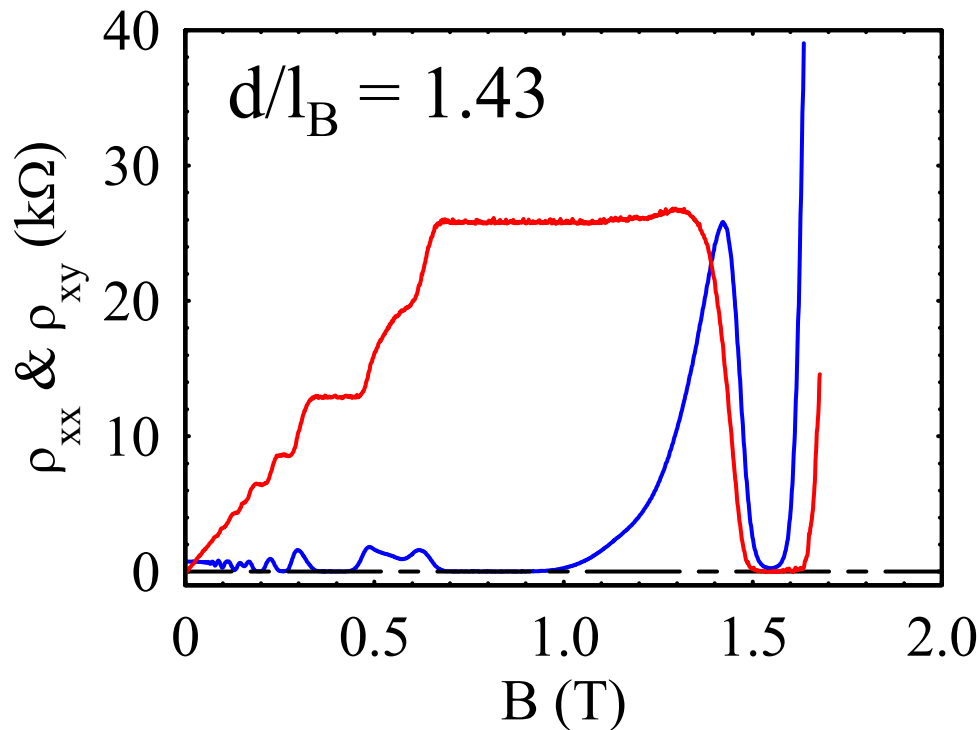


(Eisenstein 2003; Tutuc 2004; Wiersma 2004)

NEW GAP FOR TOTAL FILLING FACTOR $\nu = 1$ AT $d/l_B < 1.64$



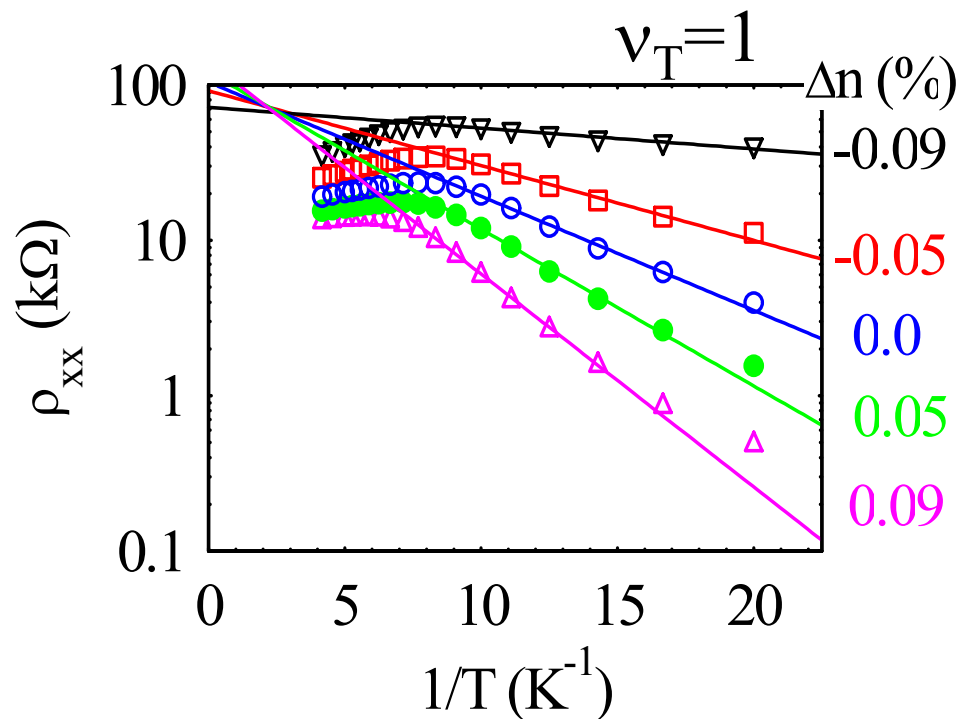
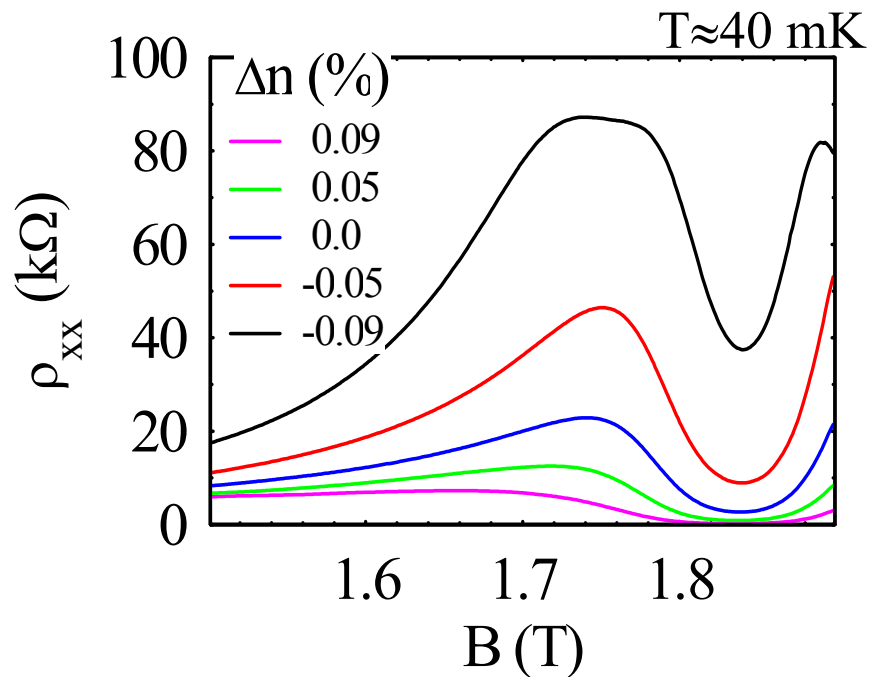
counter-current superfluidity



➤ with equal counter-flowing I , both ρ_{xx} and ρ_{xy} tend to zero

(Eisenstein 2004; Tutuc 2004; Wiersma 2004)

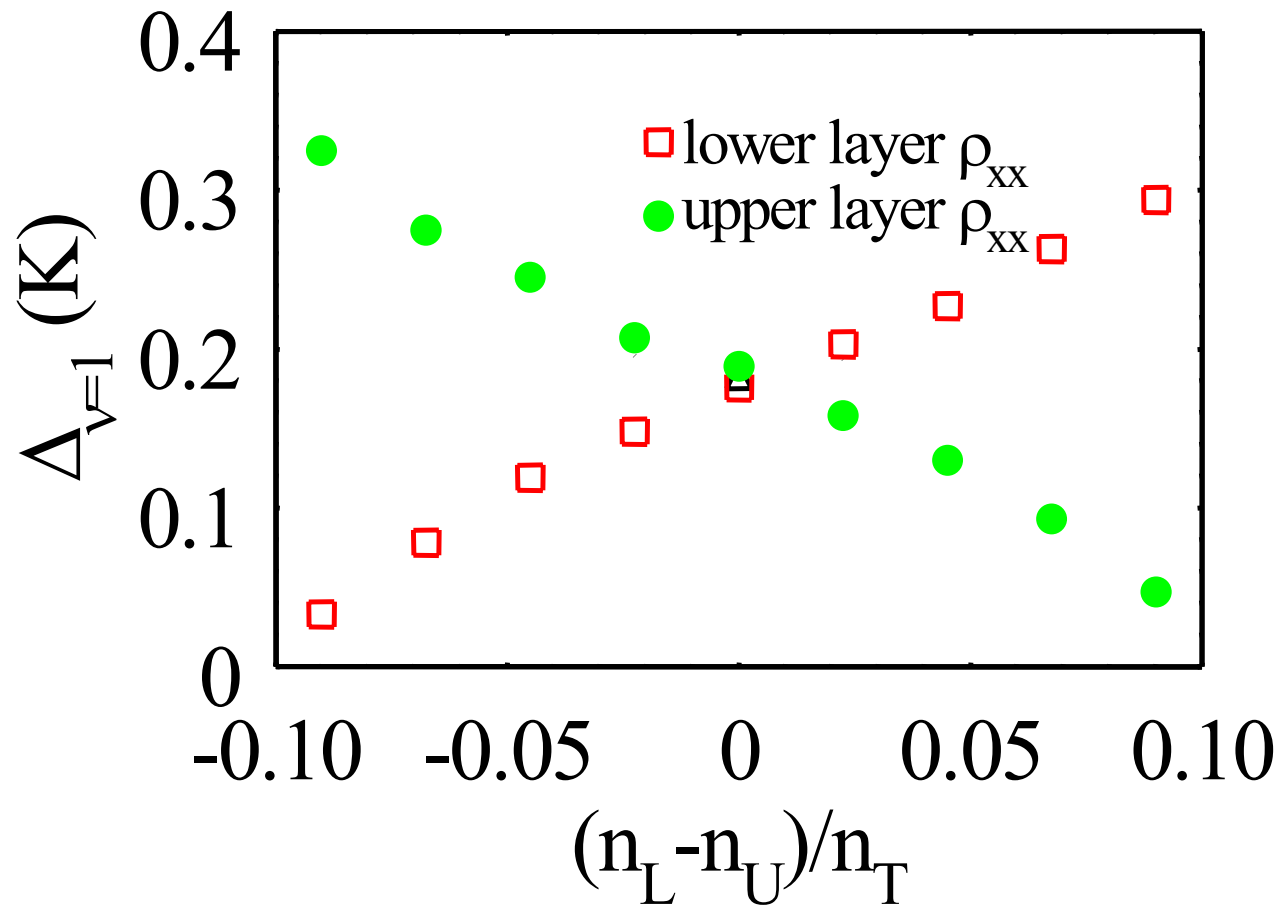
IMBALANCE AT TOTAL FILLING FACTOR 1 (e.g. $\nu_l=0.49$ and $\nu_u=0.51$)



the total filling factor remains 1, but charge is transferred from layer1 to layer2

- **The two layers behave very differently upon a symmetric density imbalance.....**
- **Larger energy gap for layer with larger carrier density**

Activation energy at $v_{\text{tot}}=1$ for each layer as
function of imbalance



➤ Asymmetric activation energy upon symmetric
density imbalance

SUMMARY

**THE USE OF THE QHE IN METROLOGY IS
THE MOST IMPORTANT APPLICATION
OF THIS EFFECT BUT MORE GENERAL:
TWO-DIMENSIONAL SYSTEMS IN
STRONG MAGNETIC FIELDS ARE MODEL
SYSTEMS FOR MANY FUNDAMENTAL
PHENOMENA IN SOLID STATE PHYSICS!**